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Bifurcation of self-assembly pathways to sheet or cage controlled by kinetic template effect

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The template effect is a key feature to control the arrangement of building blocks in assemblies, but its kinetic nature remains elusive compared to the thermodynamic aspects, with the exception of very simple reactions. Here we report a kinetic template effect in a self-assembled cage composed of flexible ditopic ligands and Pd(II) ions. Without template anion, a micrometer-sized sheet is kinetically trapped (off-pathway), which is converted into the thermodynamically most stable cage by the template anion. When the template anion is present from the start, the cage is selectively produced by the preferential cyclization of a dinuclear intermediate (on-pathway). Quantitative and numerical analyses of the self-assembly of the cage on the on-pathway revealed that the accelerating effect of the template is stronger for the early stage reactions of the self-assembly than for the final cage formation step itself, indicating the kinetic template effect.

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s seen in DNA-replication, the template effect^{1,2} is a powerful strategy for efficient synthesis of assemblies whose building blocks are well arranged, such as macrocycles³⁻⁹, cages^{10,11}, interlocked and knotted molecules¹²⁻²⁷, and submicrometer-sized materials^{28–34}. Basically, this effect makes the interconnection of the building blocks feasible by their preorganization by binding to the template molecule(s). As a consequence, the template effect is effective in the synthesis of assemblies composed of conformationally flexible building blocks. When the building blocks are connected by irreversible bonds, once an undesired bond is formed, such intermediates can never lead to the desired structure. Thus, the template molecule biases the reaction towards the correct pathway by modulating the energy landscape so as to selectively decrease the energy barriers of proper bond connections under kinetic control². In molecular self-assembly, where building blocks are connected by reversible bonds, the reaction is rather controlled by thermodynamics. Owing to the reversible nature of the chemical bonds between the building blocks, even when the building blocks are connected in an incorrect manner, the thermodynamically most stable structure is produced under thermodynamic control by correction of the interconnections. Therefore, the thermodynamic template effect plays a major role in most molecular self-assembly systems 13,15,18. As the template molecule that stabilizes the final assembly would also stabilize the transition states and the intermediates produced along the correct self-assembly pathway(s), the importance of the kinetic template effect on molecular selfassembly has been implied but is not clearly understood.

Here we report a bifurcation of self-assembly pathways by a kinetic template that determines the product, a kinetically trapped micrometer-sized sheet structure or the thermodynamically most stable 1-nm-sized coordination cage. In the absence of the template molecule (NO₃⁻), the self-assembly of ditopic ligand 1 and Pd(II) source ([PdPy*₄](OTf)₂, Py* indicates 3-chloropyridine) leads to a metastable micrometer-sized sheet structure as a major product under kinetic control (Fig. 1). With the template, the

 (NO_3^-) @ $[Pd_21_4]^{4+}$ cage, where one NO_3^- anion is bound to the cavity of the cage, is produced in 79% yield through the onpathway. Quantitative and numerical analyses of the self-assembly of the cage in the presence of the template anion revealed that the production of the intermediates for the cage is significantly accelerated by the template anion, which is also confirmed by the acceleration of the formation of a cyclic model structure in the presence of NO_3^- and the strong binding of the cyclic structure with NO_3^- . Besides the stabilization of the final cage by the encapsulation of NO_3^- , a kinetic template effect accelerates the formation of primitive intermediates for the cage by the template anion and contributes strongly to the bifurcation of the self-assembly pathways.

Results

Micrometer-sized sheet formation on the off-pathway. The selfassembly of the helical [Pd214]4+ cage was reported by Steel and McMorran^{35,36}. Due to the high flexibility of the ditopic ligand 1, the resulting cage can bind a variety of anionic species (PF₆⁻, BF₄⁻, ClO₄⁻, ReO₄⁻, and I⁻) in its cavity, whose size can be changed by twisting the helix in an induced-fit manner. The order of the binding strength for anions is $ClO_4^- > BF_4^- > ReO_4^- >$ PF₆⁻, which suggests that smaller anions are more strongly bound in the cage with the exception that ClO_4^- (62.5 Å³) is a better guest than BF_4 (49.3 Å³)³⁶. The self-assembly of the cage from 1 and [PdPy*4](OTf)2 in CD3NO2 at 298 K was carried out to investigate the intermediates produced during the selfassembly by QASAP (quantitative analysis of self-assembly process)^{37–39}. In our previous research on the self-assembly process of this cage from 1 and [PdPy*4](BF4)2, a 200-nm-sized sheet structure was transiently produced during the self-assembly and this sheet structure was finally converted to the (BF₄-)@ $[{\rm Pd_21_4}]^{4+}$ cage⁴⁰. When the self-assembly of the cage was carried out using OTf⁻ as a counter anion and monitored by $^1{\rm H}$ NMR spectroscopy (Fig. 2, Supplementary Fig. 1 and Supplementary

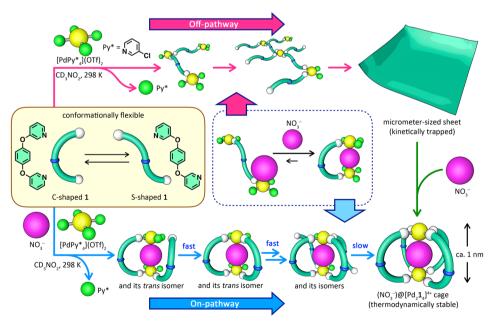


Fig. 1 Summary of the self-assembly of the $[Pd_2\mathbf{1}_4]^{4+}$ cage. A schematic representation of the bifurcation of pathways for the self-assembly of the (NO_3^-) @ $[Pd_2\mathbf{1}_4]^{4+}$ cage from ditopic ligand $\mathbf{1}$ and $[PdPy^*_4](OTf)_2$. Due to the conformational flexibility of $\mathbf{1}$, $\mathbf{1}$ adopts C- and S-shaped conformations in solution. In the absence of a good template (NO_3^-) , oligomerization is preferred from S-shaped ligands to lead to a kinetically trapped micrometer-sized sheet structure (off-pathway). The sheet can be converted to the thermodynamically stable $[Pd_2\mathbf{1}_4]^{4+}$ cage by a good template, NO_3^- . The cage can be produced through the other pathway in the presence of NO_3^- (on-pathway), where the C-shaped conformation is induced by the template to form the (NO_3^-) @ $[Pd_2\mathbf{1}_2Py^*_4]^{4+}$ cyclic structure

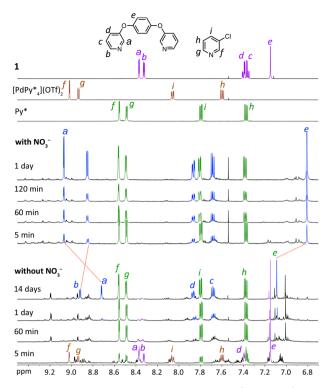


Fig. 2 Monitoring of the self-assembly of the $[Pd_2\mathbf{1}_4]^{4+}$ cage by 1H NMR spectroscopy. 1H NMR spectra (500 MHz, CD₃NO₂, 298 K) of the reaction mixture of the self-assembly of the $[Pd_2\mathbf{1}_4]^{4+}$ cage from $\mathbf{1}$ and $[PdPy^*_4]$ (OTf)₂ in CD₃NO₂ at 298 K with and without NO₃⁻. $[\mathbf{1}]_0 = 2.0$ mM, $[Pd]_0 = 1.0$ mM, $[NO_3^-]_0 = 2.0$ mM

Tables 1-6), the cage formation was significantly retarded (Fig. 3a). The yield of the $(OTf^-)@[Pd_2\mathbf{1}_4]^{4+}$ cage at 1 day is only 6.3%, while that of the $(BF_4^-)@[Pd_2\mathbf{1}_4]^{4+}$ cage at 1 day is 68.3%⁴⁰. The encapsulation of one OTf⁻ anion in the cage was confirmed by ¹⁹F NMR and ¹⁹F DOSY measurements (Supplementary Fig. 2 and Supplementary Table 7). This result indicates that the counter anion largely affects the self-assembly process. STEM measurements of a reaction mixture after the convergence of the self-assembly indicate that a sheet structure was also produced in the self-assembly from 1 and $[PdPv_4](OTf)_2$ (Fig. 4a-e). However, the size of the sheet (over 100 µm) is much larger than that produced from 1 and [PdPy*4](BF4)2. Several dark areas can be seen in the STEM images, which would be formed by tangling of the sheet, suggesting that this sheet is a flexible, soft material. The same tangled sheet structures were observed by AFM measurements of a dried sample of the reaction mixture (Fig. 4f, g). Apart from the tangled parts (Fig. 4i), this sheet is relatively smooth and a step with a gap of 4.44 nm was found (Fig. 4h).

The formation of the sheet was not prevented even in the case where the self-assembly was carried out at 70 °C and the yield of the cage was not improved by heating (Supplementary Figs. 3 and 4), indicating that the sheet produced from 1 and $[PdPy^*_4](OTf)_2$ is more stable than the sheet produced from 1 and $[PdPy^*_4](BF_4)_2^{40}$ and that most of the $(OTf^-)@[Pd_21_4]^{4+}$ cages produced under this condition (35%) would not be derived from the sheet. Indeed, when the self-assembly was conducted with BArF⁻ (tetrakis[3,5-bis(trifluoromethyl)phenyl]borate), which is too large to be encapsulated in the $[Pd_21_4]^{4+}$ cage, the $[Pd_21_4]^{4+}$ cage was produced in 17% yield without a template anion (Supplementary Figs. 5 and 6).

As the sheet structure is kinetically trapped, the self-assembly using OTf⁻ anion tends to promote the growth of the sheet structure under kinetic control, suggesting that OTf⁻ is not a

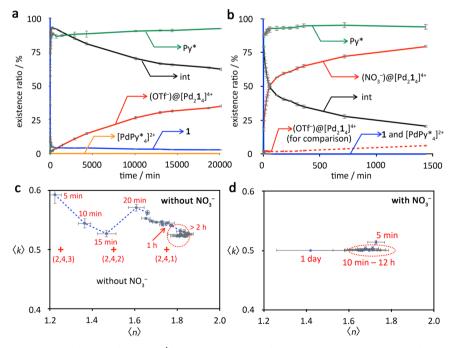


Fig. 3 QASAP data for the self-assembly of the $(X^-)@[Pd_2\mathbf{1}_4]^{4+}$ cage. The self-assembly was conducted from **1** and $[PdPy^*_4](OTf)_2$ in CD_3NO_2 at 298 K with and without NO_3^- . **a** Existence ratios of the substrates and the products for the self-assembly of the cage without NO_3^- . $[\mathbf{1}]_0 = 2.0$ mM, $[Pd]_0 = 1.0$ mM. **b** Existence ratios of the substrates and the products for the self-assembly of the cage with NO_3^- . $[\mathbf{1}]_0 = 2.0$ mM, $[Pd]_0 = 1.0$ mM, $[NO_3^-]_0 = 2.0$ mM. **c** An n-k plot for the self-assembly of the cage with NO_3^- . Error bars indicate the standard errors of the means of the existence ratios (**a** and **b**) and the $(\langle n \rangle, \langle k \rangle)$ values (**c** and **d**). The (n, k) value for $Pd_a\mathbf{1}_bPy^*_c$ indicates as (a, b, c)

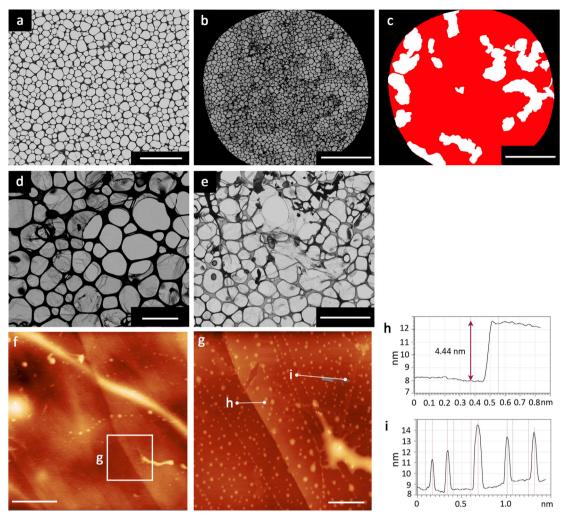


Fig. 4 Characterization of the sheet structure. The sheet was produced in the self-assembly from **1** and $[PdPy^*_4](OTf)_2$ with $n-Bu_4NOTf$ in CD_3NO_2 at 298 K. **a-e** STEM on a TEM microgrid and **f-i** AFM on a graphene substrate (dried sample of the reaction mixture). **a** An empty TEM microgrid. The scale bar indicates 20 μ m. **b** Whole image on a TEM microgrid. The white area corresponds to the background grid and the dark area corresponds to the very thin sheet-type structure. The scale bar indicates 40 μ m. **c** The sheet structure in **b** is shown in red, while white areas indicate bare TEM microgrid. The scale bar indicates 40 μ m. **d**, **e** Magnified images of the very thin sheet-type structure. The scale bars in **d** and **e** indicate 5 and 10 μ m, respectively. **f** A 20 × 20 μ m² AFM image. The scale bar indicates 5 μ m. A 5 × 5 μ m² white square indicates the scanning area for **g**. **g** Magnified 5 × 5 μ m² image of **f**. The scale bar indicates 1 μ m. The white lines in **g** indicate the extracted profile to measure the height. **h** and **i** Height profiles. **h** Crosses over the difference in levels (4.44 nm) where a sheet is on top of another sheet. **i** Crosses over five lumps

good guest for the $[Pd_2\mathbf{1}_4]^{4+}$ cage. As expected, competition experiments indicate that smaller BF_4^- is a stronger guest than OTf $^-$ (90.5 Å 3) for the cage (Supplementary Figs. 7–9 and Supplementary Table 8). To check the ability of counter anions to convert the sheet into the cage, $n\text{-Bu}_4\text{NX}$ (X: ClO_4^- , BF_4^- , or PF_6^-) was added after the formation of the sheet prepared from $\mathbf{1}$ and $[PdPy^*_4](OTf)_2$ (Supplementary Figs. 10–16 and Supplementary Tables 9–11). The rate of the conversion of the sheet to the cage became faster by the addition of smaller guests, indicating that the conversion ability seems to correlate to the size of the anions.

The cage formation on the on-pathway. In the competition experiments of various anions, it was found that NO_3^- (42.3 ų) is more strongly bound to the cage than ClO_4^- (Supplementary Fig. 17). Therefore, the addition of $n\text{-Bu}_4NNO_3$ considerably accelerated the conversion of the sheet to the cage compared with $n\text{-Bu}_4NClO_4$ or $n\text{-Bu}_4NBF_4$ (Supplementary Fig. 16 and Supplementary Table 12). We then carried out the self-assembly from 1

and $[PdPy^*_4](OTf)_2$ in the presence of $n\text{-Bu}_4NNO_3$ to prevent the formation of the sheet during the self-assembly (Fig. 2 and Supplementary Tables 13–17). The 1H NMR signals of the $(NO_3^-)@[Pd_21_4]^{4+}$ cage were clearly observed even at 5 min and the self-assembly reaction almost converged in 1 day to produce the cage in 79% yield (Fig. 3b), indicating that the cage formation is dramatically accelerated by NO_3^- . The H^a signal of the (NO_3^-) $@[Pd_21_4]^{4+}$ cage was largely shifted downfield by 0.36 ppm as compared with that of the $(OTf^-)@[Pd_21_4]^{4+}$ cage (Fig. 2), which suggests that NO_3^- was strongly bound to the cavity of the cage.

Crystal structure of the (NO_3^-) @ $[Pd_21_4]^{4+}$ cage. The structure of the (NO_3^-) @ $[Pd_21_4]^{4+}$ cage was revealed by single-crystal X-ray analysis (Fig. 5, Supplementary Figs. 18 and 19, and Supplementary Tables 18 and 19). Single crystals of the (NO_3^-) @ $[Pd_21_4]^{4+}$ cage were obtained from a solution of the cage in CH_3NO_2 by slow diffusion of i- Pr_2O at 298 K for 10 days. The cage was strongly twisted with a twist angle of 84.6° accompanied by a short $Pd\cdots Pd$ distance of 7.167 Å, which are similar to those

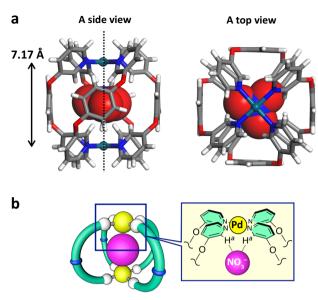


Fig. 5 Crystal structure of $(NO_3^-)@[Pd_2\mathbf{1}_4]^{4+}$. **a** Top and side views of the $(NO_3^-)@[Pd_2\mathbf{1}_4]^{4+}$. cage. Color labels: turquoise, Pd; gray, C; blue, N; red, O; white, H. The dotted black line in the side view indicates the helix axis. **b** Schematic indication of the hydrogen bonding interaction of the pyridyl hydrogen atoms (H^a) and the NO_3^- anion encapsulated in the cage

of the (I⁻)@[Pd₂ $\mathbf{1}_4$]⁴⁺ cage (84.8°, 7.442 Å)³⁶. The NO₃⁻ anion in the cage was disordered between two sites with each occupancy of 50% at the Wyckoff position of 4a on the C2 axis, lying on a plane perpendicular to the helix axis of the cage. The shortest distance between the Ha hydrogen and the oxygen atoms of the NO₃⁻ is 2.33 Å, which is shorter than the sum of the van der Waals radii of hydrogen and oxygen atoms, indicating that the CH...O hydrogen bond stabilizes the inclusion complex^{41–45}. Similar hydrogen bonds are found in the crystal structure of (ClO₄⁻)@[Pd₂1₄]⁴⁺³⁶, suggesting that the stronger binding affinity of ClO₄⁻ to the cage than that of BF₄⁻, which is smaller than ClO₄⁻, is due to the stronger hydrogen bonds between ClO₄⁻ and the cage. The average distance between the oxygen atoms in the NO_3^- and the benzene ring of the ligand 1 is 3.72 Å. When the Pd...Pd distance decreases by increasing the twist angle of the cage, the electron-rich aromatic walls in the cage are slightly moved further from each other, reducing the electrostatic repulsion between the walls and the anion encapsulated in the cage. This would be the reason why the $[Pd_21_4]^{4+}$ cage prefers smaller anions.

Investigation of the self-assembly process of the cage. The self-assembly process of the cage was investigated by the n-k analysis^{37–39}. The n value indicates the average number of the Pd(II) ions bound to a ditopic ligand 1 in a species $[\mathrm{Pd}_a\mathbf{1}_b\mathrm{Py^*}_c]^{2a+}$ (n=(4a-c)/b), while the k value indicates the ratio of the Pd(II) ions to the ditopic ligands (k=a/b). The experimentally obtained (n, k) values, which are indicated as $(\langle n \rangle, \langle k \rangle)$, are the (n, k) values of the average composition of all the intermediates $[\mathrm{Pd}_{\langle a \rangle}\mathbf{1}_{\langle b \rangle}\mathrm{Py^*}_{\langle c \rangle}]^2$ $(a)^+$, which can be determined by the quantification of all the substrates (1 and $[\mathrm{PdPy^*}_4]^{2+}$) and the products $((\mathrm{NO_3}^-)@[\mathrm{Pd}_2\mathbf{1}_4]^{4+}$ and $\mathrm{Py^*}$). The change in the $(\langle n \rangle, \langle k \rangle)$ value with time suggests the type of occurring reactions and the mainly produced intermediates during the self-assembly.

In the absence of NO_3^- (off-pathway), the $\langle n \rangle$ value largely and monotonically increased with time, while the $\langle k \rangle$ value fluctuated around 0.55 (Fig. 3c). As most of the substrates were

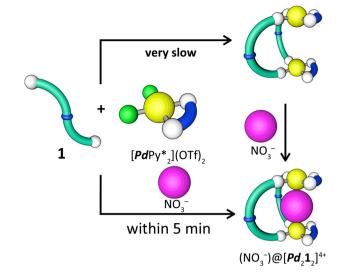


Fig. 6 The template effect of NO_3^- in the self-assembly of the [$Pd_2\mathbf{1}_2\mathbf{1}_2\mathbf{1}_4^+$ model. Pd indicates Pd(N,N,N',N'-tetramethylethylenediamine)

consumed within 30 min, the increase in the $\langle n \rangle$ value after 30 min suggests the growth of the oligomers and/or cross-linking by intra- and/or intermolecular ligand exchanges to release Py*, which causes a decrease in the $\langle c \rangle$ value. The $(\langle n \rangle, \langle k \rangle)$ value reached (1.82, 0.52) at 2 h and stayed around (1.83, 0.52) until the end of the self-assembly. Considering that the largest n value among possible intermediates with the k value of 0.5 on the onpathway is 1.75 for $[Pd_2\mathbf{1}_4Py^*]^{4+}$, the experimental, $\langle n \rangle$ value of 1.83, which is higher than 1.75, suggests the production of intermediates larger than the cage⁴⁰, which is consistent with the observation of the sheet structure.

In the self-assembly reaction carried out in the presence of NO_3^- (on-pathway), the $(\langle n \rangle, \langle k \rangle)$ value stayed around (1.67, 0.50) from 10 min to 12 h (Fig. 3d), while the cage was drastically yielded to up to 72%, after which the self-assembly almost reached convergence. The steady $(\langle n \rangle, \langle k \rangle)$ value during the production of a large amount of the cage indicates that dominant intermediates have (n, k) values close to the observed $(\langle n \rangle, \langle k \rangle)^{46}$. The $(\langle n \rangle, \langle k \rangle)$ value of (1.67, 0.50) is situated in between the (n, k)values of $[Pd_2\mathbf{1}_4Py^*_2]^{4+}$ (1.5, 0.5) and of $[Pd_2\mathbf{1}_4Py^*]^{4+}$ (1.75, 0.5), which correspond to the final precursors of the cage on the onpathway. This result indicates that these two partial cage structures are mainly produced as intermediates from an early stage of the self-assembly and then the intramolecular crosslinking occurs as the rate-determining step. This would be because the rigidity of $[Pd_2\mathbf{1}_4Py^*_2]^{4+}$ and $[Pd_2\mathbf{1}_4Py^*]^{4+}$ hinders the formation of the intermediates and transition states with a five-coordinate Pd(II) center that should be formed during intramolecular ligand exchanges on Pd(II) centers47,48. As a consequence, the template NO₃⁻ anion much contributes to the early stage of the self-assembly of the (NO₃⁻)@[Pd₂1₄]⁴⁺ cage; the NO₃⁻ anion kinetically affects the self-assembly to a great

To demonstrate the strong binding between primitive intermediates and the NO_3^- anion on the on-pathway, the complexation of a model $[Pd_21_2]^{4+}$ macrocycle (Pd indicates Pd(N,N,N',N')-tetramethylethylenediamine)) with the NO_3^- anion was tested (Fig. 6). Upon the addition of n-Bu₄NNO₃ in a CD_3NO_2 solution of the $[Pd_21_2]^{4+}$ macrocycle, the H^a signal was as largely shifted downfield (0.36 ppm) as was observed in the $(NO_3^-)@[Pd_21_4]^{4+}$ cage (Supplementary Fig. 20). This result indicates that NO_3^- can be strongly bound to the cyclic structure,

which suggests that the intramolecular cyclization of (NO_3^-) @ $[Pd_21_2Py^*_5]^{4+}$ to the (NO_3^-) @ $[Pd_21_2Py^*_4]^{4+}$ macrocycle should be promoted by the kinetic template effect of the NO_3^- anion. Indeed, the formation of the $[Pd_21_2]^{4+}$ macrocycle completed within 5 min in the presence of NO_3^- , while the yield of the macrocycle without NO_3^- at 5 min is negligible (Supplementary Fig. 20). The competition experiment for NO_3^- between the $[Pd_21_4]^{4+}$ cage and the $[Pd_21_2]^{4+}$ macrocycle indicates that the cage is a stronger host for NO_3^- than the macrocycle (Supplementary Fig. 21), which is because the cage is structurally more organized than the macrocycle. Therefore, NO_3^- anion has a bilateral template effect on the on-pathway: (i) the kinetic template effect that accelerates intramolecular cyclization of the intermediates on the on-pathway, and (ii) the thermodynamic template effect that stabilizes the final cage.

Numerical analysis of the self-assembly process of the cage. To investigate the self-assembly process of the $(NO_3^-)@[Pd_2\mathbf{1}_4]^{4+}$ cage on the on-pathway in more detail, numerical analysis (NASAP): numerical analysis of self-assembly process^{49–51}) was carried out based on the experimental data. The numerical analysis enables us to learn about the intermediates that cannot be deduced by QASAP. As the behavior of the self-assembly of the $(NO_3^-)@[Pd_2\mathbf{1}_4]^{4+}$ cage is similar to that of the cage self-assembly from the rigid ditopic ligand, NASAP for the present cage was carried out in a similar way to the rigid cage system⁵⁰. A minimum reaction network considering substrates, products, and 25 intermediates composed of no more components than in the cage $([Pd_a\mathbf{1}_bPy^*_c]^{2a+} (a \le 2, b \le 4))$ was prepared. All the reactions in the network (68 in total) are classified into the five types shown in Fig. 7a. As a result of NASAP, we found several solutions with

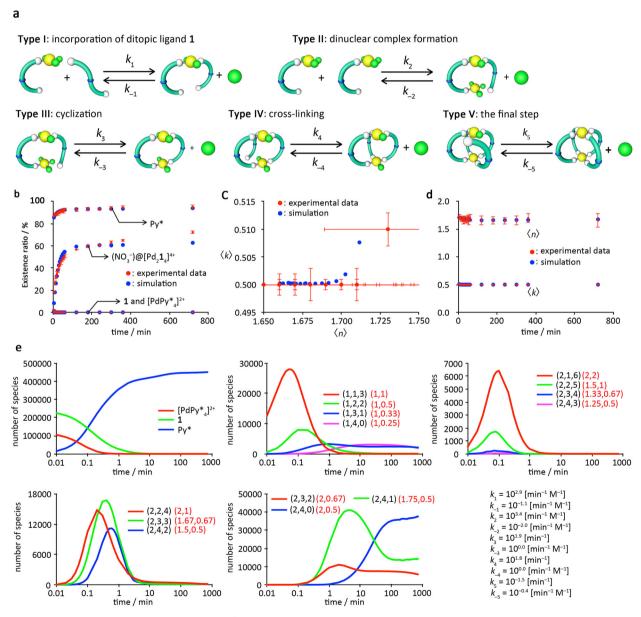


Fig. 7 NASAP data for the self-assembly of the $[Pd_2\mathbf{1}_a]^{4+}$ cage. The self-assembly from $\mathbf{1}$ and $[PdPy^*_a](OTf)_2$ in CD_3NO_2 at 298 K with NO_3^- was simulated. **a** The five reaction types in the network model of the self-assembly. Typical examples are shown in each type. The template anions encapsulated are omitted for clarity. A full network is shown in Supplementary Fig. 22. **b** Existence ratios of the substrates and the products with time. **c** Experimental and simulated n-k plots. **d** Experimental and simulated $(\langle n \rangle, \langle k \rangle)$ values with time. **e** Time variation of major species by simulation and a list of the rate constants found by NASAP. (a, b, c) indicates $[Pd_a\mathbf{1}_bPy^*_c]^{2a+}$. The (n, k) value of $[Pd_a\mathbf{1}_bPy^*_c]^{2a+}$ is also indicated in red

different sets of rate constants reproducing well the experimental results of time-dependent existence ratios of the substrates and the products in addition to the $(\langle n \rangle, \langle k \rangle)$ values (Fig. 7b–d). However, all the solutions have similar features as follows:

- (1) Very similar $k_1 = 10^{2.9} \,\mathrm{min^{-1}} \,\,M^{-1}, \; k_2 = 10^{3.4} \,\mathrm{min^{-1}} \,\,M^{-1}, \; k_5 = 10^{-1.5} \,\mathrm{min^{-1}}, \; \mathrm{and} \; k_{-5} = 10^{-0.4} \,\mathrm{min^{-1}} \,\,M^{-1} \;\mathrm{values} \;\mathrm{were} \;\mathrm{obtained}.$
- (2) As the rates of backward reactions except in the final step (k₋₅) are significantly smaller than those of the corresponding forward reactions, these rate constants (k₋₁, k₋₂, k₋₃, and k₋₄) do not much affect the self-assembly, which is confirmed by the result that the number of backward reactions is negligibly small in all the reaction steps except for the final stage. This result indicates that even though the Pd(II)-N bond formation is reversible, the self-assembly proceeds in an irreversible manner, which would be because the template anion navigates the self-assembly along the correct pathways.

According to the experimental result showing the considerably quick formation of $(NO_3^-)@[Pd_21_2]^{4+}$ (Fig. 6), the large k_3 value can be estimated. Based on this, a suitable set of rate constants in the cyclization $(k_3$ and $k_{-3})$ and cross-linking $(k_4$ and $k_{-4})$ steps were chosen from the data sets that reproduce the experimental data. One of the typical results is shown in Fig. 7b–e. k_3 ($10^{1.9}$ min⁻¹) and k_4 ($10^{1.8}$ min⁻¹) are much larger than k_5 ($10^{-1.5}$ min⁻¹), which indicates that the intramolecular cross-linking in the early stage of the self-assembly is promoted by the kinetic template effect of NO_3^- . In the early stage of the self-assembly, $[Pd_21Py^*_6]^{4+}$ is mainly produced (Fig. 7e). Then, $[Pd_21_2Py^*_4]^{4+}$, $[Pd_21_3Py^*_3]^{4+}$, and $[Pd_21_4Py^*_2]^{4+}$ are produced. Finally, $[Pd_21_4Py^*]^{4+}$ becomes the dominant species, which is due to a small k_5 .

Kinetic template effect in the cage assembly. According to the results mentioned above, the energy landscape of the selfassembly of the cage is schematically shown in Fig. 8. Whether the self-assembly proceeds towards the formation of the cage (onpathway) or towards the sheet structure (off-pathway) is kinetically controlled by the difference between the energy barriers of the intra- and intermolecular reactions in the primitive dinuclear intermediates such as $[Pd_2\mathbf{1}_2Py^*_5]^{4+}$. Without NO_3^- , the energy barrier of the formation of the sheet ($\Delta G^{\ddagger}_{\text{off}}$) is smaller than that of the (OTf⁻)@[Pd₂ $\mathbf{1}_4$]⁴⁺ cage (ΔG^{\ddagger}_{on}), which is mainly due to the preference of open structures with S-shaped ditopic ligands, so the metastable sheet structure is kinetically trapped through the off-pathway. In the presence of NO₃⁻, this good template anion induces the C-shaped conformation in the dinuclear complexes, which decreases the energy barrier of the formation of the cage by preorganization to open the on-pathway ($\Delta G^{\ddagger}_{\text{off}}$) ΔG^{\ddagger}_{on}).

Discussion

In the self-assembly from ditopic ligand 1 and $[PdPy^*_4]^{2+}$, the reaction pathway was largely affected by the counter anions. For the self-assembly with OTf⁻ anions (off-pathway), the very weak template effect of OTf⁻ caused the production of the kinetically trapped sheet structure larger than 100 µm. In contrast, the presence of NO_3^- in the self-assembly afforded the thermodynamically most stable $(NO_3^-)@[Pd_21_4]^{4+}$ cage, whose production was significantly accelerated by the kinetic template effect (on-pathway). QASAP for the cage formation elucidated that the NO_3^- anion promotes the reactions in the early stage of the self-assembly to a greater extent than those in the final step. This result is supported by the high binding affinity of a cyclic $[Pd_21_2]^{4+}$ model complex for NO_3^- and the acceleration of the

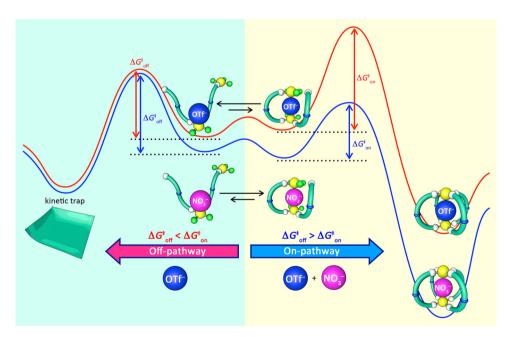


Fig. 8 A simplified energy landscape of the self-assembly of the cage. It is to be noted that the conversion of dinuclear intermediates $([Pd_2\mathbf{1}_2Py^*_5]^{4+})$ is shown as a typical structure) to the cage (right side) and to the sheet (left side) is not a single step but contains multiple reactions. Without a good template (NO_3^-) , an S-shaped conformation of the ditopic ligands $\mathbf{1}$ is preferred and the energy barrier for the formation of the $(OTf^-)@[Pd_2\mathbf{1}_4]^{4+}$ cage $(\Delta G^{\ddagger}_{on})$ is higher than that for the sheet formation $(\Delta G^{\ddagger}_{off})$, which biases the self-assembly towards the off-pathway leading to the metastable sheet structure. In the presence of a good template (NO_3^-) , ΔG^{\ddagger}_{on} is smaller than $\Delta G^{\ddagger}_{off}$, so the self-assembly takes place through the on-pathway to lead to the thermodynamically most stable $(NO_3^-)@[Pd_2\mathbf{1}_4]^{4+}$ cage under kinetic control. If the self-assembly was controlled by the thermodynamic template effect, the product would be determined exclusively by the relative thermodynamic stability between the sheet and the $(X^-)@[Pd_2\mathbf{1}_4]^{4+}$ cage

 $[Pd_21_2]^{4+}$ macrocycle formation in the presence of NO₃⁻. NASAP also supports the strong kinetic template effect on the on-pathway, showing that the rate constants of the intramolecular cyclization in the early stage of the self-assembly $(k_3 \text{ and } k_4)$ are much larger than that in the final step (k_5) . NO₃⁻, the best template anion, does not only efficiently convert the kinetically trapped sheet structure to the cage but is also able to alter the self-assembly pathway itself by the strong kinetic template effect on the early stage of the self-assembly to take the on-pathway.

Methods

General. 1 H and 19 F NMR spectra were recorded using a Bruker AV-500 (500 MHz) spectrometer. All 1 H spectra were referenced using a residual solvent peak, CD₃NO₂ (δ 4.33).

Materials. Unless otherwise noted, all solvents and reagents were obtained from commercial suppliers (TCI Co., Ltd., WAKO Pure Chemical Industries Ltd., KANTO Chemical Co., Inc., and Sigma–Aldrich Co.) and were used as received. CD₃NO₂ was purchased from Acros Organics and used after dehydration with Molecular Sieves 4 Å. Ditopic ligand 1 was prepared according to the literature³⁵.

Monitoring of the self-assembly of the (OTf⁻)@[Pd₂1₄]⁴⁺ cage. A 2.4 mM solution of [2.2] paracyclophane in CHCl₃ (125 µL), which was used as an internal standard, was added to two NMR tubes (tubes I and II) and the solvent was removed in vacuo. A solution of [PdPy*4](OTf)2 (36 mM) in CD3NO2 was prepared (solution A). Solution A (50 μL) and CD₃NO₂ (500 μL) were added to tube I. The exact concentration of [PdPy*4](OTf)2 in solution A was determined through the comparison of the signal intensity of [2.2]paracyclophane by ¹H NMR. A solution of ditopic ligand 1 (36 mM) in CHCl $_3$ (100 μL) was added to tube II and the solvent was removed in vacuo. Then CD3NO2 (550 µL) was added to tube II and the exact amount of 1 in tube II was determined through the comparison of the signal intensity with [2.2]paracyclophane by ¹H NMR. 0.50 eq. (against the amount of ligand 1 in tube II) of solution A (ca. 50 µL; the exact amount was determined based on the exact concentration of solution A and of ligand in tube II) were added to tube II at 263 K. The self-assembly of the (OTf-)@[Pd₂1₄]⁴⁺ cage was monitored at 298 K by ¹H NMR spectroscopy. An example of the ¹H NMR spectra is shown in Fig. 2 and Supplementary Fig. 1. The exact ratio of 1 and [PdPy*4](OTf)2 was unambiguously determined by the comparison of the integral value of each ¹H NMR signal with those of [2.2]paracyclophane. The amounts of 1, [PdPy*4]2+, [Pd214]4+, and Py* were quantified by the integral values of each ¹H NMR signal against the signal of the internal standard ([2.2]paracyclophane). In order to confirm the reproducibility, the same experiment was carried out four times (runs 1-4) in total. These data, the average values of the existence ratios, and the $(\langle n \rangle, \langle k \rangle)$ values are listed in Supplementary Tables 1-6, 9-11, and 13-17.

Determination of the existence ratio of each species. The relative integral value of each ¹H NMR signal against the internal standard [2.2]paracyclophane is used as the integral value in this description. We define the integral values of the signal for the substrates, the products, and the kinetically trapped species at each time t as follows; $I_{\rm L}(t)$: 1/4 of the integral value of the e proton in free ligand 1; $I_{\rm M}(t)$: the integral value of the f proton of Py* in [PdPy*₄]²⁺; $I_{\rm Cage}(t)$: 1/4 of the integral value of the e proton in (X⁻)@[Pd₂1₄]⁴⁺; $I_{\rm Py^-}(t)$: the integral value of the f proton of free Py*.

 $I_{\rm M}(0)$ was determined based on the exact concentration of solution **A** determined by $^{\rm 1}{\rm H}$ NMR and the exact volume of solution **A** added into tube **II**. $I_{\rm L}(0)$ was determined by $^{\rm 1}{\rm H}$ NMR measurement before the addition of solution **A** into tube **II**.

Existence ratio of $[PdPy^*_4]^{2+}$: As the total amount of $[PdPy^*_4]^{2+}$ corresponds to $I_M(0)$, the existence ratio of $[PdPy^*_4]^{2+}$ at t is expressed by $I_M(t)/I_M(0)$. Existence ratio of 1: As the total amount of free ligand 1 corresponds to $I_L(0)$, the existence ratio of 1 at t is expressed by $I_L(t)/I_L(0)$.

Existence ratio of Py*: As the total amount of Py* corresponds to $I_{\rm M}(0)$, the existence ratio of Py* at t is expressed by $I_{\rm Py*}(t)/I_{\rm M}(0)$.

Existence ratio of (X^-) @ $[Pd_21_4]^{4+}$: As (X^-) @ $[Pd_21_4]^{4+}$ is quantified based on 1, the existence ratio of the cage at t is expressed by $I_{Cage}(t)/I_L(0)$.

Existence ratio of the total intermediates not observed by $^1\mathrm{H}$ NMR: The existence ratio of the total intermediates not observed by $^1\mathrm{H}$ NMR is determined based on the amount of ligand 1 in the intermediates. Thus the existence ratio of the total intermediate not observed by $^1\mathrm{H}$ NMR is calculated by subtracting the other species containing 1 (free 1 and (X⁻)@[Pd₂1₄]⁴⁺) from the total amount of 1 ($I_L(0)$). The existence ratio of the total intermediates at t is expressed by ($I_L(0) - I_{L(t)} - I_{Cage}(t)$).

 $\langle a \rangle$: The total amount of Pd(II) ions corresponds to $I_{\rm M}(0)/4$. The amount of Pd (II) ions in [PdPy*₄]²⁺ at t corresponds to $I_{\rm M}(t)/4$. The amount of Pd²⁺ ions in (X⁻)@[Pd₂1₄]⁴⁺ at t corresponds to $I_{\rm Cage}(t)/2$. The amount of Pd(II) ions in the intermediates at t is thus expressed by $I_{\rm M}(0)/4 - I_{\rm M}(t)/4 - I_{\rm Cage}(t)/2$.

 $\langle b \rangle$: The total amount of ligand 1 corresponds to $I_{\rm L}(0)$. The amount of free ligand 1 at t corresponds to $I_{\rm L}(t)$. The amounts of ligand 1 in $({\rm X}^-)@[{\rm Pd}_21_4]^{4+}$ at t corresponds to $I_{\rm Cage}(t)$. The amount of ligand 1 in the intermediates at t is thus expressed by $I_{\rm L}(0) - I_{\rm L}(t) - I_{\rm Cage}(t)$. $\langle c \rangle$: The total amount of Py* corresponds to $I_{\rm M}(0)$. The amount of free Py* at t

 $\langle c \rangle$: The total amount of Py* corresponds to $I_M(0)$. The amount of free Py* at t corresponds to $I_{\text{Py}^+}(t)$. The amount of Py* in [PdPy* $_4$]²⁺ at t corresponds to $I_M(t)$. The amount of Py* in the intermediates at t is thus expressed by $I_M(0) - I_{\text{Py}^+}(t) - I_{M}(t)$.

The $\langle n \rangle$ and $\langle k \rangle$ values are determined with these $\langle a \rangle$, $\langle b \rangle$, and $\langle c \rangle$ values by Eqs. (1) and (2).

$$\langle n \rangle = \frac{4\langle a \rangle - \langle c \rangle}{\langle b \rangle} \tag{1}$$

$$\langle k \rangle = \frac{\langle a \rangle}{\langle b \rangle} \tag{2}$$

Quantitative analysis of the self-assembly process. In QASAP, all the substrates (1 and $[PdPy^*_4](OTf)_2$), and the products (the $(X^-)@[Pd_21_4]^{4+}$ cage and Py^*) were quantified by 1H NMR spectroscopy during the self-assembly and then the amount of the intermediates not observed by 1H NMR (Int) and the average composition of the unobservable intermediates, $Pd_{(a)}1_{(b)}Py^*_{(c)}$, were obtained. The existence ratios of the substrates and the products and (a), (b), (c), (n), and (a) with time are listed in Supplementary Tables 1–6 and 9–17 and plotted in Fig. 3.

STEM measurement. [PdPy* $_4$](OTf) $_2$ (0.595 µmol), **1** (1.19 µmol), and n-Bu $_4$ NOTf (1.19 µmol) were quantified and mixed in CD $_3$ NO $_2$ (ca. 650 µL; [1] $_0$ = 1.82 mM). The solution was left for 4 weeks at 298 K and then diluted 170 times with CH $_3$ NO $_2$. Two microliter of the diluted solution was poured onto the substrate (TEM microgrids, Okenshoji Co. Ltd.). Then the substrate was freeze-dried and measurements were carried out. The STEM image is shown in Fig. 4b–e.

AFM measurement. [PdPy* $_4$](OTf) $_2$ (0.595 µmol), **1** (1.19 µmol), and $n\text{-Bu}_4$ NOTf (1.19 µmol) were quantified and mixed in CD $_3$ NO $_2$ (ca. 650 µL; [$\mathbf{1}$] $_0$ = 1.82 mM). The solution was left for 4 weeks at 298 K and then diluted 170 times with CH $_3$ NO $_2$. Ten microliter of the diluted solution was poured onto the substrate (graphene). Then the substrate was freeze-dried and vacuumed overnight. The AFM image is shown in Fig. 4f–i.

Anion competition experiments. ^{19}F DOSY NMR measurements confirm the encapsulation of OTf $^-$ in the cavity of the $[\text{Pd}_2\mathbf{1}_4]^{4+}$ cage. Anion competition experiments have been carried out by adding 4 eq. to cage (1 eq. to the anion already present in solution) of tetrabutylammonium $(n\text{-Bu}_4\text{N})$ salts of various polyatomic anions. Displacement of the encapsulated anions has been observed through ^1H and ^{19}F NMR measurements (Supplementary Figs. 7–9).

One hundred microliter of a 3 mM CD₃NO₂ solution of the cage (0.3 μ mol) was added to an NMR tube. Four hundred microliter of CD₃NO₂ were then added. At this stage, the cage is encapsulating OTf⁻, and the addition of a different anion will determine the relative binding strengths to the cage of the two anions. Fifty microliter of a 24 mM solution of the tetrabutylammonium salts of the anion of interest (1.2 μ mol) was added to the NMR tube and the encapsulation process was monitored by ¹⁹F NMR spectroscopy. Next, 50 μ L of a 24 mM solution of a different anion were added to the solution. The solutions of the cage and anions were prepared beforehand based on the following molecular weights: cage 1865.5 g mol⁻¹; n-Bu₄NPF₆ 387.43 g mol⁻¹; n-Bu₄NBF₄ 329.27 g mol⁻¹; n-Bu₄NClO₄ 341.91 g mol⁻¹.

Determination of the relative binding affinities of anions. In order to quantitatively determine the relative affinities of the different anions to the $[Pd_21_4]^{4+}$ cage, anion competition experiments starting from the cage encapsulating the strongest bound anion (NO_3^-) were performed (Eq. (3)).

$$NO_3^-@cage + X^- \rightleftarrows (X^-)@cage + NO_3^-$$
 (3)

A 2.4 mM solution of [2.2]paracyclophane in CHCl₃ (125 μ L), which was used as an internal standard, was added to an NMR tube and the solvent was removed in vacuo. Two hundred microliter of a 0.5 mM solution of (NO₃⁻)@[Pd₂1₄]⁴⁺ in CD₃NO₂ were added to the NMR tube, followed by 300 μ L of CD₃NO₂. The exact concentration of (NO₃⁻)@[Pd₂1₄]⁴⁺ in the solution was determined through the comparison of the signal intensity of [2.2]paracyclophane by ¹H NMR spectroscopy. Solutions of *n*-Bu₄NX (X = ClO₄, BF₄, PF₆, and OTf) with concentrations varying based on their binding strength (*n*-Bu₄NClO₄: 40 mM, *n*-Bu₄NBF₄: 200 mM, *n*-Bu₄NPF₆: 400 mM, *n*-Bu₄NOTf: 400 mM) were prepared in CD₃NO₂. Increasing amounts (from 10 to 100 μ L) of an anion solution was added and ¹H NMR spectra were recorded. The amount of *n*-Bu₄NX added was controlled in order to obtain (NO₃⁻)@[Pd₂1₄]⁴⁺ and the new cage encapsulating a different anion in equilibrium, to enable quantification. The relative binding constants

 (K_{comp}) was defined by Eq. (4).

$$K_{\text{comp}} = \frac{[(X^{-})@\text{cage}][\text{NO}_{3}^{-}]}{[\text{NO}_{3}^{-}@\text{cage}][X^{-}]}$$
 (4)

As the total concentration of NO₃⁻ is four times the initial concentration of the cage before the addition of $n\text{-Bu}_4\text{NX}$ ([(NO₃⁻)@cage]₀), [NO₃⁻] can be expressed by Eq. (5).

$$[NO_3^-] = 4 \times [(NO_3^-)@cage]_0 - [(NO_3^-)@cage]$$
 (5)

[X-] in Eq. (4) is expressed by Eq. (6)

$$[X^{-}] = [n-Bu_4N^{+}] - [(X^{-})@cage]$$
 (6)

Thus, using Eqs. (5) and (6), Eq. (4) is expressed by Eq. (7).

$$K_{\rm comp} = \frac{\left[({\rm X}^-)@{\rm cage} \right] \cdot \left(4 \left[({\rm NO}_3^-)@{\rm cage} \right] - \left[\left(({\rm NO}_3^-) \right)@{\rm cage} \right] \right)}{\left[{\rm NO}_3^-@{\rm cage} \right] \cdot \left([{\it n-Bu}_4{\rm N}^+] - \left[({\rm X}^-)@{\rm cage} \right] \right)} \eqno(7)$$

As all the concentrations in Eq. (7) can be determined by ¹H NMR spectroscopy, K_{comp} were calculated using Eq. (7). The data used for the calculation of the K_{co} values for X = ClO₄, BF₄, and PF₆ are summarized in Supplementary Table 8. The K_{comp} values for OTf⁻ were not determined as the binding strength difference between this anion and NO₃⁻ was too large, and no peaks for (OTf⁻)@[Pd₂1₄]⁴⁺ were observed even after the addition of 1200 eq. of n-Bu₄NOTf to (NO₃⁻)@ $[Pd_2\mathbf{1}_4]^{4+}$.

Competition experiment for NO₃⁻ between the cage and the macrocycle. The $(NO_3^-)@[Pd_21_2]^{4+}$ macrocycle was prepared from $[PdPy^*_2](OTf)_2$ and 1 in the presence of n-Bu₄NNO₃ in CD₃NO₂ at 298 K. To this solution, a solution of 1 eq. of (OTf⁻)@[Pd₂1₄](OTf)₃ in CD₃NO₂ was added. ¹H NMR spectra shown in Supplementary Fig. 21 show peaks corresponding to $(NO_3^-)\hat{@}[Pd_2\mathbf{1}_4]^{4+}$ and $[Pd_21_2]^{4+}$, indicating that the NO₃⁻ anion initially bound to the $[Pd_21_2]^{4+}$ macrocycle was selectively encapsulated by the [Pd₂1₄]⁴⁺ cage, demonstrating the stronger affinity of NO_3^- for the cage rather than for the macrocycle.

X-ray analysis of (NO₃⁻)@[Pd₂1₄]⁴⁺. The single crystal was immersed in and coated with Paraton N oil (Hampton Research Corp.), and mounted on a MicroMountTM (MiteGen LLC). Diffraction data of the single crystal were collected on a SuperNova single-crystal X-ray diffractometer with an Eos CCD detector (Rigaku Oxford Diffraction) at 294 K under ambient conditions, using Cu $K\alpha$ ($\lambda = 1.54184$ Å) radiation monochromated by multilayer mirror optics. Bragg spots were integrated using the CrysAlisPro program package (Rigaku Oxford Diffraction). An empirical absorption correction based on the multi-scan method using spherical harmonics was implemented in the SCALE3 ABSPACK scaling algorithm. The structure was solved by an intrinsic phasing method on the SHELXT program 52 and refined by a full-matrix least-squares minimization on F^2 executed by the SHELXL program 53 , using the Olex2 software package (OlexSys Ltd)⁵⁴. The structure was determined as an inversion twin having the polar space group of Aea2 by using a twin law matrix: -1 0 0 0 1 0 0 0 -1, where the Flack parameter⁵⁵ was given as 0.004(3). Thermal displacement parameters where refined anisotropically for all non-hydrogen atoms. All the hydrogen atoms were located at calculated positions and the parameters were refined with a riding model. For counter anions, we could find a disordered NO₃⁻ molecule in the [Pd₂1₄]⁴⁺ cage and two OTf- molecules, which are crystallographically equivalent to each other, in the clearance of the crystal. However, another anion could not be satisfactorily solved due to a terrible disorder. The data were corrected for disordered electron density by using the PLATON SQUEEZE method⁵⁶. The crystal structure is shown in Fig. 5 and Supplementary Figs. 18 and 19. Crystallographic data and structural characteristics of the cage are summarized in Supplementary Tables 18 and 19, respectively. Crystallographic information file for (NO₃⁻)@[Pd₂1₄]²⁺ is provided in Supplementary Data 1. The X-ray crystallographic coordinates for structures reported in this Article have been deposited at the Cambridge Crystallographic Data Centre (CCDC), under deposition number CCDC 1935011. These data can be obtained free of charge from the CCDC via http://www.ccdc.cam.ac.uk/ data_request/cif.

Numerical analysis of self-assembly process of the cage. For the numerical analysis of self-assembly process (NASAP), a reaction network for the self-assembly of the $\left[Pd_21_4\right]^{4+}$ cage, which is indicated as (2,4,0), is constructed as follows. Starting from the final cage (2,4,0), the reaction path is traced back to the substrates, that is, [PdPy*4]2+ and 1. In this back propagation process, all the directly accessible molecular species are considered as the intermediates. Note that in this network model the intermediate species consisting of more components than the cage (2,4,0) are excluded. With this procedure taken, it is found that the total of 29 molecular species (including both the reactants and the products themselves) construct a minimal reaction network composed of 68 reactions, each of which contain the forward and backward processes. The resultant minimal reaction network is shown in Supplementary Fig. 22.

Although we call it minimal, this reaction network turns out to be so large that it is impossible to assign rate constants to each reaction and to search for the parameters in such a vast parameter space to fit the experimental results best.

Therefore, we divided the whole network into five classes possessing similar characteristics and defined the rate constants in Fig. 7a:

Type I: For the coordination of a free ditopic ligand 1 releasing a leaving ligand Py*: k_1 [min⁻¹ M⁻¹] and k_{-1} [min⁻¹ M⁻¹] for the forward and backward reactions, respectively.

Type II: For the formation of dinuclear species from two mononuclear species, with Pd(II) ions bridged by a ditopic ligand 1: k_2 [min⁻¹ M⁻¹] and k_{-2} [min⁻¹ M⁻¹] for the forward and backward reactions, respectively.

Type III: For the cyclization in dinuclear species: k_3 [min⁻¹] and k_{-3} [min⁻¹ M-1 for the forward and backward reactions, respectively.

Type IV: For the cross-linking in dinuclear species: k_4 [min⁻¹] and k_{-4} [min⁻¹ M-1] for the forward and backward reactions, respectively.

Type V: For the final reaction (cage completion): k_5 [min⁻¹] and k_{-5} [min⁻¹ M⁻¹] for the forward and backward reaction, respectively.

Note here that each rate constant is defined per reaction site, based on the modeling procedure reported previously. So the actual reaction rate for each reaction is estimated as the above constant multiplied by the total number of available combinations. For example, for a ligand reaction between [PdPy*4]2+ and 1 to produce $[Pd1Py_3^*]^{2+}$ and Py_3^* , the rate constant is given as k_1 times 4 (the number of Pd-Py* bonds in [PdPy*4]2+) times 2 (the number of coordination sites in 1), i.e.,

$$\left[PdPy_{\ 4}^{*}\right]^{2+} + 1 \xrightarrow{8k_{1}} \left[Pd1Py_{\ 3}^{*}\right]^{2+} + Py^{*} \tag{8}$$

We adopted this setting to explicitly distinguish the structural difference among the species with the same composition.

In order to numerically track the time evolution of the existence ratios for both reactants and products and the $(\langle n \rangle, \langle k \rangle)$ values, we have adopted a stochastic approach based on the chemical master equation, the so-called Gillespie algorithm $^{57-60}$. In this algorithm, for all the possible N reactions including molecular species S_{ai} , S_{bi} , S_{ci} , ...,

$$S_{ai} + S_{bi} + \dots \rightarrow S_{ci} + \dots (i = 1, \dots, N)$$

$$(9)$$

The total reaction rate R_{tot} is calculated as

$$R_{\text{tot}} = r_1 + r_2 + \dots + r_N \tag{10}$$

$$r_i = k_i[S_{ai}][S_{bi}]\dots$$

Starting from the initial time t = 0, at each instant t, which one of the reactions to occur is determined with the uniform random number, $s_1 \in (0,1)$ as

if
$$s_1 \leq \frac{r_1}{R_{\text{tot}}}$$
, then reaction 1 occurs,

if
$$\frac{r_1}{R_{tot}} < s_1 \le \frac{r_1 + r_2}{R_{tot}}$$
, then reaction 2 occurs,

if
$$\frac{r_1}{R_{\text{tot}}} < s_1 \le \frac{r_1 + r_2}{R_{\text{tot}}}$$
, then reaction 2 occurs, if $\frac{r_1 + \dots + r_{N-1}}{R_{\text{tot}}} < s_1 \le 1$, then reaction N occurs.

Another uniform random number $s_2 \in (0,1)$ is independently given to fix the incremental dt as

$$dt = \ln(1/s_2)/R_{\text{tot}} \tag{11}$$

Time is updated as t = t + dt, together with the update of the numbers of corresponding molecular species, i.e., $S_{ai} \rightarrow S_{ai} - 1$, $S_{bi} \rightarrow S_{bi} - 1$, $S_{ci} \rightarrow S_{ci} + 1$, The reason why this approach traces the chemical reactions and actually works well is given in the literatures in detail, along with the practical way to implement it 57-60.

With the initial conditions (numbers of species), $\langle PdPy^*_4 \rangle_0 = 1,200, \langle 1 \rangle_0 =$ 2,400, $\langle \text{others} \rangle_0 = 0$, rate constant search was performed in a ten-dimensional parameter space $(k_1, k_{-1}, k_2, k_{-2}, k_3, k_{-3}, k_4, k_{-4}, k_5, k_{-5})$. The Avogadro number and the volume of the simulation box were set to be $N_A = 6.0 \times 10^{23}$ and $V = 2.0 \times 10^{23}$ 10⁻¹⁸ L, respectively, which gives the same concentrations as the experiments were carried out under. After the rate constant search was finished, refined simulations were performed for some rate parameter sets that give existence ratios and (n, k) plot in good agreement with the experimental counterparts. The adequacy of the fitting to the experimental data was evaluated from the residual sum of squares (RSS) with the average of the experimental data, obtained from three runs. For all the time steps t_i at which the experimental data of existence ratios R_{ex}^{S} and parameters $n_{\rm ex}$ and $k_{\rm ex}$ are available, RSS's are calculated with the numerically obtained values R_{nu}^S and so on as (note that $S = [PdPy_4^*]^{2+}$, 1, $[Pd_21_4]^{4+}$, or Py^*),

$$RSS_{1} = \sum_{t_{i}} \sum_{S} \left(R_{\text{nu},t_{i}}^{S} - R_{\text{ex},t_{i}}^{S} \right)^{2}$$
 (12)

$$RSS_2 = \sum_{t_i} \left(n_{\text{nu},t_i} - n_{\text{ex},t_i} \right)^2 + \sum_{t_i} \left(k_{\text{nu},t_i} - k_{\text{ex},t_i} \right)^2$$
(13)

A representative result is shown in Fig. 7b-d, in which the initial particles and the volume of the simulation box were set to be a hundred times larger than the rough parameter search, i.e., $\langle PdPy^*_4 \rangle_0 = 120,000, \langle 1 \rangle_0 = 240,000, \text{ and } V = 2.5 \times 10^{-16} \text{ L}.$ A similar behavior was confirmed with several runs for the particle numbers given above.

Data availability

The authors declare that all the other data supporting the findings of this study are available within the article and its supplementary information files and from the

corresponding author upon request. Crystallographic information file for (NO_3^-) @ $[Pd_21_4]^{2+}$ is provided in Supplementary Data 1. The X-ray crystallographic coordinates for structures reported in this Article have been deposited at the CCDC, under deposition number CCDC 1935011. These data can be obtained free of charge from the CCDCC via http://www.ccdc.cam.ac.uk/data_request/cif.

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Author contributions

L.H.F.-T., T.T, W.Z., T.K., and S.H. conceived the project. S.H. prepared the manuscript and all the authors discussed the results and commented on the manuscript. L.H.F.-T. and W.Z. carried out QASAP. L.H.F.-T. carried out competition experiments and self-assembly of the Pd(II) complexes under various conditions. T.T., R.S. K.H., and E.N. performed STEM measurements. T.T. performed AFM measurements. L.H.F.-T. and A.O. carried out single-crystal X-ray measurement and analysis. S.T. and H.S. carried out NASAP.

Competing interests

The authors declare no competing interests.

Additional information

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