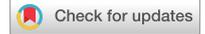




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Mechanisms of slab avalanche release and impact in the Dyatlov Pass incident in 1959

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The Dyatlov Pass incident is an intriguing unsolved mystery from the last century. In February 1959, a group of nine experienced Russian mountaineers perished during a difficult expedition in the northern Urals. A snow avalanche hypothesis was proposed, among other theories, but was found to be inconsistent with the evidence of a lower-than-usual slope angle, scarcity of avalanche signs, uncertainties about the trigger mechanism, and abnormal injuries of the victims. The challenge of explaining these observations has led us to a physical mechanism for a slab avalanche caused by progressive wind-blown snow accumulation on the slope above the hikers' tent. Here we show how a combination of irregular topography, a cut made in the slope to install the tent and the subsequent deposition of snow induced by strong katabatic winds contributed after a suitable time to the slab release, which caused severe non-fatal injuries, in agreement with the autopsy results.

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During the night of February 1, 1959, nine Russian hikers died under unexplained circumstances during a skiing expedition in the northern Ural Mountains. The group had decided to set up their camp on the slope of the Kholat Saykhl (Fig. 1a); the name means “Dead Mountain” in the local Mansi language. Something unexpected happened after midnight that caused expedition members to cut the tent suddenly from the inside and escape towards a forest, more than 1 km downslope (Fig. 1b), without appropriate clothes, under extremely low temperatures (below -25°C , see Supplementary Note 3), and in the presence of strong katabatic winds induced by the passing of an arctic cold front¹.

Twenty-six days to three months after the tragedy, search teams found bodies in the forest and on their way back to the tent. According to the 1959 Soviet criminal investigation, “a compelling natural force” led to the death of the Dyatlov group. However, the nature of this force has not been identified. The mystery arises from numerous unexplained observations. While hypothermia was determined to be the main cause of death, four hikers had severe thorax or skull injuries, two were found with missing eyes and one without tongue; some were almost naked and barefoot, traces of radioactivity were found on some of their clothes, and signs of glowing orange spheres floating in the sky were reported that night¹.

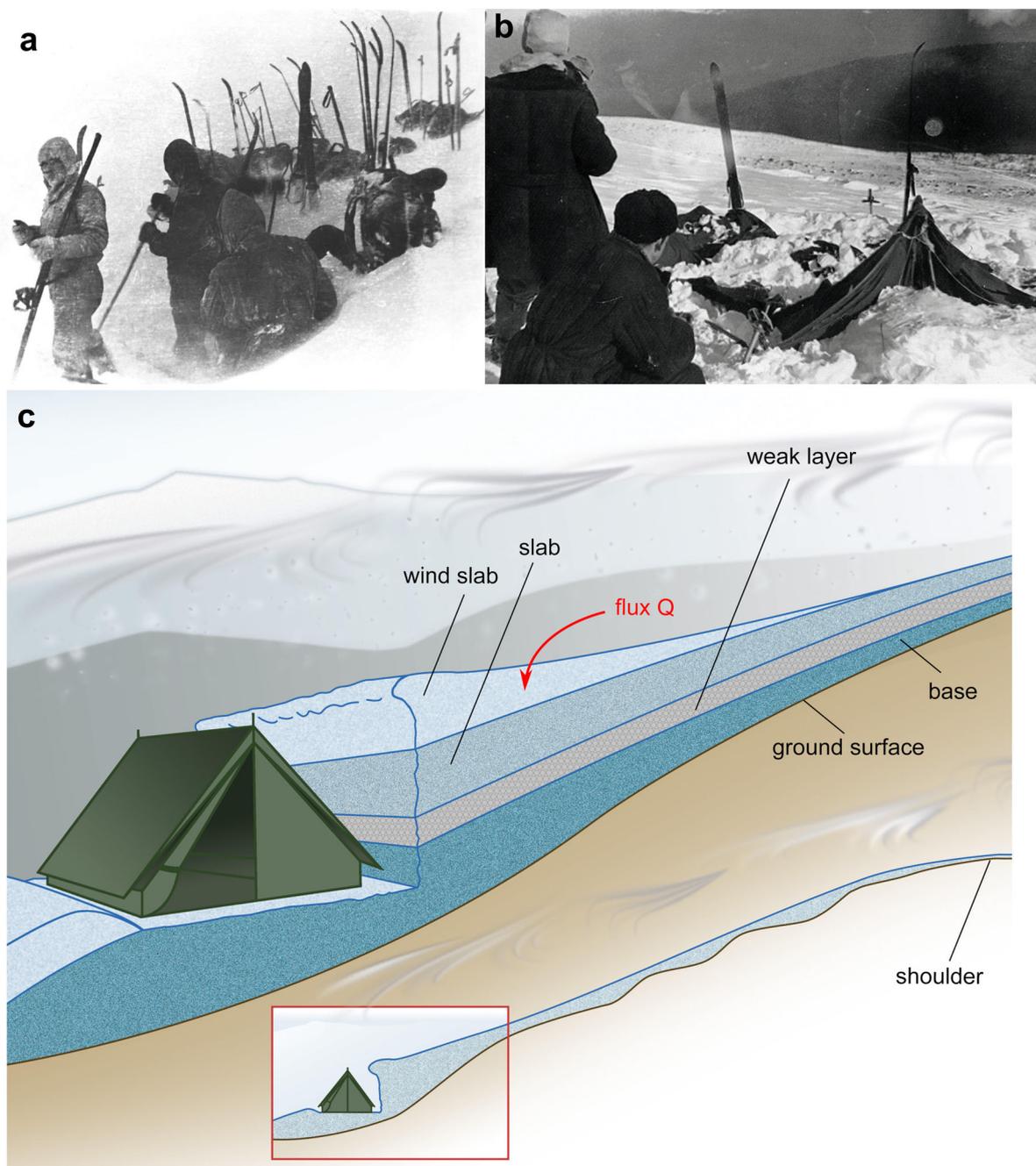


Fig. 1 Pictures taken at the tent location shortly before and weeks after the incident, and a sketch of the slope before the incident. **a** Last picture of the Dyatlov group taken before sunset, while making a cut in the slope to install the tent. Photograph courtesy of the Dyatlov Memorial Foundation. **b** Broken tent covered with snow as it was found during the search 26 days after the event. Photograph courtesy of the Dyatlov Memorial Foundation. **c** Configuration of the Dyatlov tent installed on a flat surface after making a cut in the slope below a small shoulder (see Fig. 2a). Snow deposition above the tent is due to wind transport of snow (with deposition flux Q).

Several theories have been proposed to explain this incident, including infrasound-induced panic, animals, attacks by Yetis or local tribesmen, katabatic winds, a snow avalanche, a romantic dispute, nuclear-weapons tests, etc. The originally popular avalanche theory has been questioned due to several contradictory pieces of evidence¹: (1) no obvious signs of an avalanche or debris were reported by the search team that arrived 26 days later, (2) the average slope angle above the tent location was not sufficiently steep for an avalanche (lower than 30°), (3) the hypothetical avalanche released during the night, at least nine hours after the cut was made in the slope, and (4) the thorax and skull injuries were not typical for avalanche victims.

In 2015, the Investigative Committee of the Russian Federation (ICRF) re-opened the investigation and in 2019 concluded that a snow avalanche was the most probable cause of the accident^{2,3}. The results of this investigation have been challenged recently by the office of the Prosecutor General of the Russian Federation, who in 2019 started its own investigation and in July 2020 came to the same conclusion as ICRF. Both investigations have not, however, disclosed scientific explanations for the four counter-arguments listed above and therefore keep being challenged by the relatives, public, and researchers. In particular, a 2019 Swedish-Russian expedition disagreed with the ICRF conclusions, instead proposing that the direct impact of katabatic winds on the tent was the main contributing factor.

Based on the significant amount of published material^{1–9}, it seems that previous investigations lack an important ingredient: a quantifiable physical mechanism that can reconcile the avalanche hypothesis with seemingly conflicting evidence. Identifying such a mechanism may provide new insights into the nature of storm-triggered snowpack instabilities, which is another important motivation for this work.

Here, we show that—even though the occurrence of an avalanche at this location is unlikely under natural conditions—the combination of four critical factors allowed the release of a small snow slab directly above the tent. These factors include (Fig. 1c): (1) the location of the tent under a shoulder in a locally steeper slope to protect them from the wind, (2) a buried weak snow layer parallel to the locally steeper terrain, which resulted in an upward-thinning snow slab, (3) the cut in the snow slab made by the group to install the tent, (4) strong katabatic winds that led to progressive snow accumulation due to the local topography (shoulder above the tent) causing a delayed failure. Furthermore, the possible construction of a parapet¹ above the cut (a classical safety procedure to protect the tent from the wind, Fig. SF3) could have accelerated the failure process. The proposed physical mechanism couples the onset of dynamic shear-fracture propagation in the weak snow layer with wind-induced snow transport. Provided a realistic wind deposition flux, our model shows that the conditions for avalanche release can be met after a delay of 7.5 to 13.5 h from the moment the hikers made the cut in the slope, in agreement with the forensic evaluation of the time of death. Dynamic avalanche simulations suggest that even a relatively small slab could have led to severe but non-lethal thorax and skull injuries, as reported by the post-mortem examination¹.

Results

Local topography. The mountain slope at the location of the tent is highly irregular. Around 100 m above the tent, there is a shoulder which separates a rather flat plateau and a steeper slope below (Fig. 2a). This slope consists of 4–6 m high steps¹ (Fig. 1c and Fig. SF2) and the tent was installed below one of them, where it was easier to make a cut in a locally flatter slope. The choice of the tent location was also likely driven by the fact that the larger

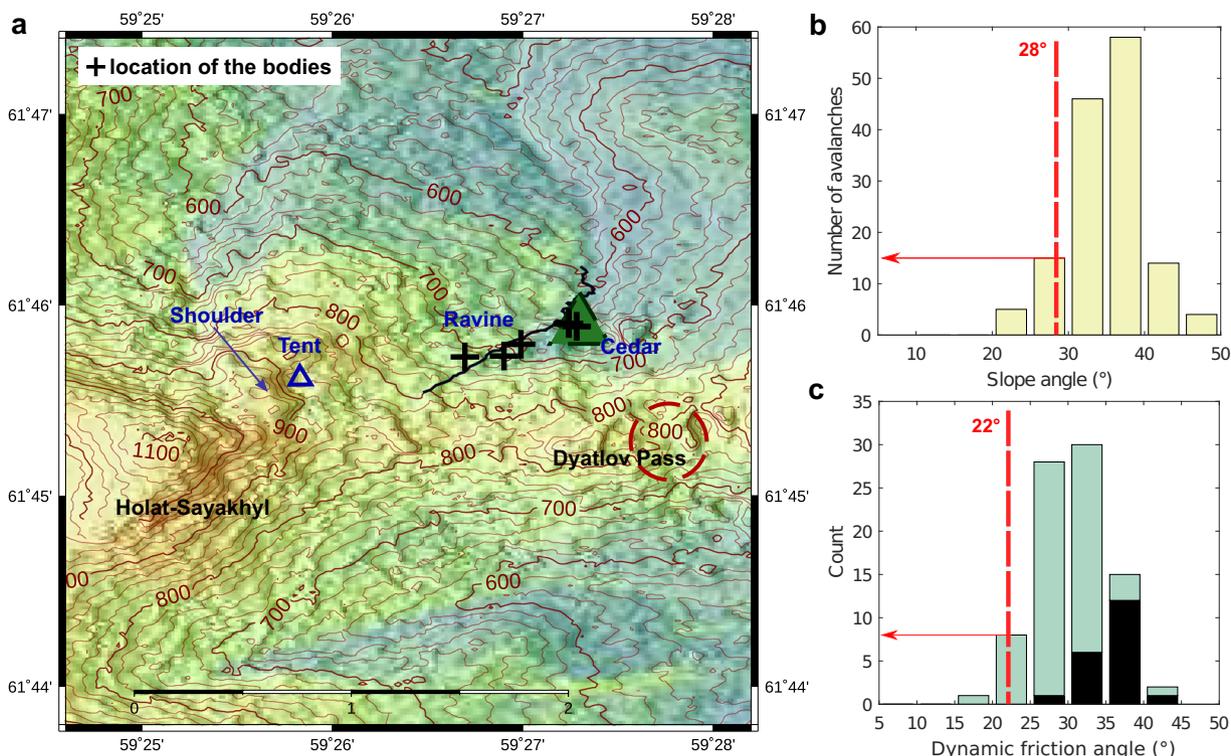


Fig. 2 Local terrain in the Dyatlov Pass, reported snow dynamic friction values, and typical slope angles in human-triggered avalanches. **a** Terrain map of the Dyatlov Pass—indicated by the red circle (adapted based on JAXA aster data, from USGS Earth Explorer, NASA, USGS, JAXA, CC BY 2.5), blue triangle and black crosses indicate locations of the tent and of the hikers’ bodies, respectively. **b** Slope angles reported for 139 accidentally triggered avalanches¹¹. **c** Dynamic friction-angle distribution based on van Herwijnen et Heierli.¹³ Green = faceted types of crystals (depth hoar, faceted crystals, rounded facets, and surface hoar), black = new snow, decomposed and fragmented crystals, and rounded grains.

scale shoulder would protect them from the strong winds. In reality, as we show below, this choice of location could have contributed to the accident: small scale topographic variability resulted in a locally steep weak snow layer while the larger shoulder contributed to significant wind-driven snow accumulation above the tent, eventually leading to an instability.

Slope angle and friction. Major arguments against the avalanche hypothesis include insufficient signs of the occurrence of an avalanche (no apparent deposit or crown fracture) and the relatively mild slope ($\sim 23^\circ \pm 2^\circ$). It appears, however, that the ground surface in the vicinity of the estimated tent location was steeper (up to 30°) than the average snow slope. Subsequent snowfalls smoothed the irregular terrain to the observed average 23° slope. This implies directly that the slab above the layer of depth hoar was thinner uphill, which has three main consequences: (1) It results in the average slope of the buried weak layer being about 28° , increasing the probability of slab release (Fig. 2b). (2) It reduces tensile support at the top of the slab, considerably limiting the avalanche volume. (3) It makes it more difficult to trace avalanche signs, especially 26 days after the incident.

While a 28° slope may still be perceived as being too mild to cause an avalanche—based on the often-quoted and implicit rule of thumb that a minimum of 30° is required¹⁰—in reality, the critical slope angle can be as low¹¹ as 20° (Fig. 2b), provided the dynamic friction angle (sometimes called crack-face friction¹¹) of the snow is sufficiently low. In fact, field measurements have shown that the dynamic friction angle of snow can be as low as 15° , especially for very low temperatures¹². In particular, the buried crystals of depth hoar, which were reported by the investigation on the site (see Supplementary Note 3), tend to exhibit rather low friction values¹³ (Fig. 2c).

Additional load due to wind-transported snow. In spite of the fact that the 28° inclination of the buried weak layer was higher than the angle of friction, the snowpack did not fail for at least nine hours after the slope was cut (see Supplementary Note 1), due to cohesion in the weak layer. In principle, overcoming cohesion does not necessarily require additional loading. Recent work on delayed snow avalanches¹⁴ has proposed a release mechanism driven by rate-dependent processes in the snow slab

and the weak layer¹⁰, which can develop under constant loads. It cannot, however, accommodate a nine-hour delay, due to the relatively short extent of the slab. It follows that the true mechanism must involve additional loading of the slope. Given the extremely low temperatures and strong katabatic winds, it is unlikely that anyone would have climbed above the tent during the night, disturbing the weak layer. In the absence of significant snowfall, the only way to accumulate additional load is through wind transport¹⁵.

Snow accumulation above the tent resulted from katabatic winds and the presence of a shoulder located above the tent (Fig. 2a). Possible construction of a small snow parapet by the Dyatlov group (classical safety measure for snow camping, Fig. SF3), could contribute to additional loading.

Below, we present an analytical model for a thinning snow slab gradually loaded by wind-transported snow above the cut in the slope, which evaluates the wind deposition flux necessary to reproduce the forensic estimate of delay. Subsequent numerical modeling confirms that the observed injuries of the Dyatlov group members are consistent with the failed-slab dynamics.

Conditions for a delayed avalanche. The proposed delayed-release mechanism for a variable-thickness slab (based on the local topography) is illustrated in Fig. 3. After the expedition members made the cut in the slope (Fig. 3a), the shear stress in the weak layer did not immediately reach the peak shear strength. Due to wind-driven snow deposition, the slope gradually became loaded over the growing length l_{cw} , causing the growth of shear stresses in the weak layer. In addition, partial snow sintering¹⁶ leads to strengthening of the wind-transported snow layer. Hence, the growth of l_{cw} is affected by the gradual increase of the slab thickness, and continues until the shear stress in the weak layer reaches the peak shear strength τ_p in the vicinity of the cut (Fig. 3b). A further snow deposition does not mobilize additional shear resistance in the weak layer; in contrast, it initiates rapid softening of the weak layer close to the cut, resulting in the loss of equilibrium, dynamic uphill growth of the basal shear fracture, and slab release.

The slab release condition is derived in the Methods section as a solution of the plain strain (2D) boundary value problem of a variable-thickness cohesive slab under a variable-thickness

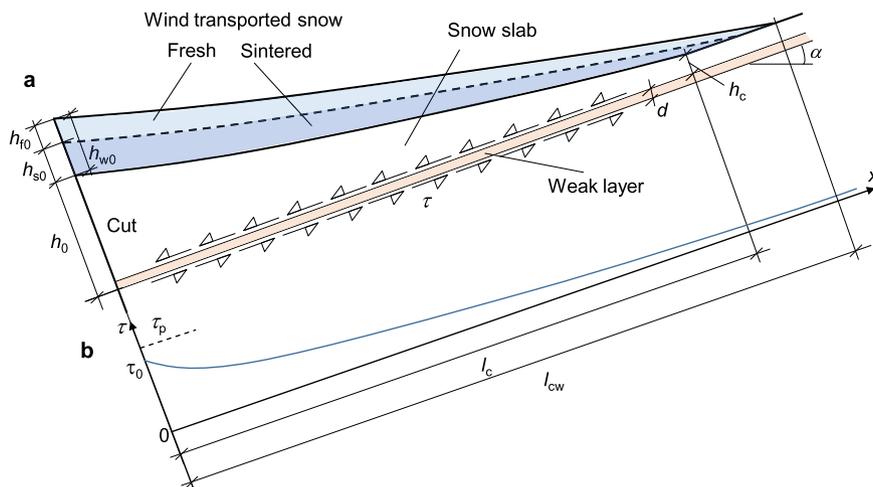


Fig. 3 The mechanism of delayed release of a wind-induced avalanche. **a** Geometry: A planar weak layer of thickness d is inclined at an angle α to the horizontal. It is buried below a snow slab of variable depth, decreasing from h_0 at the cut ($x=0$) to h_c at the straight upper slope ($x \geq l_c$). After the cut is made, a wind-transported snow layer of the height h_{w0} (at the cut) loads the slope, causing local thickening of the slab over the height h_{s0} . **b** Shear stress in the weak layer.

cohesionless snow load, when the shear stress in the weak layer at the cut τ_0 reaches the peak strength τ_p :

$$\tau_0 = \tau_{g0} + r_1 \frac{P_{g0}}{L_0} + \frac{r_3}{r_3 + 2} \frac{P_{w0}}{L_0} \geq \tau_p. \tag{1}$$

Forces and stresses in Eq. (1) are defined as

$$P_{g0} = \frac{1}{2} K_0 \rho g h_0^2 \cos \alpha, P_{w0} = \rho_w g h_{w0} L_0 \cdot \sin \alpha, \tag{2}$$

$$\tau_{g0} = \rho g h_0 \sin \alpha, \tau_p = (\rho h_0 + \rho_w h_{w0}) g \cos \alpha \tan \varphi + c,$$

where φ and c are the angle of internal friction and the cohesion of the weak layer, ρ and ρ_w are the densities of the original slab and of the wind-transported snow, respectively, h_{w0} is the thickness of the wind-deposited snow at the cut, K_0 is the at rest lateral snow pressure coefficient, $L_0 = l_c (1 - \sqrt{h_c/h_0})^{-1}$ is a characteristic length, with quantities l_c , h_c and h_0 defined in Fig. 3a. The parameters r_1 and r_3 are given by

$$r_1 = \frac{1 + \sqrt{1 + 4\lambda_0}}{2}, r_3 = \frac{1 + \sqrt{1 + 4\lambda_s}}{2}, \tag{3}$$

$$\lambda_s = \frac{\lambda_0 h_0}{h_0 + h_{s0}}, \lambda_0 = \frac{GL_0^2}{E' h_0 d},$$

where the quantities h_{s0} and d are defined in Fig. 3a, G is the shear modulus of the weak layer, E' is the plane strain elastic modulus of the slab. The numbers λ_0 and λ_s characterize the ratio between the geometrical quantity L_0 and the characteristic elastic length¹⁴ of the slab-weak layer system before and after snow transport, respectively.

Figure 4a, b provides a conceptual framework for calculating the time of avalanche release. It has been shown (see Methods) that delayed slab release is only possible when the angle of internal friction in the weak layer φ falls within the following range (Fig. 4a):

$$\tan \varphi_{\min} < \tan \varphi < \tan \varphi_{\max}(\lambda_0),$$

$$\tan \varphi_{\min} = \tan \alpha - \frac{c}{\rho g h_0} \sqrt{1 + \tan^2 \alpha} + r_1 \frac{K_0 h_0}{2 L_0}, \tag{4}$$

$$\tan \varphi_{\max}(\lambda_0) = \frac{1 + \sqrt{1 + 4\lambda_0}}{5 + \sqrt{1 + 4\lambda_0}} \tan \alpha,$$

For a value of φ within the above range, the shortest and longest possible delays occur when h_{w0} reaches the minimum ($h_{w0, \min}$) and maximum ($h_{w0, \max}$) critical values defined by

infinite and zero sintering rates, respectively (Fig. 4b):

$$h_{w0, \min} = h_0 \frac{\rho}{\rho_w} \frac{\tan \varphi - \tan \varphi_{\min}}{\tan \varphi_{\max}(\lambda_0) - \tan \varphi}, \tag{5}$$

$$h_{w0, \max} = h_0 \frac{\rho}{\rho_w} \frac{\tan \varphi - \tan \varphi_{\min}}{\tan \varphi_{\max}(\lambda_s) - \tan \varphi}.$$

Finally, we obtain the bounds for the time of delayed release (Fig. 4c) by substituting the bounds for h_{w0} into the equation

$$\Delta t = \frac{\rho_w h_{w0} L_0}{3Q} \left(1 - \left(1 - \frac{l_c}{L_0} \right)^3 \right), \tag{6}$$

where Q is the snow deposition rate.

The proposed analytical framework allowed for back-calculation of the wind deposition flux Q from the range of possible delays between 9.5 and 13.5 h based on forensic data (see Supplementary Note 1). For the geometric and physical parameters of the Dyatlov case (presented in the Methods and discussed in Supplementary Note 6), a reasonable fit of the observed delay range (Fig. 4c) is given by $Q = 0.008 \text{ kg m}^{-1} \text{ s}^{-1}$. Extensive research on snow accumulation shows¹⁵ that this deposition flux requires average wind velocities in the range of 2–12 m s^{-1} which is in agreement with data from nearby weather stations on the night of the accident (see Supplementary Note 3).

Impact on a human body. In addition to explaining the delay, our proposed mechanism provides the pre-failure slab geometry, which can help in understanding how a relatively small slab caused the severe but non-fatal injuries reported. We address this question by combining a novel numerical model with existing data for human-thorax injuries from impact tests performed by the automotive industry^{17,18}.

Three-dimensional numerical simulations based on the Material Point Method (MPM) and finite-strain elastoplasticity¹⁹ (see Methods) show that this small-slab avalanche impacted the hikers lying on the tent floor and filled the excavated space but did not have a significant runout, consistent with the reported lack of clear avalanche signs (Fig. 5). The predicted length of 5.0 m for tensile failure of the slab is in agreement with the analytical model. The simulated snow slab reached a velocity around 2 m/s upon impact (see Fig. SF7, Supplementary Note 5 and Supplementary Movies 1, 2). At this velocity, an impact on a human thorax of a typical snow block with a volume of 0.125–0.5 m^3 and density 400 kg/m^3 results in a maximum thorax

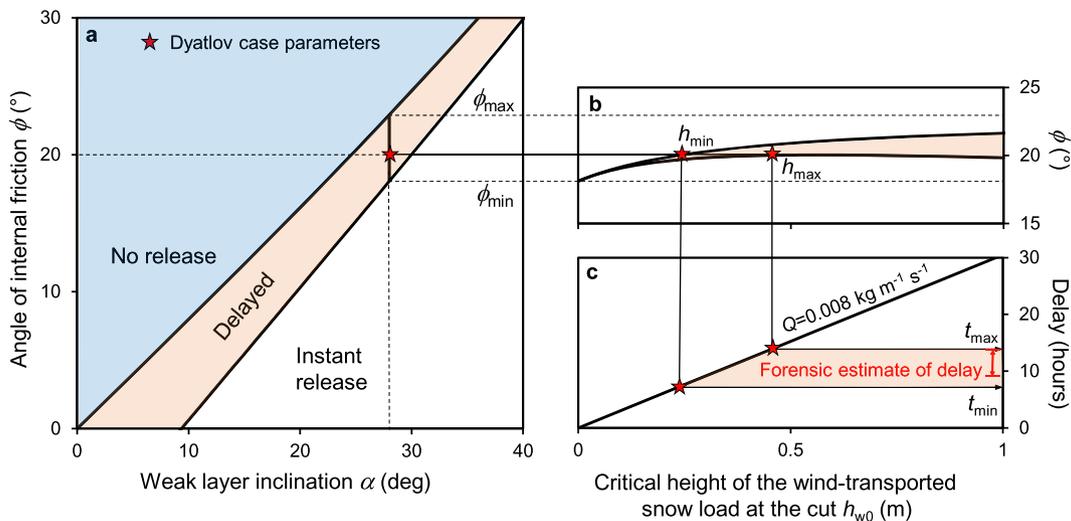


Fig. 4 Conceptual framework for calculating the time of avalanche release. a Conditions for delayed slab release. **b** Bounds for the critical height of the wind-transported load. **c** Predicted vs. forensically estimated delays.

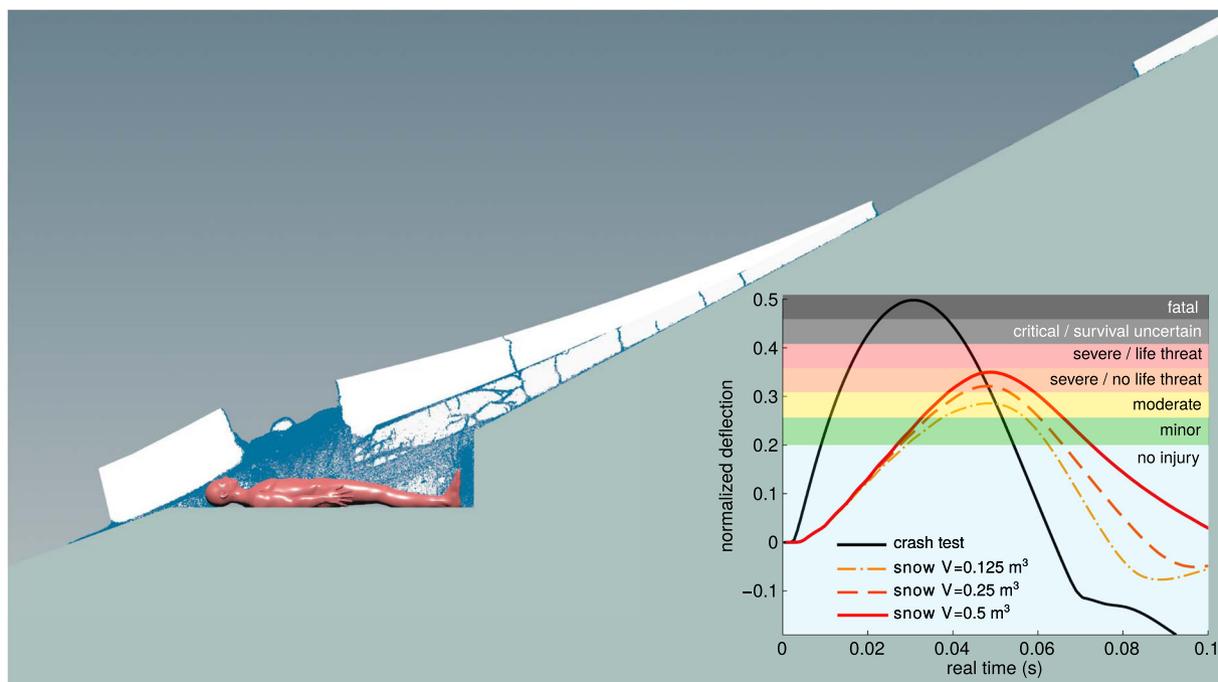


Fig. 5 MPM simulation of the dynamics of a snow-slab avalanche and its impact on a human body. Blue snow particles represent regions in which the yield condition has been met. The inset shows a simulated (3D MPM) thorax deflection (normalized by an original thorax height of 20 cm) for a crash test with a 10 kg rigid mass impacting the thorax at a 7 m/s velocity (black curve) and for impacts by 0.125, 0.25, and 0.5 m³ elastoplastic snow blocks of 400 kg/m³ density and velocities of 2 m/s (orange dashed-dotted curve, red dashed curve, and red solid curve, respectively). Injury levels correspond to the AIS¹¹.

deformation between 28% and 34%, corresponding to the lower range of values reported from crash tests by Kroell et al.¹⁸ for a 10 kg mass impacting the thorax at a speed of 7 m/s (Fig. 5, Supplementary Note 5 and Supplementary Movies 3–6). According to the Abbreviated Injury Scale¹⁸ (AIS), these deflections would mostly lead to non-fatal thoracic injuries from moderate to severe, in agreement with the autopsy report of the Dyatlov-incident criminal investigation. Such injuries are not usually observed in avalanche victims, because impacts rarely occur against stiff obstacles. In the Dyatlov case, the victims were trapped between the falling slab and the tent floor, which was placed on compacted snow reinforced by skis¹.

Discussion

Significant progress in snow and avalanche research over the past two decades^{19–23} has allowed better understanding of avalanche dynamics and of the processes related to snow-slab avalanche release^{24–28}. Nevertheless, no mechanism similar to the one inspired by the Dyatlov mystery has been explored in the literature, and its physical quantification required new theoretical developments.

In our analytical model, these developments include a snow slab with a spatially variable thickness and its evolution due to sintering of the wind-transported snow, which affects the instability of a buried weak snow layer. This is highly relevant for the study of natural storm-triggered slab avalanches²⁹ because its application is not limited only to wind-blowing snow events but can also account for additional loads due to a snowfall. The variable slab geometry resulting from irregular local topography and the cut made in the slope play a critical role in determining whether or when an instability will occur. Our numerical simulation of the impact of a snow avalanche on a human body constrained by an obstacle combines advanced elastoplastic

constitutive models with large-deformation dynamic numerical analysis (MPM) and biomechanical modeling of the human body. This opens new perspectives for research on the effects of snow avalanches on human health and safety.

Needless to say that our models are based on a number of assumptions, which can be justified for this particular case study and relaxed for future research. For example, given the very low reported temperatures, we assumed a brittle behavior for the weak layer which allows neglecting the effects of the process zone³⁰. Moreover, weak layer volumetric collapse^{19,22,23} did not have to be accounted for in our approach because this layer remains completely intact before the onset of instability. Furthermore, the analytical model assumes a 2D geometry which in this case can be justified by the fact that the length of the shoulder controlling snow deposition is much larger than the length of the tent. Yet, the 2D profile of the deposited snow has been simplified for the sake of obtaining a closed-form solution. An important source of uncertainty lies in the dependency of the wind deposition flux on the average wind velocity. The available research¹⁵ shows a very wide range of measured deposition fluxes for a relatively narrow range of the average wind velocity. Nevertheless, the range of wind velocity back-calculated using the analytical model and the forensic estimation of the delay is in good agreement with the range reported in nearby weather stations during the night of the accident.

Concerning the numerical models, because our main focus was the global thorax response, the skeleton and individual ribs were not analyzed. Focusing on the thorax impact, the MPM simulation is initiated at the onset of slab release and the weak layer is not explicitly modeled. In spite of these simplifications, both the analytical and numerical models independently predicted a similar size of the failed slab, providing additional validation for the new mechanism. In addition, while our simulations show that in principle, the observed injuries could have resulted from the

avalanche impact, the impact-induced deformations of the thorax would be rather sensitive to the size of the disintegrated slab blocks (Fig. 5) and thus to the relative positions of the bodies with respect to the cut and slope direction. Given this uncertainty, it is also possible¹ that the thorax injuries were the result of a later snow impact in a very steep ravine where the bodies of the victims, escaping the avalanche area, were found.

Solving the Dyatlov Pass mystery is an enormous task, which is far beyond the scope of this paper. We hope, however, that our work may contribute to determining the plausibility of the avalanche hypothesis. More importantly, it allows the quantification of conditions that can help to prevent similar incidents. Clearly, for a cut in the snow slope to cause a delayed slab release, it requires a relatively rare combination of: (1) a sufficiently steep, weak layer at the base of the snowpack, (2) a cut in the slope, and (3) significant snow accumulation after the cut due to wind transport. However, once these conditions are present, the occurrence of a delayed release requires fairly common values of geometrical and mechanical parameters (see Fig. 4), and Dyatlov-related investigations have indeed reported a non-negligible number of similar accidents¹ (see Supplementary Note 2). This implies that building a tent even on a relatively mild slope (less than 30°) can be dangerous and should not be recommended when combined with a cut in the slope. Instead, digging a snow cave may be a safer solution, as confirmed by the increasing use of this practice for winter camping in recent decades³¹.

In conclusion, our work shows the plausibility of a rather rare type of snow slab instabilities that could possibly explain the Dyatlov Pass incident. Yet, we do not explain nor address other controversial elements surrounding the investigation such as traces of radioactivity found on the victims' garments, the behavior of the hikers after leaving the tent, locations and states of bodies, etc. While possible explanations are given in multiple published sources¹⁻⁹ as well as by both the Investigative Committee and the Prosecutor General of the Russian Federation, we believe that this will always remain an intrinsic part of the Dyatlov Pass Mystery.

Online content. Any methods, additional references, Nature Research reporting summaries, source data, extended data, supplementary information, acknowledgements, peer review information, details of author contributions and competing interests, and statements of data and code availability are available at <https://doi.org/10.1038/XXX>.

Methods

Problem formulation for the analytical model of delayed avalanche release. A simplified delayed slab release model is based on the mechanism illustrated in Fig. 1a. We assume a plane strain problem with a cut in a curved slope, with a planar slope-parallel weak layer of angle α , thickness d at the depth h described by a parabolic equation:

$$\begin{cases} h(x) = h_0 \left(1 - \frac{x}{L_0}\right)^2 & \text{for } x < l_c, \\ h(x) = h_c & \text{for } x \geq l_c, \end{cases} \quad (7)$$

where h_0 is the depth of the weak layer at the cut ($x = 0$), h_c is the constant depth of the weak layer at the upper straight portion of the slope ($x \geq l_c$), l_c is the distance from the cut to the point on the slope where the slope surface becomes parallel to the weak layer. The characteristic length L_0 is defined from the condition $h(x = l_c) = h_c$:

$$L_0 = \frac{l_c}{1 - \sqrt{h_c/h_0}}, \quad (8)$$

The choice of the parabolic slope approximation has been based on the following considerations. Firstly, it reflects a smooth uphill steepening of the slope. Secondly, it leads to a second-order Euler–Cauchy differential equation with a simple analytical solution. Thirdly, it is geometrically rather close to the simplest linear approximation of the slope between the cut ($x = 0$) and the beginning of the constant thickness slab ($x = l_c$).

After the cut is made, the snow keeps accumulating on the slope behind the tent due to the wind transport, with $h_w(x, t)$ being the thickness of the wind-transported snow at the time t after the construction of the parapet. Assuming that the surface of the new snow layer can also be described by a parabolic function, the thickness of the wind-transported snow is

$$\begin{aligned} h_w(x, t) &= h_s(x, t) + h_f(x, t) = (h_{s0}(t) + h_{f0}(t)) \left(1 - \frac{x}{L_0}\right)^2 \text{ for } x < l_{cw}, \\ h_w(x, t) &= h_c \text{ for } x > l_{cw}; \quad l_{cw} = L_0 \left(1 - \sqrt{\frac{h_c}{h_0 + h_{s0} + h_{f0}}}\right), \end{aligned} \quad (9)$$

where h_f is the portion of the new snow that is still fresh, while h_s is the portion which is already sintered, with h_{f0} and h_{s0} denoting the thickness of each portion at the cut ($x = 0$). The parabolic approximation for the surface of the wind-transported snow reflects the fact that snow deposition due to the wind transport reduces away from the tent. Note that the tent represented an obstacle for the wind flow, in particular if a parapet was built above the cut to protect the tent against wind and snow.

The initial (before the cut) internal lateral force P_g in the snow slab is

$$P_g = \sigma_g h = \frac{1}{2} K_0 \sigma_n h = \frac{1}{2} K_0 \rho g h^2 \cos \alpha, \quad (10)$$

where ρ is the snow density, K_0 is the at rest lateral snow pressure coefficient. In general, the value of K_0 depends on the history of snow deposition, but can be bounded (for horizontal snow layer) between the estimate via Poisson's ratio ν : $K_0 = \frac{\nu}{1-\nu}$ (elastic) and the estimate given by Jaky's formula³²: $K_0 = 1 - \sin \varphi_s$ (for a normally consolidated granular material), where φ_s is the angle of internal friction of the snow slab.

The initial stress state (before the cut) in the weak layer is

$$\tau_g = \rho g h \sin \alpha; \quad \sigma_n = \rho g h \cos \alpha, \quad (11)$$

where τ_g is the initial shear stress, causing the initial displacement (δ_g), σ_n is the normal stress. In the following, we adopt a net value $\Delta\tau = \tau - \tau_g$ for the shear stress τ in the weak layer, and the net values $\Delta P = P - P_g$ and $\Delta\delta = \delta - \delta_g$ for the internal lateral force P and displacement δ of the snow slab, respectively.

Neglecting inertia forces, the equilibrium condition for the snow slab is given as

$$\frac{\partial \Delta P}{\partial x} = \Delta\tau - \tau_w(x), \quad \Delta\tau = \tau - \tau_g, \quad \Delta P = P - P_g. \quad (12)$$

The shear response of the weak layer is assumed to be linear:

$$\Delta\tau = \frac{G}{d} \Delta\delta, \quad \Delta\gamma = \frac{\Delta\delta}{d}, \quad \Delta\delta = \delta - \delta_g, \quad (13)$$

where G is the shear modulus of the weak layer and

$$\delta_g = \frac{d}{G} \tau_g, \quad \tau_g = \rho g h \cdot \sin \alpha, \quad \tau_w = \rho_w g (h_s + h_f) \cdot \sin \alpha, \quad (14)$$

where δ_g is the initial displacement of the slab, resulting from the constant initial shear stress τ_g (before the cut).

Extension in the snow slab is also assumed to be linear:

$$\Delta P = \Delta\sigma h = E' h \Delta\varepsilon = E' h \frac{\partial \Delta\delta}{\partial x}, \quad (15)$$

where $E' = E/(1 - \nu^2)$ is the plain strain modulus of the snow slab. Combining Eqs. (7), (13) and (15) gives

$$\Delta P = \frac{E' h d}{G} \frac{\partial \Delta\tau}{\partial x} = \frac{E' h_0 d}{G} \left(1 - \frac{x}{L_0}\right)^2 \frac{\partial \Delta\tau}{\partial x} \quad (16)$$

and

$$\Delta P = \frac{E'(h + h_s) d}{G} \frac{\partial \Delta\tau}{\partial x} = \frac{E'(h_0 + h_{s0}) d}{G} \left(1 - \frac{x}{L_0}\right)^2 \frac{\partial \Delta\tau}{\partial x} \quad (17)$$

for the curved portions of the original and the thickened slab, respectively.

It is assumed that after the slope is cut, behavior in the weak layer is linear elastic, with the shear stress τ in Fig. 3b not yet reaching the peak strength τ_p . Due to the wind-driven snow deposition h_w , the slope gets loaded by additional shear stress τ_w , until at a certain time Δt after the cut the shear stress in the weak layer τ reaches the peak strength τ_p in the vicinity of the cut. Further increase in h_w will not mobilize additional shear resistance in the weak layer, on the contrary, it will initiate rapid softening of the weak layer close to the cut, increasing the downhill lateral load on the still intact portion of the weak layer. This will result in the loss of equilibrium, unstable uphill growth of the basal shear fracture and the release of the slab.

Conditions in the snow slab immediately after the cut. In this and the following sections we neglect the straight portion of the slope and assume that within $0 \leq x \leq L_0$ the whole slab is parabolic. It can be shown that for $h_c/h_0 \leq 0.2$ (consistent with the Dyatlov case), this simplification has a negligible effect on the solution.

At the moment of the cut, the thickness of the slab is given by Eq. (7), therefore $\tau_w = 0$, and differentiating Eq. (12) with respect to x and substituting Eq. (16) into it gives a differential equation for net lateral forces:

$$(1 - \bar{x})^2 \frac{\partial^2 \Delta P}{\partial \bar{x}^2} = \lambda_0 \Delta P \quad \text{for } 0 \leq \bar{x} \leq 1, \tag{18}$$

where

$$\bar{x} = \frac{x}{L_0}, \lambda_0 = \frac{L_0^2}{l_{c0}^2}, l_{c0} = \sqrt{\frac{E' h_0 d}{G}}. \tag{19}$$

Equation (18) is the well-known second-order Euler–Cauchy differential equation, with a solution given by

$$\begin{aligned} \Delta P(\bar{x}) &= C_1(1 - \bar{x})^{r_1} + C_2(1 - \bar{x})^{r_2}, \\ r_1 &= \frac{1 + \sqrt{1 + 4\lambda_0}}{2}, r_2 = \frac{1 - \sqrt{1 + 4\lambda_0}}{2}, \end{aligned} \tag{20}$$

where C_1 and C_2 are constants to be found from boundary conditions. In order to have a finite solution at $\bar{x} = 1$, C_2 has to be set to zero, and from the boundary condition at $\bar{x} = 0$, where the lateral force is equal to zero ($\Delta P = -P_g|_{\bar{x}=0}$) due to the cut:

$$\Delta P|_{\bar{x}=0} = C_1 = -P_{g0}, P_{g0} = \frac{1}{2} K_0 \rho g h_0^2 \cos \alpha. \tag{21}$$

Substituting these constants into Eq. (20) provides stress conditions in the slab and the weak layer after the cut in the slope:

$$\begin{aligned} P_c(\bar{x}) &= P_g(\bar{x}) + \Delta P(\bar{x}) = P_g(\bar{x}) - P_{g0}(1 - \bar{x})^{r_1}, \\ \tau_c(\bar{x}) &= \tau_g(\bar{x}) + \frac{1}{L_0} \frac{\partial \Delta P}{\partial \bar{x}} = \tau_g(\bar{x}) + \frac{r_1}{L_0} P_{g0}(1 - \bar{x})^{r_1-1} \end{aligned} \tag{22}$$

with the boundary conditions at the cut $\bar{x} = 0$:

$$P_c|_{\bar{x}=0} = 0; \tau_c|_{\bar{x}=0} = \tau_{g0} + \frac{r_1}{L_0} P_{g0}. \tag{23}$$

For the slab not to fail immediately after the cut the following condition should be satisfied:

$$\begin{aligned} \tau_c|_{\bar{x}=0} &= \tau_{g0} + \frac{r_1}{L_0} P_{g0} < \tau_{p0}, \\ \tau_{p0} &= \sigma_3 \tan \varphi + c = \rho_w g (h_{s0} + h_{f0}) \cos \alpha \tan \varphi + c, \end{aligned} \tag{24}$$

where φ and c are the angle of internal friction and cohesion in the weak layer. In this case, the normal force and shear stress from Eq. (22) will serve as initial conditions for the next stage—loading of the slab by the wind-transported snow.

Failure of the undercut slab loaded by the wind-transported snow. After the wind-transported snow reached the thickness h_w given by Eq. (9), the additional shear stress τ_w in Eq. (12) is now larger than zero:

$$\begin{aligned} \tau_w(\bar{x}) &= \rho_w g h_w(\bar{x}) \cdot \sin \alpha = \frac{P_{w0}}{L_0} (1 - \bar{x})^2, \\ P_{w0} &= \rho_w g (h_{s0} + h_{f0}) L_0 \cdot \sin \alpha, \end{aligned} \tag{25}$$

where ρ_w is the density of the wind-transported snow. The portion h_s of the new snow has sintered, increasing the thickness of the original slab, as reflected in Eq. (17). After substituting $\tau_w(\bar{x})$ into Eq. (12), differentiating it with respect to x and combining it with Eq. (17) we obtain the following differential equation for net lateral forces in the sintered slab:

$$(1 - \bar{x})^2 \frac{\partial^2 \Delta P}{\partial \bar{x}^2} = \lambda_s \Delta P + 2P_{w0}(1 - \bar{x})^3 \quad \text{for } 0 \leq \bar{x} \leq 1, \tag{26}$$

where

$$\bar{x} = \frac{x}{L_0}, \lambda_s = \frac{\lambda_0 h_0}{h_0 + h_{s0}}. \tag{27}$$

Solution of Eq. (26) is given by

$$\begin{aligned} \Delta P(\bar{x}) &= C_1(1 - \bar{x})^{r_3} + C_2(1 - \bar{x})^{r_4} - \frac{2P_{w0}}{\lambda_s - 6} (1 - \bar{x})^3, \\ r_3 &= \frac{1 + \sqrt{1 + 4\lambda_s}}{2}, r_4 = \frac{1 - \sqrt{1 + 4\lambda_s}}{2}, \end{aligned} \tag{28}$$

where C_1 and C_2 are constants. Again, in order to have a finite solution at $\bar{x} = 1$, C_2 has to be set to zero, and from the boundary condition at $\bar{x} = 0$, where the lateral force is equal to zero due to the cut:

$$\Delta P|_{\bar{x}=0} = C_1 - \frac{2P_{w0}}{\lambda_s - 6} = 0 \tag{29}$$

substituting these constants into Eq. (28) provides a solution for the net normal

forces:

$$\Delta P(\bar{x}) = \frac{2P_{w0}}{\lambda_s - 6} [(1 - \bar{x})^{r_3} - (1 - \bar{x})^3], r_3 = \frac{1 + \sqrt{1 + 4\lambda_s}}{2}. \tag{30}$$

This leads to the following normal forces in the slab and shear stresses in the weak layer:

$$\begin{aligned} P(\bar{x}) &= P_c(\bar{x}) + \Delta P(\bar{x}) \\ &= P_g(\bar{x}) - P_{g0}(1 - \bar{x})^{r_1} + \frac{2P_{w0}}{\lambda_s - 6} [(1 - \bar{x})^{r_3} - (1 - \bar{x})^3], \\ \tau(\bar{x}) &= \tau_c(\bar{x}) + \tau_w(\bar{x}) + \frac{1}{L_0} \frac{\partial \Delta P}{\partial \bar{x}} \\ &= \tau_g(\bar{x}) + \frac{r_1}{L_0} P_{g0}(1 - \bar{x})^{r_1-1} + \frac{P_{w0}}{L_0} (1 - \bar{x})^2 \\ &\quad - \frac{2P_{w0}}{\lambda_s - 6} \left[\frac{r_3}{L_0} (1 - \bar{x})^{r_3-1} - \frac{3}{L_0} (1 - \bar{x})^2 \right]. \end{aligned} \tag{31}$$

At the cut $\bar{x} = 0$, using $\lambda_s = r_3^2 - r_3$ we obtain

$$P_0 = 0, \tau_0 = \tau_{g0} + \frac{r_1}{L_0} P_{g0} + \frac{P_{w0} \lambda_s - 2r_3}{L_0} = \tau_{g0} + \frac{r_1}{L_0} P_{g0} + \frac{P_{w0}}{L_0} \frac{r_3}{r_3 + 2} \tag{32}$$

and when $h_{w0} = h_{f0} + h_{s0}$ becomes sufficiently large for this shear stress to reach the peak strength:

$$\tau_0 = \tau_{g0} + r_1 \frac{P_{g0}}{L_0} + \frac{r_3}{r_3 + 2} \frac{P_{w0}}{L_0} \geq \tau_p = \tau_{p0} + \tau_{pw} \tag{33}$$

the slab will fail. Shear stresses and normal forces in Eq. (33) are defined as

$$\begin{aligned} P_{g0} &= \frac{1}{2} K_0 \rho g h_0^2 \cos \alpha, P_{w0} = \rho_w g (h_{s0} + h_{f0}) L_0 \cdot \sin \alpha, \tau_{g0} = \rho g h_0 \sin \alpha, \\ \tau_{p0} &= \rho g h_0 \cos \alpha \tan \varphi + c, \tau_{pw} = \rho_w g (h_{s0} + h_{f0}) \cos \alpha \tan \varphi. \end{aligned} \tag{34}$$

Relationship (33) has been validated numerically for the Dyatlov case parameters using the Material Point Method (see Supplementary Note 4).

Time to failure. The time to failure is a function of the area A_w of the wind-transported snow at failure derived by integration of Eq. (9) and of the snow deposition rate Q , which is a function of the average wind speed v :

$$\Delta t = \frac{\rho_w A_w}{Q(\langle v \rangle)}, A_w = \frac{1}{3} h_{w0} L_0 \left(1 - \left(1 - \frac{l_c}{L_0} \right)^3 \right), \tag{35}$$

where the small area of new snow between l_c and l_{cw} in Fig. 3a has been neglected. After the wind-transported snow sinters, it causes the thickening of the original slab, which constrains the slab displacements and slows down the growth of shear stresses in the weak layer. Therefore, if the snow sinters immediately, the peak strength in the weak layer is reached slower. It follows that the largest amount of the wind-transported snow $h_{w0, \max}$ required for the avalanche release can be calculated assuming that the snow sinters instantaneously over the entire thickness h_w , i.e. $h_{f0} = 0$. The upper bound of delay can then be expressed as

$$\Delta t_{\max} = \frac{\rho_w h_{w0, \max} L_0}{3Q(\langle v \rangle)} \left(1 - \left(1 - \frac{l_c}{L_0} \right)^3 \right), \tag{36}$$

where $h_{w0, \max} = h_{s0}$ is determined by solving numerically Eq. (33), with stresses and forces substituted from Eq. (34):

$$h_{w0, \max} = h_{s0} = h_0 \frac{\rho}{\rho_w} \frac{\tan \varphi - \tan \varphi_{\min}}{\tan \varphi_{\max}(\lambda_s) - \tan \varphi}, \tag{37}$$

where

$$\tan \varphi_{\min} = \tan \alpha - \frac{c}{\rho g h_0} \sqrt{1 + \tan^2 \alpha} + r_1 \frac{K_0 h_0}{2L_0}, \tag{38}$$

$$\tan \varphi_{\max}(\lambda_s) = \frac{r_3}{r_3 + 2} \tan \alpha, r_3 = \frac{1 + \sqrt{1 + 4\lambda_s}}{2}, \lambda_s = \frac{\lambda_0 h_0}{h_0 + h_{s0}}.$$

Using the same reasoning, it follows that the smallest amount of the wind-transported snow required for the avalanche release $h_{w0, \min}$ can be calculated assuming that the new snow does not sinter. Substituting $h_{s0} = 0$ into Eqs. (37)–(38) gives the equation for the lower bound of the thickness of the wind-deposited snow at which the slab will fail:

$$h_{w0, \min} = h_{f0} = h_0 \frac{\rho}{\rho_w} \frac{\tan \varphi - \tan \varphi_{\min}}{\tan \varphi_{\max}(\lambda_0) - \tan \varphi}, \tag{39}$$

where

$$\tan \varphi_{\min} = \tan \alpha - \frac{c}{\rho g h_0} \sqrt{1 + \tan^2 \alpha} + r_1 \frac{K_0 h_0}{2L_0}, \tag{40}$$

$$\tan \varphi_{\max}(\lambda_0) = \frac{r_1}{r_1 + 2} \tan \alpha; r_1 = \frac{1 + \sqrt{1 + 4\lambda_0}}{2},$$

which, when substituted into Eq. (35), gives the lower bound for the time to failure:

$$\Delta t_{\min} = \frac{\rho_w h_{w0, \min} L_0}{3Q(\langle v \rangle)} \left(1 - \left(1 - \frac{l_c}{L_0} \right)^3 \right). \tag{41}$$

For a delayed release to be possible, two conditions have to be satisfied. The first one is that the slab does not fail immediately after the cut, which according to Eq. (24), after substitution of forces and stresses from Eq. (34) imposes the following

restriction on friction:

$$\tan \varphi_{\min} < \tan \varphi, \tag{42}$$

where $\tan \varphi_{\min}$ is defined in Eq. (38). For Eqs. (37) and (39) this implies that that delayed release is only possible when

$$\tan \varphi_{\min} < \tan \varphi < \tan \varphi_{\max}(\lambda_s) \leq \tan \varphi_{\max}(\lambda_0), \tag{43}$$

where $\tan \varphi_{\max}$ is defined in Eqs. (38) and (40).

The Dyatlov case. The following parameters for the Dyatlov case have been adopted (see Supplementary Note 6):

$$\begin{aligned} \alpha &= 28^\circ, h_0 = 0.5 \text{ m}, h_c = 0.1 \text{ m}, h_p = 0.5 \text{ m}, l_p = 0.5 \text{ m}, \\ l_c &= 4 \text{ m} (21.6^\circ \text{ slope at the cut}), l_{c0} = 1.0 \text{ m}, g = 9.81 \text{ ms}^{-2}, \\ \rho_w &= 400 \text{ kg m}^{-3}, \rho = 300 \text{ kg m}^{-3}, K_0 = 0.5. \end{aligned}$$

A reasonable value of the friction in the weak layer²⁰ (see Supplementary Note 6) is $\varphi = 20^\circ$. This sets the upper bound of cohesion, for which a finite $h_{w0, \max}$ can still be determined, at $c \approx 440 \text{ Pa}$. This is well within the range reported by Jamieson and Johnson³³, and from Eqs. (37)–(40) we obtain

$$h_{w0, \min} = 0.24 \text{ m}; h_{w0, \max} = 0.44 \text{ m}.$$

By adjusting the deposition mass flux to $Q = 0.008 \text{ kg m}^{-1} \text{ s}^{-1}$, from Eqs. (36) and (41) we determine

$$\Delta t_{\min} = 7.2 \text{ h}; \Delta t_{\max} = 13.5 \text{ h},$$

which overlaps with the forensically estimated range of $\Delta t = 9.5 - 13.5 \text{ h}$ (see Supplementary Note 1). Extensive research on snow accumulation shows¹⁵ that this deposition flux requires average wind velocities in the range of $2-12 \text{ m s}^{-1}$ which is in agreement with data from nearby weather stations on the night of the accident (see Supplementary Note 3). The possible range of friction angles in Eq. (43) leading to delayed slab release is shown in Fig. 4a as a function of the slope inclination. Figure 4b shows the corresponding range of the critical heights of the wind-transported snow load that cause a delayed release for two cases: with and without sintering, described by Eqs. (37) and (39), respectively. Using Eq. (35), the times of delay are plotted as a function of the height of the wind-transported snow in Fig. 4c.

Dimensions of the failed slab. After the shear fracture propagated into the weak layer, the slab may fail in tension at the distance l_t from the cut, over the width B parallel to the cut. Here we determine the width B of the failed slab, assuming that the tension crack formed at the boundary of the wind-transported load defined in Eq. (9):

$$l_t = l_{cw} = L_0 \left(1 - \sqrt{\frac{h_c}{h_0 + h_{s0} + h_{t0}}} \right),$$

where the thickness of the slab is h_c . The areas A_0 and A_s of the initial and sintered slab cross-sections between the cut and the crack are derived by integration of Eqs. (7) and (9), respectively:

$$\begin{aligned} A_0 &= \frac{1}{3} h_0 L_0 \left(1 - \left(1 - \frac{l_t}{L_0} \right)^3 \right) + h_c (l_{cw} - l_c), \\ A_s &= \frac{1}{3} (h_0 + h_{s0} + h_{t0}) L_0 \left(1 - \left(1 - \frac{l_{cw}}{L_0} \right)^3 \right) \end{aligned} \tag{44}$$

and the equilibrium at the onset of the tension crack formation is given by

$$(A_0 \rho + (A_s - A_0) \rho_w) B g \cos \alpha (\tan \alpha - \tan \varphi) = h_c B \sigma_t + 2 l_{cw} h_c \sigma_s. \tag{45}$$

In Eq. (45) the left-hand side represents the net driving force acting on the slab, while the right-hand side is the sum of the tensile resistance at the back of the slab and the shear resistance at the sides of the slab, with σ_t and σ_s the tensile and shear strength, respectively. It is assumed that the contribution of the wind-transported snow to side resistance can be neglected, and the slab is thinning at the sides to h_c . Equation (45) can be rewritten to determine the width of the failed slab B:

$$B = \frac{2 l_{cw} h_c \sigma_s}{(A_0 \rho + (A_s - A_0) \rho_w) g \cos \alpha (\tan \alpha - \tan \varphi) - h_c \sigma_t}. \tag{46}$$

For the parameters of the Dyatlov case:

$$\varphi = 20^\circ, \sigma_t = 6.0 \text{ kPa}, \sigma_s = 5.2 \text{ kPa}, l_c = 4.0 \text{ m}, h_c = 0.1 \text{ m}, h_0 = 0.5 \text{ m}, h_{w0} = 0.5 \text{ m}$$

the tension crack can form at $l_t = l_{cw} = 4.95 \text{ m}$ resulting in $B = 8.8 \text{ m}$, consistent with the observed B/l_t ratios³⁴ and comparable to the width of the cut $b=6.5-7.5 \text{ m}$ (for a 4.5 m long tent, the cut had to be around $1.0-1.5 \text{ m}$ longer on each side).

Modeling the impact of the avalanche using the Material Point Method. We simulate the snow slab dynamics and snow block impacts using the model recently developed by Gaume et al.¹⁹. This model uses the Material Point Method, finite-strain elastoplasticity and a Cohesive Cam Clay constitutive relationship to

simulate snow and avalanche mechanics. We recall here the main characteristics of the model.

The mass and momentum balance equations are solved using the Material Point Method (MPM)³⁵ and finite-strain elastoplasticity. MPM is a hybrid Eulerian-Lagrangian method which is well suited to studying problems involving large deformations, collisions and fractures. It is thus suitable to analyzing the impact of a snow slab on a human body. ‘‘Particles’’ are used to track position, velocity and deformation gradients and a fixed background mesh is used to solve the balance equations. Here we used the Affine Particle In Cell (APIC) method for the transfer between grid and particles³⁶ which allows an exact conservation of momentum and angular momentum. In addition, we use cubic B-splines as shape functions which guarantees the continuity of the gradients at the nodes. More details about the MPM model and finite-strain elastoplasticity can be found in Gaume et al.¹⁹.

A mixed-mode yield surface²⁰ defined in the space of the p-q invariants of the stress tensor is used. The pressure p is defined as $p = -\text{tr}(\tau)/3$ where τ is the Kirchhoff stress tensor. The von Mises equivalent stress q is defined as $q = (3/2 \mathbf{s} : \mathbf{s})^{1/2}$ with $\mathbf{s} = \tau + p\mathbf{I}$ the deviatoric stress tensor (\mathbf{I} : identity matrix). The cohesive Cam Clay yield surface is given by

$$y(p, q) = (1 + 2\beta)q^2 + M^2(p + \beta p_0)(p - p_0) = 0, \tag{47}$$

in which p_0 is the pre-consolidation pressure, M is the slope of the critical state line and β controls the resistance to tension. At the end of the stress increment, if $y(p, q) < 0$ the material is elastic and follows Hooke’s law (with a Young’s modulus E and Poisson’s ratio ν) implemented in the framework of hyperelasticity with a St Venant – Kirchhoff model with Hencky strain³⁷.

If the snow fails, hardening or softening is simulated by expanding or shrinking the yield surface, respectively, through variations in p_0 . Compression leads to hardening, promoting compaction, while tension leads to softening, promoting fracture. The hardening law is formulated as a function of the volumetric plastic strain ϵ_v^p according to

$$p_0 = K \sin h(\xi \max(-\epsilon_v^p, 0)), \tag{48}$$

in which K is the bulk modulus and ξ is the hardening factor.

We model the human body as an hyperelastic solid (St Venant–Kirchhoff model with Hencky strain³⁷). The human body is simulated as a bulk solid with material properties taken from thorax impact tests performed by the automotive industry¹⁸. This approach allowed us not to simulate all individual bones and organs of the human body.

The geometry of the slope is taken to be the same as in the analytical model (Fig. 3). The bed surface satisfies a slip boundary condition. The thinning snowpack and the size of the wind-transported slab were also implemented according to the analytical model (see Section 1 of the Methods). The human body of a male of average size (1.70 m) lying on its back was simulated on a rigid bed surface.

In order to calibrate our model, we first simulate the impact of a 10 kg rigid block ($0.15 \times 0.15 \times 0.06 \text{ m}$) moving with velocity 7 m/s on a 3D human thorax with restrained back (see Supplementary Note 5 and Supplementary Movie 3). This setup corresponds to the automotive crash experiments performed by Kroell et al.¹⁸. We adjust the elastic modulus of the body in order to reproduce the same maximum normalized deflection of 0.49 that resulted in fatal injuries. Next, we perform a high-resolution 2D avalanche simulation using the main features known about the Dyatlov tent configuration (Fig. 1) so as to evaluate the snow slab impact velocity (up to 2 m/s , see Supplementary Note 5 and Supplementary Movie 2) and the range of typical snow block dimensions (up to 0.5 m^3 , see Supplementary Note 5 and Supplementary Movies 4–6). Next, we simulated the impact of snow blocks of $0.125, 0.25$, and 0.5 m^3 , 400 kg/m^3 density and impact velocity 2 m/s (same mechanical properties as the wind-slab) on a human thorax with restrained back. Finally, the severity of injuries was determined by relating the maximum normalized deflections to the Abbreviated Injury Scale (AIS, see Supplementary Note 6) presented by Kroell et al.¹⁸.

The following parameters for the Dyatlov case have been adopted (see Supplementary Note 6):

$$\alpha = 28^\circ; h_0 = 0.5 \text{ m}; h_c = 0.1 \text{ m}; h_w = 0.5 \text{ m}; l_{wc} = 5.0 \text{ m}.$$

The simulations were performed with a background mesh size $dx = 0.005 \text{ m}$, 4 particles per element in 2D and 8 particles per element in 3D.

We used the following snow and bed surface mechanical properties for the Dyatlov case (see Supplementary Note 6):

$$\begin{aligned} \rho &= 300 \text{ kg m}^{-3}, E = 8 \text{ MPa}, \nu = 0.3, \\ \beta &= 0.2, M = 0.8, p_0 = 30 \text{ kPa}, \xi = 5, \\ \rho_w &= 400 \text{ kg m}^{-3}, E_w = 17 \text{ MPa}, \nu_w = 0.3, \beta_w = 0.1, \\ M_w &= 0.8, p_{0w} = 100 \text{ kPa}, \xi_w = 5, \\ \varphi_{\text{bed}} &= 22^\circ. \end{aligned}$$

As mentioned above, mechanical properties of the human body are chosen based on thorax impact tests performed on human cadavers with restrained back¹⁸ to match the corresponding maximum deflection of 0.49 obtained upon impact of a 10 kg rigid mass with 7 m/s impact velocity. We used the following elastic modulus

and Poisson's ratio (see Supplementary Note 6):

$$E_{hb} = 0.215 \text{ MPa}; \nu_{hb} = 0.35.$$

Data availability

All data needed to evaluate the conclusions in the paper are present in the manuscript and the electronic supplementary material. Data supporting the plots of the manuscript is available at <https://doi.org/10.5281/zenodo.4302235>

Code availability

The code necessary to compute the delay for slab avalanche release and avalanche size can be found at <https://doi.org/10.5281/zenodo.4088052>. A description of the MPM model can be found in a previous publication at <https://www.nature.com/articles/s41467-018-05181-w>.

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Author contributions

J.G. conceived the key idea of the study, performed the numerical analysis and co-wrote the manuscript. A.M.P. developed the analytical model of delayed avalanche release and co-wrote the manuscript.

Competing interests

The authors declare no competing interests.

Additional information

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