



Probing loop currents and collective modes of charge density waves in Kagome materials with NV centers



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Recently, the unconventional charge density wave (CDW) order with loop currents has attracted considerable attention in the Kagome material family AV_3Sb_5 ($A = K, Rb, Cs$). However, experimental signatures of loop current order remain elusive. In this work, based on the mean-field free energy, we analyze the collective modes of unconventional CDW order in a Kagome lattice model. Furthermore, we point out that phase modes in the imaginary CDW (iCDW) order with loop current orders result in time-dependent stray fields. We thus propose using nitrogen-vacancy (NV) centers to detect these time-dependent stray fields, providing a potential experimental approach to identifying loop current order.

In condensed matter physics, electron correlations can lead to the emergence of new states of matter with various electronic and spin orders. Loop current order is an intriguing electronic order that leads to local current loops in a material, spontaneously breaking time-reversal symmetry. In the late 1990s, in an effort to understand the pseudogap phase, C. M. Varma proposed that loop current order could exist within the CuO_2 unit cell of cuprates^{1,2}. However, the experimental identification of loop current order in cuprates remains challenging and controversial^{3–5}.

Recently, the newly discovered Kagome materials AV_3Sb_5 ($A = K, Rb, Cs$) have emerged as an alternative platform for exploring loop current order^{6–8}. In the AV_3Sb_5 family, various experimental signatures suggest the presence of unconventional charge density waves (CDWs) with time-reversal symmetry breaking, as indicated by scanning tunneling microscopy⁹, spin resonance (μSR)¹⁰, magneto-optical Kerr effect¹¹, and other techniques^{6–8}. To break time-reversal symmetry, theoretically proposed CDW orders in these Kagome materials often involve loop current order, where the order parameter is imaginary^{12–16}, leading to so-called imaginary charge density waves (iCDW). Despite significant progress in this field, there is still no definitive experimental evidence for loop current order in AV_3Sb_5 . Moreover, recent high-resolution polar Kerr measurements have instead suggested the absence of time-reversal symmetry breaking in the charge-ordered state of CsV_3Sb_5 ^{17,18}. The study of loop current order in Kagome materials continues to attract growing interest^{19–21}.

On the other hand, understanding the collective excitations of an ordered state is crucial for gaining deeper insights into its nature. Loop current fluctuations are known to give rise to various intriguing physical phenomena in strongly correlated systems^{22–24}. Recently, the amplitude

modes of charge order in CsV_3Sb_5 have been experimentally investigated^{25,26}, and the ultrafast control of charge order in Kagome metals has been numerically studied²⁷. Although many previous theoretical works have modeled iCDW order with loop currents^{12–16}, a simple theoretical analysis of their collective excitations remains elusive. Key open questions include whether the collective excitations of iCDW exhibit novel properties and whether these excitations can serve as a probe for detecting loop current order. These questions, along with recent experimental progress on Kagome materials, motivate the present study. Additionally, we are inspired by our previous work on real triple-Q CDW order parameters, where we analyzed phase shifts and band geometry effects²⁸. We now are curious about any interesting properties from the imaginary triple-Q CDW order related to the phase degree of freedom.

In this work, we theoretically analyze the collective excitations of triple-Q order parameters, including both real CDW (rCDW) and iCDW order, in a Kagome lattice model. We explicitly obtain the phase and amplitude modes and find a crucial distinction: in iCDW order, phase and amplitude modes mix, whereas in rCDW order, they remain decoupled. Furthermore, we propose that phase mode excitations can serve as a probe for detecting loop currents in the iCDW phase using nitrogen-vacancy (NV) centers, as loop current fluctuations generate magnetic noise. The proposed experimental setup is illustrated in Fig. 1. In the past, NV centers have been used or proposed for probing various correlated orders, including currents and chirality fluctuation in high temperature superconductors²⁹, anti-ferromagnetic order^{30–32}, conventional superconducting effects^{33–35}, and quantum spin liquids^{36,37} (see refs. 38,39 for a review). Our proposal provides new motivation for applying NV center detection in the search for loop current order.

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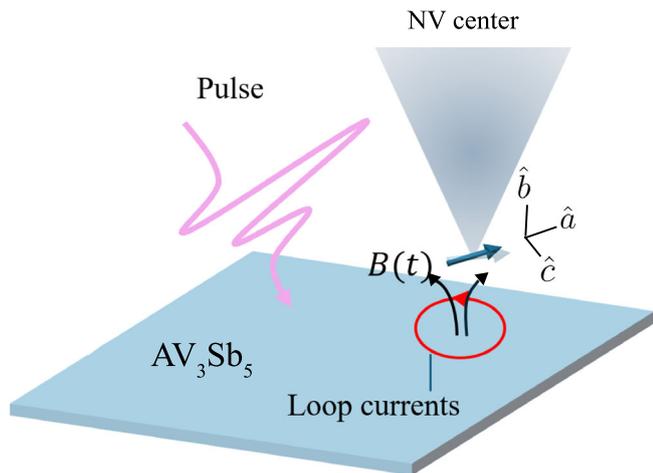


Fig. 1 | Schematic of the proposed setup to detect the loop current order using NV centers. In this setup, time-dependent magnetic fields arise from loop current fluctuations induced by a laser pulse. The corresponding magnetic noise can be detected by the NV center.

Results

Kagome lattice model with triple-Q CDW

To set the stage, we briefly recall the Kagome lattice model. The Kagome lattice is shown in Fig. 2a, with the corresponding point group symmetry being D_{6h} . Each unit cell consists of three sublattices: A, B, and C. The unit vectors are given by $\mathbf{a}_1 = (2, 0)a$ and $\mathbf{a}_2 = (1, \sqrt{3})a$, where a is the bond length. The energy bands with nearest-neighbor hopping t are shown in Fig. 2b. In the AV_3Sb_5 family, the chemical potential is near the Van Hove singularity points (red dashed line), which plays a crucial role in inducing various symmetry-breaking orders. Fig. 2c depicts the Brillouin zone. The Van Hove singularity points are located at three distinct M points: M_1 , M_2 , and M_3 . The Bloch wavefunctions at the M_1 , M_2 , and M_3 points arise from the A, B, and C sublattices, respectively.

The coupling between the Van Hove singularity points leads to charge instability. In experiments on AV_3Sb_5 materials, a 2×2 CDW order has been observed using scanning tunneling microscopy (STM)^{9,40,41}. As demonstrated previously^{14,19}, a natural way to generate such a CDW order is through a triple-Q coupling, with $\mathbf{Q}_1 = (\frac{\sqrt{3}}{2}, -\frac{1}{2})|M|$, $\mathbf{Q}_2 = (-\frac{\sqrt{3}}{2}, -\frac{1}{2})|M|$, and $\mathbf{Q}_3 = (0, 1)|M|$, where $|M| = \frac{\pi}{\sqrt{3}a}$ [Fig. 2c]. The three \mathbf{Q} vectors induce coupling between the M points, and the folded Brillouin zone is highlighted by the gray lines in Fig. 2c. The ansatz for the CDW order is given by:

$$\Delta_{CDW}(\mathbf{r}) = \begin{pmatrix} 0 & \Delta_{Q_3}(\mathbf{r}) & \Delta_{Q_2}^*(\mathbf{r}) \\ \Delta_{Q_3}(\mathbf{r})^* & 0 & \Delta_{Q_1}(\mathbf{r}) \\ \Delta_{Q_2}(\mathbf{r}) & \Delta_{Q_1}^*(\mathbf{r}) & 0 \end{pmatrix}, \quad (1)$$

where $\Delta_{Q_j}(\mathbf{r}) = |\Delta_{Q_j}|e^{i(\mathbf{Q}_j \cdot \mathbf{r} + \theta_j)}$, and the basis is (c_A, c_B, c_C) , with c being the electron annihilation operator. Here, we define the phase degree of freedom of order parameter Δ_{Q_j} as θ_j .

It is important to note that the CDW order parameters can be complex due to the phase degree of freedom θ_j . Because of the commensurability of this triple-Q CDW, the values of θ_j are not arbitrary and must be determined by minimizing the free energy, as discussed in the following section.

Phenomenologically, the mean-field free energy can be expanded as a series in powers of the order parameter $\Delta_{\mathbf{Q}}$. In the triple-Q case, the allowed terms are of the form $\Delta_{Q_1}^{n_1} \Delta_{Q_2}^{n_2} \Delta_{Q_3}^{n_3}$, where $\sum_{n_i} n_i \mathbf{Q}_i = \mathbf{G}$. Here, n_i are integers, \mathbf{G} represents the reciprocal lattice vectors, and we define $\Delta_{Q_i}^{n_i} = (\Delta_{Q_i})^{n_i}$ when $n_i \geq 0$, and $\Delta_{Q_i}^{n_i} = (\Delta_{Q_i}^*)^{|n_i|}$ when $n_i < 0$. For the CDW with triple-Q vectors shown in Fig. 2, the free energy up to the fourth order is given

by^{12,13,42–44}

$$F \approx \sum_{\alpha} (b \cos 2\theta_{\alpha} - \lambda'_{\alpha}) |\Delta_{Q_{\alpha}}|^2 + \lambda_2 |\Delta_{Q_1}| |\Delta_{Q_2}| |\Delta_{Q_3}| \cos(\theta_1 + \theta_2 + \theta_3) + \lambda_3 |\Delta_{Q_1}| |\Delta_{Q_2}| |\Delta_{Q_3}| \cos(\theta_1) \cos(\theta_2) \cos(\theta_3) + u_1 \left(\sum_{\alpha} |\Delta_{Q_{\alpha}}|^4 \right) + u_2 \sum_{\alpha \neq \beta} |\Delta_{Q_{\alpha}}|^2 |\Delta_{Q_{\beta}}|^2. \quad (2)$$

According to ref. 13, the phenomenological free energy can also be derived from the specific electron-electron interactions (see Supplementary Information for details), where λ_3 is zero. To reduce number of parameters, we adopt the convention of ref. 13 with $\lambda_3 = 0$, and the C_3 symmetry that requires $\theta_1 = \theta_2 = \theta_3 = \theta_0$ and $|\Delta_{Q_1}| = |\Delta_{Q_2}| = |\Delta_{Q_3}|$ [Supplementary Information Note 1]. Since the dominant term is the second-order term, the free energy is minimized when $\theta_0 = \frac{\pi}{2}$ or $-\frac{\pi}{2}$ for $b > 0$, which corresponds to the iCDW phase. On the other hand, the free energy is minimized when $\theta_0 = 0$ or π for $b < 0$, which corresponds to the rCDW phase. The phase diagram is sketched in Fig. 2d. The sign of b is closely related to the interactions. Note that if $\lambda_2 < 0$ ($\lambda_2 > 0$), the rCDW phase with $\theta_0 = 0$ ($\theta_0 = \pi$) is more favorable than with $\theta_0 = \pi$ ($\theta_0 = 0$) due to the third-order term.

We emphasize that the microscopic origin of the interactions driving the CDW is not the focus of this work. The phenomenological free energy in Eq. (2) applies to both electron-electron and electron-phonon interactions. Depending on the type of interaction (electron-electron or electron-phonon), the second- to fourth-order terms in the free energy F can be represented by the Feynman diagrams shown in Fig. 2e.

Collective modes analysis

We are now ready to analyze the collective modes based on the phenomenological free energy. By incorporating the fluctuations of the CDW order parameters, the Lagrangian is given by

$$\mathcal{L} = \sum_{\alpha} \kappa_0 |\partial_{\tau} \Delta_{Q_{\alpha}}|^2 + \kappa_1 |\nabla \Delta_{Q_{\alpha}}|^2 + (b \cos 2\theta_{\alpha} - \lambda'_{\alpha}) |\Delta_{Q_{\alpha}}|^2 + \lambda_2 |\Delta_{Q_1}| |\Delta_{Q_2}| |\Delta_{Q_3}| \cos(\theta_1 + \theta_2 + \theta_3) + u_1 \sum_{\alpha} |\Delta_{Q_{\alpha}}|^4 + u_2 \sum_{\alpha \neq \beta} |\Delta_{Q_{\alpha}}|^2 |\Delta_{Q_{\beta}}|^2. \quad (3)$$

The first two terms in \mathcal{L} describe the time and spatial fluctuations, respectively. To obtain the phase and amplitude modes, we rewrite the order parameters as $\Delta_{Q_{\alpha}, \mathbf{q}} \approx \Delta_{Q_{\alpha}} (1 + \mathcal{A}_{\alpha}(\mathbf{q})) e^{i(\theta_{\alpha} + \theta_{\alpha}(\mathbf{q}))}$. Using the C_3 symmetry, the amplitude modes can be projected into the A and $E_{1,2}$ irreducible representations:

$$\mathcal{A}_q^{(A)} = \frac{1}{\sqrt{3}} (\mathcal{A}_1(q) + \mathcal{A}_2(q) + \mathcal{A}_3(q)), \quad (4)$$

$$\mathcal{A}_q^{(E_1)} = \frac{1}{\sqrt{2}} (\mathcal{A}_1(q) - \mathcal{A}_3(q)), \quad (5)$$

$$\mathcal{A}_q^{(E_2)} = \frac{1}{\sqrt{6}} (\mathcal{A}_1(q) - 2\mathcal{A}_2(q) + \mathcal{A}_3(q)), \quad (6)$$

where $q = (\mathbf{q}, \omega)$ and ω is the frequency. The phase modes can be projected into the following channels:

$$\theta_q^{(A)} = \frac{1}{\sqrt{3}} (\theta_1(q) + \theta_2(q) + \theta_3(q)), \quad (7)$$

$$\theta_q^{(E_1)} = \frac{1}{\sqrt{2}} (\theta_1(q) - \theta_3(q)), \quad (8)$$

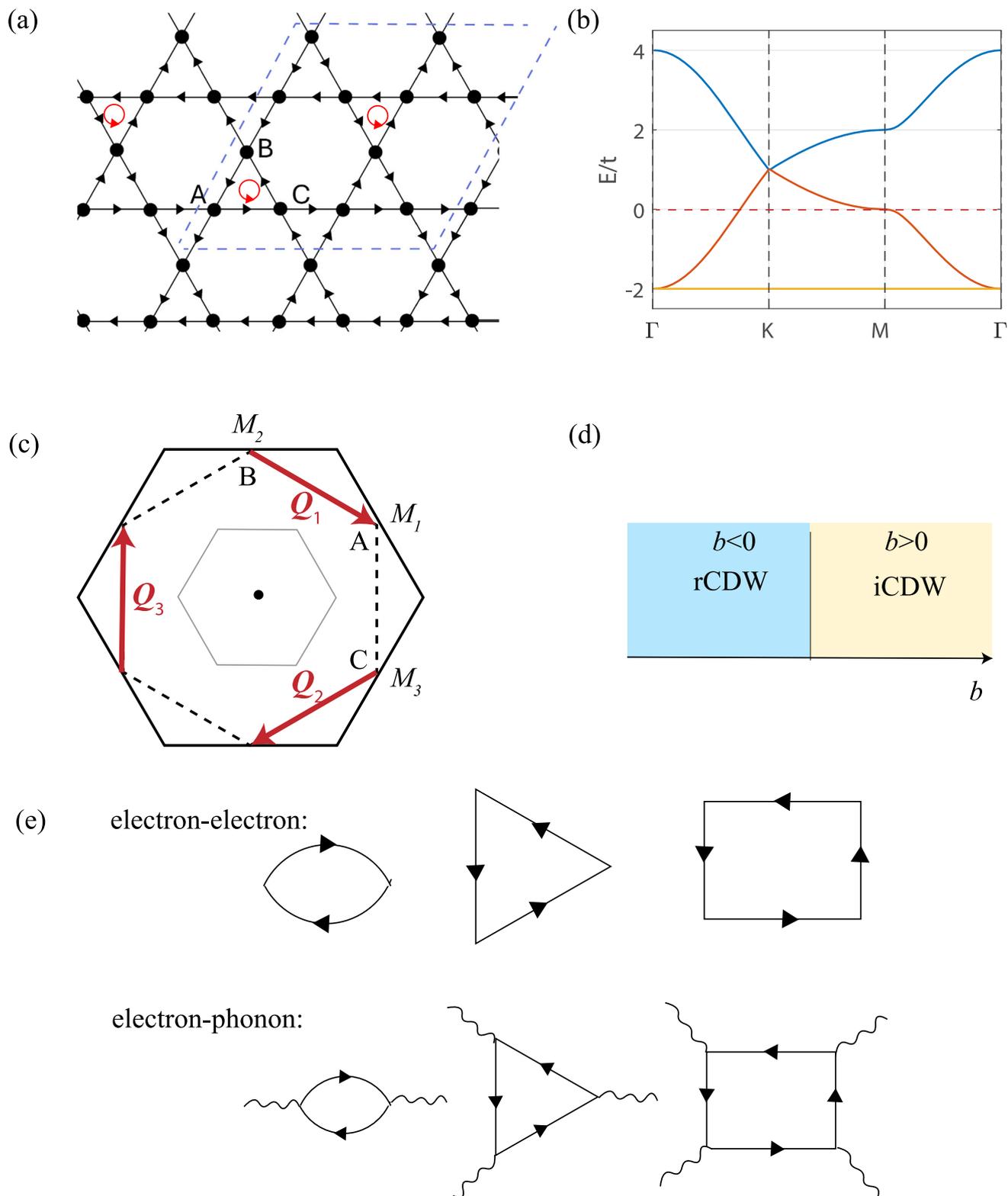
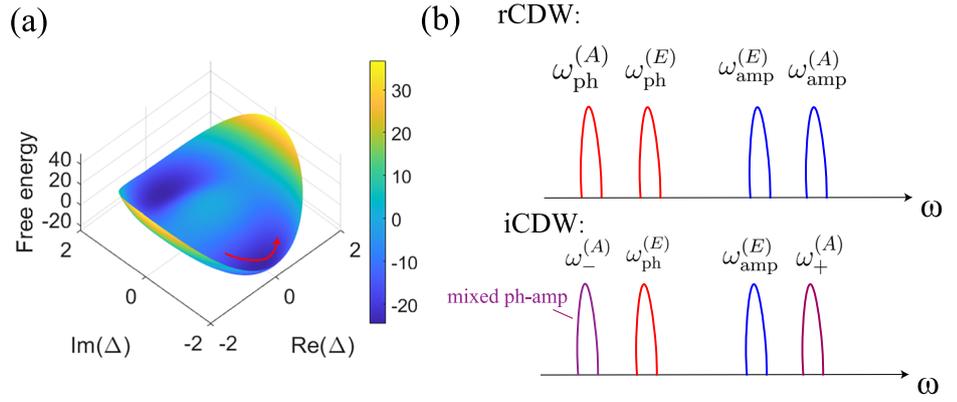


Fig. 2 | Kagome lattice model. **a** The Kagome lattice with triple-Q CDW order. Here, A, B, and C label the three sublattices, and the phases are indicated by the arrows in the iCDW phase. The red circles are the loop currents in the small triangle plaquettes. **b** The single-particle electronic band structure of the Kagome lattice toy model. **c** The schematic plot of the original Brillouin zone (black solid line) and the

folded Brillouin zone (gray line). The M points, with wavefunctions localized on the A, B, and C sublattices, are highlighted. **d** A schematic phase diagram controlled by b in Eq. (2). When $b < 0$ ($b > 0$), the rCDW (iCDW) phase tends to be favored. **e** The Feynman diagram representation for the free energy terms (top panel for electron-electron interaction, bottom panel for electron-phonon interaction).

Fig. 3 | The CDW collective excitations. **a** The free energy landscape from Eq. (2) with parameters $b = 1$, $\lambda'_1 = 5$, $\lambda_2 = 0.1$, $\lambda_3 = 0$, $u_1 = 0.5$, and $u_2 = 0.5$. The red arrow represents the fluctuation of the complex order parameter. **b** A schematic plot of the spectral arrangement of phase (red) and amplitude (blue) modes for rCDW and iCDW orders. Here, the phase and amplitude modes in the A channel mix (purple), while they remain uncoupled for E modes.



$$\theta_q^{(E_2)} = \frac{1}{\sqrt{6}}(\theta_1(q) - 2\theta_2(q) + \theta_3(q)). \quad (9)$$

As shown in Supplementary Information Note 2, the fluctuation part of the Lagrangian can be simplified as

$$\begin{aligned} \mathcal{L}_{\text{fluc}}(\omega, \mathbf{q}) = & (\kappa_1 \mathbf{q}^2 - \kappa_0 \omega^2 + 4(u_1 + 2u_2)|\Delta_Q|^2) \mathcal{A}_q^{(A)} \mathcal{A}_{-q}^{(A)} \\ & + (\kappa_1 \mathbf{q}^2 - \kappa_0 \omega^2 + 2|b| - \frac{3}{2}\lambda_2 |\Delta_Q| \cos(3\theta_0)) \theta_q^{(A)} \theta_{-q}^{(A)} \\ & + \frac{3}{2}\lambda_2 |\Delta_Q| \sin(3\theta_0) (\mathcal{A}_q^{(A)} \theta_{-q}^{(A)} + \mathcal{A}_{-q}^{(A)} \theta_q^{(A)}) \\ & + (\kappa_1 \mathbf{q}^2 - \kappa_0 \omega^2 + 2|b|) (\theta_q^{(E_1)} \theta_{-q}^{(E_1)} + \theta_q^{(E_2)} \theta_{-q}^{(E_2)}) \\ & + (\kappa_1 \mathbf{q}^2 - \kappa_0 \omega^2 - \frac{3}{2}\lambda_2 \cos(3\theta_0) |\Delta_Q| \\ & + 4(u_1 - u_2) |\Delta_Q|^2) (\mathcal{A}_q^{(E_1)} \mathcal{A}_{-q}^{(E_1)} + \mathcal{A}_q^{(E_2)} \mathcal{A}_{-q}^{(E_2)}). \end{aligned} \quad (10)$$

Here, the A - and E -modes are separated due to the C_3 symmetry. As expected, both the phase and amplitude modes are gapped in this commensurate triple-Q CDW. More intuitively, the free energy landscape exhibits local minima in the complex Δ plane, and fluctuations around these local minima give rise to the massive modes (see Fig. 3a for an illustration). Interestingly, we observe a mixing term between the phase mode and amplitude mode, $\propto \sin(3\theta_0) (\mathcal{A}_q^{(A)} \theta_{-q}^{(A)} + \mathcal{A}_{-q}^{(A)} \theta_q^{(A)})$. This term is finite in the iCDW phase with $\theta_0 = \frac{\pi}{2}, -\frac{\pi}{2}$, and vanishes for rCDW with $\theta_0 = 0, \pi$. For rCDW, a direct mixing term between phase and amplitude modes that breaks time-reversal symmetry is not allowed. An example of such a forbidden term is $(\beta_1 + \beta_2 \cos(3\theta_0)) (\mathcal{A}_q^{(A)} \theta_{-q}^{(A)} + \mathcal{A}_{-q}^{(A)} \theta_q^{(A)})$. Note that under the time-reversal operation, $\theta_q \mapsto -\theta_{-q}$, $\mathcal{A}_q \mapsto \mathcal{A}_{-q}$, and $\theta_0 \mapsto -\theta_0$. It can also be seen that all terms in $\mathcal{L}_{\text{fluc}}(\omega, \mathbf{q})$ are time-reversal even.

The mixed Higgs and phase modes in the iCDW (at $\mathbf{q} = 0$, i.e., M points) respect

$$\begin{vmatrix} -\kappa_0 (\omega^{(A)})^2 + 4(u_1 + 2u_2) |\Delta_Q|^2 & \frac{3}{2} \lambda_2 \sin(3\theta_0) |\Delta_Q| \\ \frac{3}{2} \sin(3\theta_0) \lambda_2 |\Delta_Q| & -\kappa_0 (\omega^{(A)})^2 + 2|b| \end{vmatrix} = 0. \quad (11)$$

This gives

$$\begin{aligned} \kappa_0 (\omega_{\pm}^{(A)})^2 = & |b| + 2(u_1 + 2u_2) |\Delta_Q|^2 \\ & \pm \sqrt{(|b| - 2(u_1 + 2u_2) |\Delta_Q|^2)^2 + \frac{9}{4} \lambda_2^2 |\Delta_Q|^4}. \end{aligned} \quad (12)$$

Here, $\omega_{\pm}^{(A)}$ denotes the energy of the mixed phase-amplitude mode. We summarize the expected collective mode spectrum for rCDW and iCDW in Fig. 3b. Note that the ordering of these modes along the frequency axis, depending on parameters, may differ from that shown in Fig. 3b.

Loop current detection with NV Centers

The phase fluctuation in the iCDW phase is particularly interesting because it implies that the magnetic flux associated with the loop current order is dynamic, generating a time-varying magnetic stray field. The iCDW order effectively mediates imaginary inter-sublattice hopping, which gives rise to current within each bond¹². The phase of iCDW order or bound current direction is illustrated with black arrows in Fig. 2a^{14,19}. The loop currents appear when the arrows are connected in a clockwise or counterclockwise direction within each plaquette. According to the Peierls substitution principle, the flux within these small triangular plaquettes is given by the sum of the phases: $\propto \sum_{\alpha} \theta_{\alpha} = \sqrt{3} \theta^{(A)}$. Note that such flux is absent for rCDW, as the order parameter is real and does not break time-reversal symmetry. When the A_1 phase mode is excited, we expect that the average flux of the system with iCDW order will oscillate in time as

$$\tilde{\Phi}(t) = \tilde{\Phi}_0 + \delta\tilde{\Phi} \sin(\omega_{\text{ph}}^{(A)} t). \quad (13)$$

Here, $\tilde{\Phi}_0$ is the static flux, and $\delta\tilde{\Phi}$ represents the amplitude of the fluctuating part. This dynamic flux is expected to generate magnetic noise, which can potentially be detected by an NV center detector³⁹.

The coupling between the stray field $\mathbf{B}(t)$ and the NV center is described by the Hamiltonian $H_{\text{NV}} = D_{\text{zfs}} \hat{S}_a^2 - \gamma_e B_0 \hat{S}_a - \gamma_e \mathbf{B}(t) \cdot \mathbf{S}$ ³⁹. Here, \hat{a} is along the quantization axis of the NV center, $D_{\text{zfs}} = 2\pi \times 2.87$ GHz is the zero-field splitting, $\gamma_e = -2\pi \times 28.02$ GHz \cdot T⁻¹ is the electron g-factor, and B_0 is a static magnetic field. The NV center exhibits two operational modes: T_1 spectroscopy and T_2 spectroscopy. Specifically, the T_1 relaxation time describes how quickly the spin population of the NV center in the $m_s = \pm 1$ states decays to the lower-energy $m_s = 0$ state, while T_2 describes the coherent dephasing time of the NV spin. The T_2 spectroscopy is primarily sensitive to low-frequency noise (Hz–MHz), while T_1 spectroscopy is sensitive to fluctuating magnetic fields at the NV's Larmor frequency (up to GHz or sub-THz regions). For example, recently proposed magnon noise (in the range of 10–100 GHz)³¹ was observed experimentally using NV relaxometry³². Moreover, recent advances in high-field NV spectroscopy have enabled the detection of magnetic noise in the sub-THz region^{45,46}. In our scenario, if the iCDW is commensurate, the phase mode gap is determined by the strength of the lattice pinning of the CDW, typically in the sub-THz region. In fact, it has been demonstrated that the CDW can be tuned into an incommensurate state by doping Kagome materials such as $\text{CsV}_3\text{Sb}_{5-x}\text{Sn}_x$ ⁴⁷, where the phase mode becomes soft.

The experimental setup we propose is shown in Fig. 1. In the iCDW phase, loop current fluctuations can be induced by an external laser pulse, exciting the phason modes. The overall geometry is similar to that used to probe magnon noise arising from non-collinear antiferromagnetic textures recently³². Let us perform a qualitative estimation of the T_1 relaxation time

induced by phason modes. According to Fermi's golden rule³⁹:

$$T_1^{-1} = \frac{3}{2} \gamma_e^2 S_B(\omega_0), \quad (14)$$

$$S_B(\omega) = \int dt e^{-i\omega t} \langle B_+(t) B_-(0) \rangle. \quad (15)$$

where ω_0 is the frequency detected by the NV center, $B_{\pm} = B_b \pm iB_c$, and \hat{b}, \hat{c} are the coordinate axes perpendicular to \hat{a} . Since the dynamics of the strip field $B(t)$ arise from the phase mode, we expect $B(t)$ to exhibit the frequency of $\omega_{ph}^{(A)}$. Therefore,

$$T_1^{-1} \sim \frac{\gamma_e^2 |B|^2}{\omega_0 - \omega_{ph}^{(A)}}. \quad (16)$$

Note that, according to the Biot-Savart law, $|B|$ depends on the distance of the NV tip from the sample. We take the local field B to be on the order of 0.01 ~ 0.1 mT, based on the orbital magnetization given in ref.^{48,19} (though it may differ in practice). Choosing $\omega_0 - \omega_{ph} \sim 10$ GHz, we estimate $T_1 \sim 10$ –1000 μ s, which falls within the sensitivity range of the NV center.^{32,39}

Discussion

In summary, we have provided a phenomenological analysis of the phase and amplitude modes of unconventional CDWs in Kagome lattice materials. Importantly, we have highlighted that the loop current order embedded in these unconventional CDWs can be probed with NV centers by exciting phase modes. We anticipate that the relevant experimental progress will significantly contribute to the search for loop current orders in real materials. Furthermore, it is also interesting to extend our experimental proposal to cuprates and explore the connection between loop current fluctuations and NV center detections in high-temperature superconductors²⁹.

Data availability

No datasets were generated or analyzed during the current study.

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References

- Varma, C. M. Non-Fermi-liquid states and pairing instability of a general model of copper oxide metals. *Phys. Rev. B* **55**, 14554–14580 (1997).
- Varma, C. M. Pseudogap phase and the quantum-critical point in copper-oxide metals. *Phys. Rev. Lett.* **83**, 3538–3541 (1999).
- Bourges, P., Bounoua, D. & Sidis, Y. Loop currents in quantum matter. *Comptes Rendus. Phys.* **22**, 7–31 (2021).
- Croft, T. P. et al. No evidence for orbital loop currents in charge-ordered YBa₂Cu₃O_{6+x} from polarized neutron diffraction. *Phys. Rev. B* **96**, 214504 (2017).
- Gheidi, S. et al. Absence of μ SR evidence for magnetic order in the pseudogap phase of Bi_{2+x}Sr_{2-x}CaCu₂O_{8+ δ} . *Phys. Rev. B* **101**, 184511 (2020).
- Neupert, T., Denner, M. M., Yin, J.-X., Thomale, R. & Hasan, M. Z. Charge order and superconductivity in kagome materials. *Nat. Phys.* **18**, 137–143 (2022).
- Wilson, S. D. & Ortiz, B. R. Av₃Sb₅ kagome superconductors. *Nat. Rev. Mater.* **9**, 420–432 (2024).
- Jiang, K. et al. Kagome superconductors AV₃Sb₅ (a = k, rb, cs). *Nat. Sci. Rev.* **10**, nwac199 (2022).
- Jiang, Y.-X. et al. Unconventional chiral charge order in kagome superconductor Kv₃Sb₅. *Nat. Mater.* **20**, 1353–1357 (2021).
- Mielke, C. et al. Time-reversal symmetry-breaking charge order in a kagome superconductor. *Nature* **602**, 245–250 (2022).
- Xu, Y. et al. Three-state nematicity and magneto-optical Kerr effect in the charge density waves in kagome superconductors. *Nat. Phys.* **18**, 1470–1475 (2022).
- Denner, M. M., Thomale, R. & Neupert, T. Analysis of charge order in the kagome metal Av₃Sb₅ (A = K, Rb, Cs). *Phys. Rev. Lett.* **127**, 217601 (2021).
- Park, T., Ye, M. & Balents, L. Electronic instabilities of kagome metals: Saddle points and Landau theory. *Phys. Rev. B* **104**, 035142 (2021).
- Feng, X., Jiang, K., Wang, Z. & Hu, J. Chiral flux phase in the kagome superconductor av₃sb₅. *Sci. Bull.* **66**, 1384–1388 (2021).
- Lin, Y.-P. & Nandkishore, R. M. Complex charge density waves at van Hove singularity on hexagonal lattices: Haldane-model phase diagram and potential realization in the kagome metals aV₃Sb₅ (a=k, rb, cs). *Phys. Rev. B* **104**, 045122 (2021).
- Li, H., Kim, Y. B. & Kee, H.-Y. Intertwined van Hove singularities as a mechanism for loop current order in kagome metals. *Phys. Rev. Lett.* **132**, 146501 (2024).
- Saykin, D. R. et al. High resolution polar Kerr effect studies of CsV₃Sb₅: tests for time-reversal symmetry breaking below the charge-order transition. *Phys. Rev. Lett.* **131**, 016901 (2023).
- Farhang, C., Wang, J., Ortiz, B. R., Wilson, S. D. & Xia, J. Unconventional specular optical rotation in the charge ordered state of kagome metal CsV₃Sb₅. *Nat. Commun.* **14**, 5326 (2023).
- Tazai, R., Yamakawa, Y. & Kontani, H. Drastic magnetic-field-induced chiral current order and emergent current-bond-field interplay in kagome metals. *Proc. Natl Acad. Sci.* **121**, e2303476121 (2024).
- Fu, R.-Q. et al. Exotic charge density waves and superconductivity on the Kagome Lattice. *arXiv e-prints* arXiv:2405.09451 (2024).
- Fernandes, R. M., Birol, T., Ye, M. & Vanderbilt, D. Loop-current order through the kagome looking glass. *arXiv e-prints* arXiv:2502.16657 (2025).
- He, Y. & Varma, C. M. Collective modes in the loop ordered phase of cuprate superconductors. *Phys. Rev. Lett.* **106**, 147001 (2011).
- Shi, Z. D., Else, D. V., Goldman, H. & Senthil, T. Loop current fluctuations and quantum critical transport. *SciPost Phys.* **14**, 113 (2023).
- Palle, G., Ojajärvi, R., Fernandes, R. M. & Schmalian, J. Superconductivity due to fluctuating loop currents. *Sci. Adv.* **10**, eadn3662 (2024).
- Liu, G. et al. Observation of anomalous amplitude modes in the kagome metal CsV₃Sb₅. *Nat. Commun.* **13**, 3461 (2022).
- Azoury, D. et al. Direct observation of the collective modes of the charge density wave in the kagome metal CsV₃Sb₅. *Proc. Natl Acad. Sci.* **120**, e2308588120 (2023).
- Lin, Y.-P., Madhavan, V. & Moore, J. E. Ultrafast optical control of charge orders in kagome metals. *arXiv e-prints* arXiv:2411.10447 (2024).
- Xie, Y.-M. & Nagaosa, N. Phase shifts, band geometry, and responses in triple-q charge and spin density waves. *Phys. Rev. B* **110**, L241108 (2024).
- Lee, P. & Nagaosa, N. Relaxation of nuclear spin due to long-range orbital currents. *Phys. Rev. B* **43**, 1223–1225 (1991).
- Appel, P. et al. Nanomagnetism of magnetoelectric granular thin-film antiferromagnets. *Nano Lett.* **19**, 1682–1687 (2019).
- Flebus, B., Ochoa, H., Upadhyaya, P. & Tserkovnyak, Y. Proposal for dynamic imaging of antiferromagnetic domain wall via quantum-impurity relaxometry. *Phys. Rev. B* **98**, 180409 (2018).
- Finco, A. et al. Imaging non-collinear antiferromagnetic textures via single spin relaxometry. *Nat. Commun.* **12**, 767 (2021).
- Schlussel, Y. et al. Wide-field imaging of superconductor vortices with electron spins in diamond. *Phys. Rev. Appl.* **10**, 034032 (2018).
- Dolgirev, P. E. et al. Characterizing two-dimensional superconductivity via nanoscale noise magnetometry with single-spin qubits. *Phys. Rev. B* **105**, 024507 (2022).

35. Monge, R. et al. Spin dynamics of a solid-state qubit in proximity to a superconductor. *Nano Lett.* **23**, 422–428 (2023).
36. Khoo, J. Y., Pientka, F., Lee, P. A. & Villadiago, I. S. Probing the quantum noise of the spinon fermi surface with NV centers. *Phys. Rev. B* **106**, 115108 (2022).
37. Lee, P. A. & Morampudi, S. Proposal to detect emergent gauge field and its Meissner effect in spin liquids using NV centers. *Phys. Rev. B* **107**, 195102 (2023).
38. Casola, F., van der Sar, T. & Yacoby, A. Probing condensed matter physics with magnetometry based on nitrogen-vacancy centres in diamond. *Nat. Rev. Mater.* **3**, 17088 (2018).
39. Rovny, J. et al. Nanoscale diamond quantum sensors for many-body physics. *Nat. Rev. Phys.* **6**, 753–768 (2024).
40. Zhao, H. et al. Cascade of correlated electron states in the kagome superconductor CsV₃Sb₅. *Nature* **599**, 216–221 (2021).
41. Liang, Z. et al. Three-dimensional charge density wave and surface-dependent vortex-core states in a kagome superconductor CSV₃Sb₅. *Phys. Rev. X* **11**, 031026 (2021).
42. McMillan, W. L. Landau theory of charge-density waves in transition-metal dichalcogenides. *Phys. Rev. B* **12**, 1187–1196 (1975).
43. Nagaosa, N. & Hanamura, E. Microscopic theory of the Raman and infrared spectra of transition-metal dichalcogenides in the charge-density-wave state. *Phys. Rev. B* **29**, 2060–2076 (1984).
44. van Wezel, J. Chirality and orbital order in charge density waves. *Europhys. Lett.* **96**, 67011 (2011).
45. Fortman, B. et al. Electron-electron double resonance detected NMR spectroscopy using ensemble NV centers at 230 GHz and 8.3 T. *J. Appl. Phys.* **130**, 083901 (2021).
46. Kollarics, S. et al. Terahertz emission from diamond nitrogen-vacancy centers. *Sci. Adv.* **10**, eadn0616 (2024).
47. Kautzsch, L. et al. Incommensurate charge-stripe correlations in the kagome superconductor CsV₃Sb_{5-x}Sn_x. *npj Quantum Mater.* **8**, 37 (2023).
48. Liège, W. Search for orbital magnetism in the kagome superconductor csv₃sb₅ using neutron diffraction. *Phys. Rev. B* **110**, 195109 (2024).

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Author contributions

Y.M.X. and N.N. initiated this work. N.N. helped to analyze the problem. Y.M.X. carried out the calculations and wrote the manuscript with suggestions from N.N.

Competing interests

The authors declare no competing interests.

Additional information

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