Coupling nanoscopic tomography and micromagnetic modelling to assess the stability of geomagnetic recorders

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The recording of planetary magnetic fields is often attributed to uniformly-magnetised nanoscopic iron oxides, called single-domain. Yet, the main magnetic constituents of rocks are more complex, non-uniformly magnetised grains in single or multi-vortex states. We know little about their behaviour due to limitations in defining their precise shape and internal magnetic structure. Here we combine non-destructive Ptychographic X-ray Computed Nano-tomography with micromagnetic modelling to explore the magnetic stability of remanence-bearing minerals. Applied to a microscopic rock sample, we identified hundreds of nanoscopic grains of magnetite/maghemite with diverse morphologies. Energy barrier calculations were performed for these irregularly shaped grains. For some grains, these morphological irregularities near the transition from single-domain to the single-vortex state allow for multiple domain states, some unstable and unable to record the field for significant periods. Additionally, some other grains exhibit temperature-dependent occupancy probabilities, potentially hampering experiments to recover the intensity of past magnetic fields.

Measuring the magnetic properties and identifying the magnetic minerals in rocks is essential to palaeomagnetism, which studies Earth's magnetic field strength and direction throughout the planet's geological history[1]. While directional palaeomagnetic data is the only quantitative measurement that allows geoscientists to study palaeoconfigurations of ancient continental landmasses[2], databases of the past magnetic field strength (palaeointensity)[3] provide links to the complex magnetohydrodynamic processes occurring deep in Earth's core[4–6]. Quantifying the magnetic phases in rocks also provides essential information on globally scaled geological/climate events[7]. Rocks usually contain a mixture of magnetic particles in various sizes, including very stable nanoscopic uniformly magnetised grains (said to be in a single-domain (SD) state) and larger non-uniformly magnetised grains, either in pseudo-single-domain (PSD) or in multi-domain (MD) states. The palaeomagnetic theory is mainly based on Néel's ferromagnetic theory[8] for SD grains, which relies on the capacity of these particles to retain their original remanence for billions of years but accounts only for a small proportion of magnetic particles contained within a typical palaeomagnetic sample.

Palaeomagnetic analysis of a sample's magnetic mineralogy and stability is usually based on bulk magnetic measurements, often capable of detecting trace amounts of magnetic minerals. Although the data obtained through these analyses use statistical procedures to ensure their reliability, critical magnetic phenomena with geological/geophysical implications can sometimes be masked in bulk magnetic measurements. The complexity of natural geological materials and the diversity of composition/geometry of natural remanence carriers in rocks indicate that the conditions assumed by classical palaeomagnetic experiments can be far from ideal. A detailed understanding of the magnetic recording reliability requires a nanoscale interpretation of the magnetic fidelity of magnetic mineral grains.

Micromagnetic modelling, which explores the magnetic properties of a grain (or a population of them) as a function of their size, shape, chemical composition, and temperature[9,10], is an important tool that can bring a far greater understanding of the magnetic recording process. Micromagnetic calculations have revealed, for example, (i) that PSD structures, and in particular vortex states, so named due to their magnetisation being dominated by single or multiple vorticity centres, are probably the most common type of magnetic domain structure in natural iron oxides[11], and often capable of retaining their remanence for timescales longer than the age of the Solar System[12]; and (ii) the theoretical discovery of a non-stable magnetic configuration in grain sizes beyond the SD threshold[13], which can produce

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unexpected magnetic properties (e.g, the reduction of coercivities and thermal stability) and has the potential to greatly affect palaeointensity data[14].

Particle size is a very important determinant of domain state and, consequently, of magnetic stability[15], but geometry is also a critical factor. Although micromagnetic modelling of irregular particle morphologies can be achieved with the use of three-dimensional finite element meshes[10], most of the theoretical knowledge built on micromagnetics of iron oxides is based on regular euhedral crystalline habits[9,12–14,16–18]. Although natural processes can trigger regular crystal growth/alteration of iron oxides (such as bio-synthesis of magnetite by magnetotatic bacteria[19,20]), tomographic techniques on iron oxide-bearing rocks very often reveal irregularly shaped grains (e.g., de Groot et al.[21]). Consequently, it is important to understand how these irregular morphologies of particles might affect their magnetic properties, especially for grains within the palaeomagnetically PSD threshold.

Nano-tomography has been used to identify submicron magnetic minerals in a variety of geological materials, and micromagnetic models have been further employed to understand their magnetic properties. Einsle et al.[22] have combined Focused Ion Beam (FIB) nano-tomography to study metallic Fe grains in olivine, as well as electron diffraction, electron tomography, and atom probe tomography (APT), to obtain the three-dimensional internal structure of chondritic meteorite samples and subsequently model the properties of Fe-Ni materials[23]. FIB nano-tomography has also been paired with micromagnetic modelling to uncover the stability and magnetic hysteresis parameters of several different materials[11,24–26].

Although FIB nano-tomography is indeed a remarkable tool that has enabled more realistic morphologies in micromagnetic modelling, it is a destructive technique that offers little quantitative information on the density of the materials. A promising technique for high-resolution tomography is Synchrotron-based Ptychographic X-ray Computed Nano-tomography (PXCT)[27]. This technique allows for imaging the complex-valued transmissivity of a specimen and, when combined with non-destructive tomography, provides a quantitative 3D distribution of the full complex index of refraction[27] at unmatched nanoscale resolution[28,29]. PXCT has been successfully applied to study ~2 Ga microfossils[30], potentially indicating the presence of micron-sized magnetofossils whose properties were micromagnetically modelled[31]. Kuppili et al.[32] recently used PXCT to map magnetite inclusions within a zircon single crystal, clearly resolving Fe-rich inclusions 300 nm in size that were subsequently analysed using a micromagnetic model to reveal their domain structures. Despite the advancements demonstrated by Bellon et al.[31] and Kuppili et al.[32], who coupled PXCT with micromagnetic models to study the properties of PSD-grains in iron oxides, it remains crucial to determine if PXCT can achieve even higher resolution when imaging smaller iron oxide grains within the rock matrix, extending the technique's applicability to rock- and palaeo-magnetic studies.

In this study, we apply PXCT (Fig. 1) to image the magnetic minerals within a microscopic sample of a Neoproterozoic remagnetised carbonate, and further model their micromagnetic behaviour through finite element numerical models. The primary remanence (acquired during pre-to-syn diagenetic conditions) of carbonate rocks is very often substituted by a
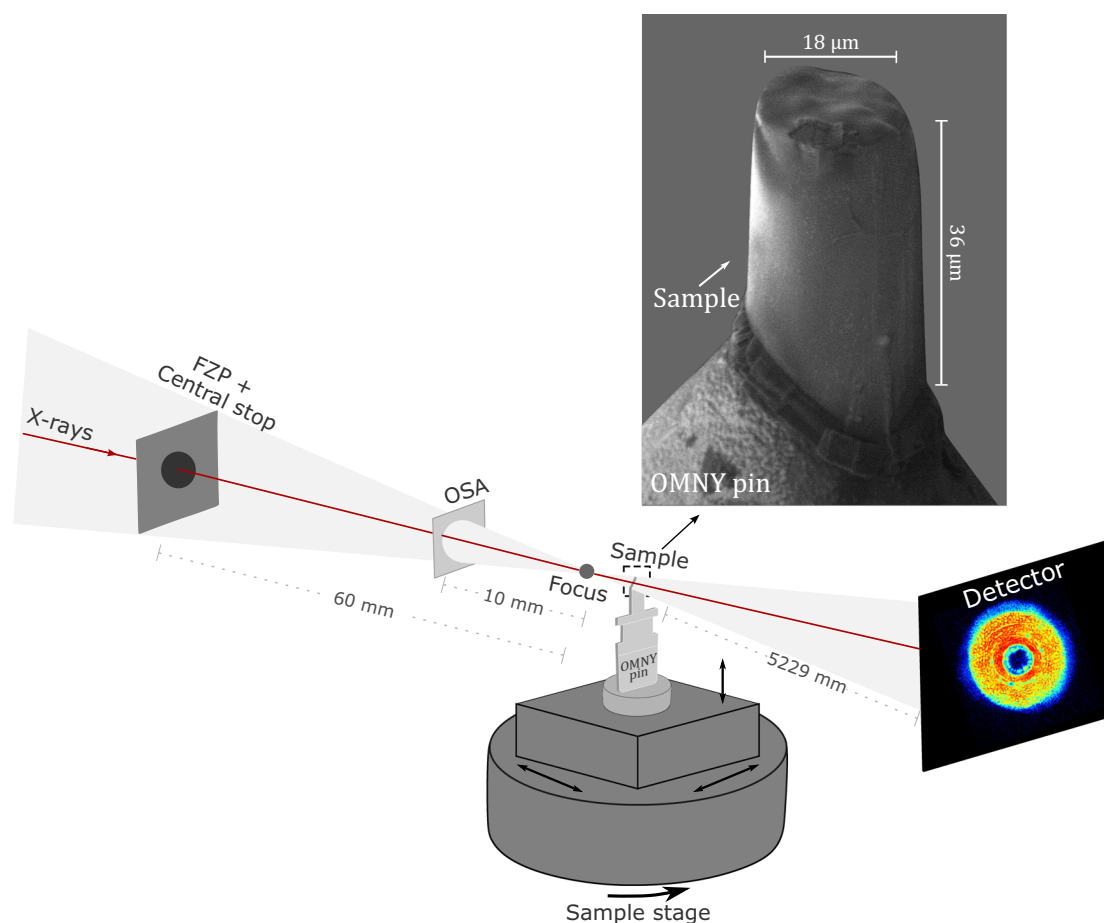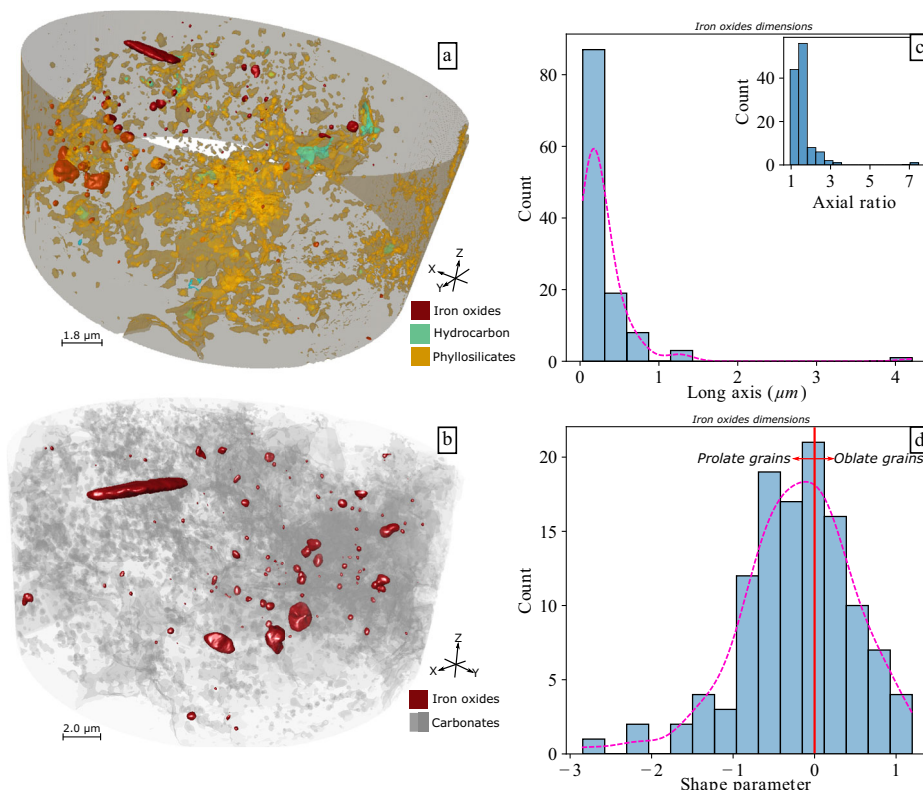

Fig. 1 | Experimental setup for the acquisition of PXCT data. X-rays are focused by a Fresnel Zone Plate (FZP), in combination with a central stop and an order sorting aperture (OSA), to define the illumination. The radiation reaches the microscopic pillar sample, mounted at the tip of an OMNY (tOMography Nano crYo) pin[74]. A scanning electron microscopy (SEM) image of the sample is shown in the upper corner of the figure. The sample stage allows a three-axial movement of the sample on top of a rotation to perform raster scans at different angles with respect to the X-ray beam. Diffraction patterns at each scan position are captured by a pixelated detector. The components sketched in this figure are not to scale. Details can be found in the text (or in the Supplementary Methods 1).

Fig. 2 | Reconstruction of the PXCT 3D electron density distribution after segmentation. The panels highlight the different materials in (**a**) and (**b**). Most of the iron oxide grains have a major elongation axis between 80 and 600 nm (**c**) and an axial ratio (P_1/P_3) <2. In (**d**), the shape parameter (ϵ, revisit Equation (4)) is quite scattered, showing a well-distributed population of triaxial ($\epsilon \approx 0$), prolate ($\epsilon \ll 0$) and oblate ($\epsilon \gg 0$) grains. The magenta dashed line represents the cumulative density distribution of the histograms.

secondary chemical remanence (CRM)[33,34] when new magnetic minerals grow or are chemically altered below their respective Curie temperature (T_c)[15]. These processes result in magnetic grains with a wide range of sizes and shapes, most of them within the SD/PSD grain size range, making them targets for micromagnetic studies of individual particles at the micro/nanoscopic scale. As the carbonate matrix is much less dense than the iron oxide particles, we have achieved a more detailed resolution than previous studies that applied PXCT for rock magnetism analysis. Our results provide new insights into the magnetic properties of natural remanence carriers in rocks and their thermomagnetic stability. Specifically, we have calculated energy barriers for the vortex states we have identified, as well as determined the effects of thermal energy on the multiplicity of domain states, which has implications for thermal-dependent experimental procedures.

Results

Nano-tomography

The processed tomograms representing the 3D electron density distribution of the specimen resulted in artifact-free volumes with a voxel size of 34.84 nm. An example is shown in the Supplementary File, Fig. S1a, while details about the PXCT measurements and data processing can be found in the Methods section. By using the accumulated histogram distribution of all of the data and the natural breaks in the distribution (Supplementary File, Fig. S1c), we have segmented five compositional classes (Supplementary File, Fig. S1d, Table S1). Our interpretations of the imaged materials presented here are also supported by previous chemical/magnetic analyses performed by Bellon et al.[35].

The classes are named according to their increasing electron density (Fig. 2). Class 1 yields the lowest electron density of $\mu = 0.31 \pm 0.11 e^- \cdot \text{Å}^{-3}$, also showing restricted volumetric occurrence. This material appears in small clusters within the sample (Fig. 2a, green colour), also showing a spatial correlation to localised porosities. We attribute this class to organic matter, specifically to bitumen. The geological formation (from which our sample comes) is naturally enriched in hydrocarbons[36], as biodegradation of the organic matter is also considered partially responsible for the growth of authigenic ferromagnetic minerals. Natural bitumen density might vary

depending on its formation and preservation, but the density of natural bitumens[37] has been reported to be $1.02-1.03$ g/cm^3, which reflects an electron density (Equation (2)) of $0.30-0.31 e^- \cdot \text{Å}^{-3}$.

Class 2 ($\mu = 0.65 \pm 0.08 \, e^- \cdot \text{Å}^{-3}$) material occupies a large volume of the sample (Fig. 2a, yellowish colour), and it is interpreted as a phyllosilicate. Smectite-illite has been previously identified as a major mineralogical constituent of these samples[35], as their conversion process (smectite to illite) is believed to release iron that sequentially reacts with the available oxygen to form iron oxides[38,39]. The density of such phyllosilicates will depend on their purity. Smectite's (end member smectite, EMS, < 2.3 g/cm^3) transformation to illite might be partial (illite-rich mixed-layer clays, IML, 2.4−2.7 g/cm^3), or complete (end-member illite, EMI, >2.7 g/cm^3)[40]. The spread distribution of Class 2 matches the expected density of a partial smectite-illitisation, as EMS and IML electron densities are between 0.69 and $0.72 e^- \cdot \text{Å}^{-3}$ (respectively).

Classes 3 ($\mu = 0.80 \pm 0.01 e^- \cdot \text{Å}^{-3}$) and 4 ($\mu = 0.88 \pm 0.03 e^- \cdot \text{Å}^{-3}$) comprise the majority of the rock matrix and are interpreted, essentially, as calcium carbonates (Fig. 2b). Class 3 matches the expected electron density of calcite (CaCO$_3$, $0.81 e^- \cdot \text{Å}^{-3}$), while Class 4 matches that of dolomite (CaMg(CO$_3$)$_2$, $0.85 \, e^- \cdot \text{Å}^{-3}$).

Class 5 gathers the highest mean electron densities of our sample ($\mu = 1.08 \pm 0.09 e^- \cdot \text{Å}^{-3}$), almost 20% larger than Class 4. The volumetric distribution of the material represented by this class is also quite distinct from the other ones, as these appear as individual grains spread in the matrix (Fig. 2b). They also represent a wider electron density distribution, with values that reach as far as $1.24 e^- \cdot \text{Å}^{-3}$. We interpret this material as the iron oxide particles in our sample. The electron density upper limit of Class 5 was also observed for partially oxidised magnetite/maghemite in previous PXCT studies[30], but is slightly lower than expected from their theoretical densities. Several aspects could implicate such discrepancies, for example: (i) chemical impurities, crystalline imperfections and oxidation; (ii) density is size-dependent in nanomaterials, being lower/greater than a correspondent macrometric material depending on the lattice parameter[41]. The most likely reason though is related to the partial volume effect, i.e, for a given small volume the measured electron density has a large contribution from the

Table 1 | Magnetic properties of the iron oxides used in our micromagnetic models at 20 °C

Mineral	Anisotropy	A_{ex}	K_1	Ms	Ref
Magnetite (Fe_3O_4)	Cubic	$1.330 \cdot 10^{-11} Jm^{-1}$	$-1.304 \cdot 10^4 Jm^{-3}$	$4.800 \cdot 10^5 Am^{-1}$	94
Maghemite (γFe_2O_3)	Cubic	$1.000 \cdot 10^{-11} Jm^{-1}$	$-4.600 \cdot 10^3 Jm^{-3}$	$3.800 \cdot 10^5 Am^{-1}$	15

A_{ex} is the exchange stiffness constant, K_1 is the anisotropy constant, and M_s is the magnetisation saturation.

voxels at the interface with its surrounding material, which can affect the final average density value. In our case, we have particles of a few hundred nanometers sampled with a 3D resolution, therefore a large proportion of the selected volume for density quantification may have a contribution from the density of the surrounding material. If the surrounding material has a lower density, the density will be underestimated. Partial volume effects have been considered before, e.g., in the segmentation of volumes of nanoporous material obtained by PXCT[42]. Prior applications of synchrotron-based techniques, specifically X-ray Fluorescence (XRF) and X-ray Absorption Near Edge Spectroscopy (XANES), have been utilised to identify magnetite/maghemite in a sister sample currently undergoing nano-tomographic analysis[35]. This additional evidence further supports our interpretation, as we follow the micromagnetic modelling of their properties.

Following the processing, segmentation, and mesh generation (refer to Methods for clarity), we have identified 118 distinct grains of iron oxides with varied shapes and sizes. Due to their high irregularity, we will discuss their sizes based on the ratios of the grains' main axes ($P_1 > P_2 > P_3$). More than 95% of the major axes are between 80 and 600 nm (see Fig. 2c), and 68% are smaller than 250 nm. The axial ratio (P_1/P_3) evidences that although these grains are irregular, the size of major and minor axes of most of them do not show big discrepancies, which is reflected in the overall rounded morphologies (Fig. 2c). The smallest particles of our sample are within the spatial resolution of the tomography and might carry uncertainties in the imaged morphology. Grains near the transition between the superparamagnetic state and the SD state (≈ 30 nm) cannot be imaged by our tomographical measurements. However, the smallest grains we have imaged (approximately 50 nm^3), despite greater morphological uncertainties, remain scientifically valid, as their approximate size is sufficient for micromagnetic modelling. We can more effectively access the morphologies by evaluating all three axes through the shape parameter (ϵ, Equation (4)). The great majority of them are triaxial to oblate-like particles ($\epsilon \geq 0$), but there is still a considerable amount of prolate-like grains ($\epsilon < 0$, Fig. 2d). The largest particle identified in our sample, quite isolated in size, is a very oblate ($\epsilon > 0$) grain, which also corresponds to the biggest axial ratio in Fig. 2c at a value just over 7.0. The presence of larger grains poses a computational challenge for micromagnetic modelling. Generating finite element meshes for their morphology while adhering to the exchange length (l_e)[43] as the maximum element size leads to excessive processing times. Consequently, we have focused exclusively on the finest grains (≤ 1000 nm), which are more likely to exhibit the vortex state. As a result, from the initial set of 118 grains, we have excluded five particles in the subsequent micromagnetic modelling steps, working with a total of 113 grains. A spreadsheet with the morphological characteristics and summarised magnetic properties (which are further discussed) of all of these grains is also provided in a public repository[44].

The magnetic grains we image in this work result from growing mechanisms that occurred below the magnetite's Curie temperature in sedimentary rocks, i.e., they originally bear a chemical remanence (CRM). In terms of micromagnetic modelling, the origin of these grains is not relevant to our calculations, as the major parameters influencing our results are the dimensions, morphology, and composition of these grains[10]. In our case, grains were discretised as finite element meshes of a material with a homogeneous chemical composition. Comparing morphologies is not a direct task, but the range of morphologies depicted in Fig. 2d is similar to that of inclusions of magnetic minerals hosted in igneous rocks[24]. Therefore, we consider the implications of our further discussions to apply to any kind of rocks bearing irregularly shaped nanomagnetic grains (composed of magnetite/maghemite).

Micromagnetics

In this section, our objectives are (i) to assess the stability of remanence by investigating domain states; and (ii) to explore the conditions under which different domain states are favoured at varying temperatures. Furthermore, we identify the temperature intervals over which these domain states dominate.
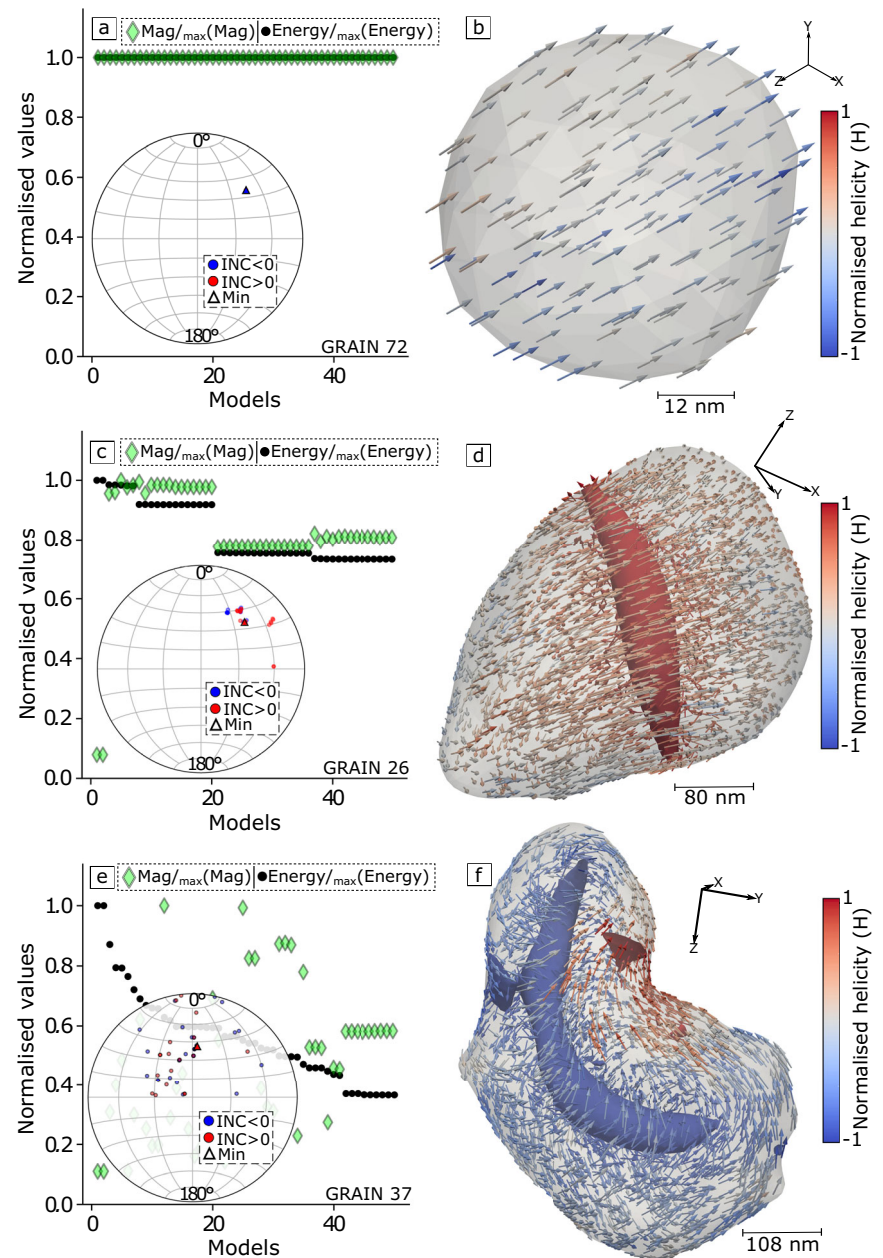
Identifying the magnetic structures of each grain involves running several models for each grain's geometry to search for local energy minimum (LEM) in the magnetic domain states (see Methods)[10]. The LEM with the lowest energy will usually represent the most stable domain state for each grain. Model LEM solutions were obtained using MERRILL[10] (an open-source 3D micromagnetics software package), where the magnetic domain states structures are represented by a unit vector at each node of the model mesh geometry. Here, for simplicity, the remanence of grains are shown as values normalised by their saturated magnetic state (Ms, Table 1). Both the remanence (Mr) values and the topology of the magnetic domain structures observed for magnetite and maghemite were very similar (Supplementary File, Fig. S3a), as were the corresponding values of their magnetic free energies (Supplementary File, Fig. S3b). This is expected since the minerals share similar magnetic material properties (Table 1). Thus although most of the results we describe here are for magnetite, we anticipate very similar behaviour for maghemite.

We observe a great variety of domain states (Fig. 3), which we categorise following the same approach of other studies[11,12,14,18]. As expected, SD states dominate in the smaller particles, which in our case are also the most rounded morphologies (Fig. 3a, b). With increasing grain sizes and as morphologies become more irregular, non-uniformly magnetised domain states arise as: single-vortex (SV) structures (Fig. 3c, d), with a vortex core aligned along a specific axis; and multi-vortex (MV) structures, which only appear for the largest grain sizes considered in our study. As grain size increases it becomes possible to nucleate multiple different domain states. These different domain structures can sometimes simply be SV states, where different LEM vortex core alignments may occur within an irregular grain morphology (Fig. 3c). Larger grains ($P_1 > 200$ nm) might result in a variety of domain states with differently twisted vortex cores, or high energy LEM's with multiple vortex cores in the same grain (Fig. 3e).

The normalised magnetisation of magnetic particles has important implications for the identification of a given domain state through bulk magnetic properties[15], particularly for non-uniformly magnetised grains, which likely dominate the assembly of stable magnetic carriers in rocks[11]. When we examine the range of a grain's LEM magnetisation that can be nucleated in each grain, our results indicate that most grains have Mr/Ms < 0.5, where SV structures are dominant. None of the lowest energy states observed in the LEM models of grains with multi-vortex structures, whether composed of magnetite or maghemite, show a Mr/Ms exceeding 0.5. Remanences greater than such threshold for MV particles have only been observed for higher energy states, which are less stable, while Mr/Ms > 0.5 (as in Supplementary File, Fig. S3a) are essentially displayed by either SD or SV-like structures.

The temporal stability of each grain was determined using the Nudged-Elastic-Band method[12,45]. This allows us to determine the minimum energy path (MEP) between any two given domain states. For each grain, we took the lowest energy state (from a set of 50 random LEM states) and calculated the minimum energy path to its anti-parallel state. In the case where a new

Fig. 3 | Examples of different types of domain states in magnetite and their behaviour, as acquired through our micromagnetic models. On the left side, we have compiled the magnetisation (green diamonds) and the corresponding magnetic energy (black dots) for each of the 50 LEM models of a specific grain. These values are normalised by the respective maximum values (of either magnetisation/energy) among the fifty models. The stereographic projections within the plots display the direction of the magnetisation for all models by converting the magnetisation components in the x (M_x), y (M_y), and z (M_z) directions to declination (DEC = $\arctan(M_y/M_x)$) and inclination (INC = $\arctan(M_z/\sqrt{M_x^2 + M_y^2})$). The inclination is coloured according to its polarity (red for positive and blue for negative), and the triangles indicate the direction of the LEM state with the lowest energy (Min). On the right, the minimum free energy model of the corresponding grain is depicted, where the arrows indicate the direction of the magnetisation, and the vortex structures inside are the isosurface hued by the helicity. SD grains show (**a, b**) practically no difference between the models, whereas SV can exhibit a variety of possible domain states (**c, d**) with distinct magnetisation (and associated energies), especially when the morphology of the grain is highly irregular (**e, f**).
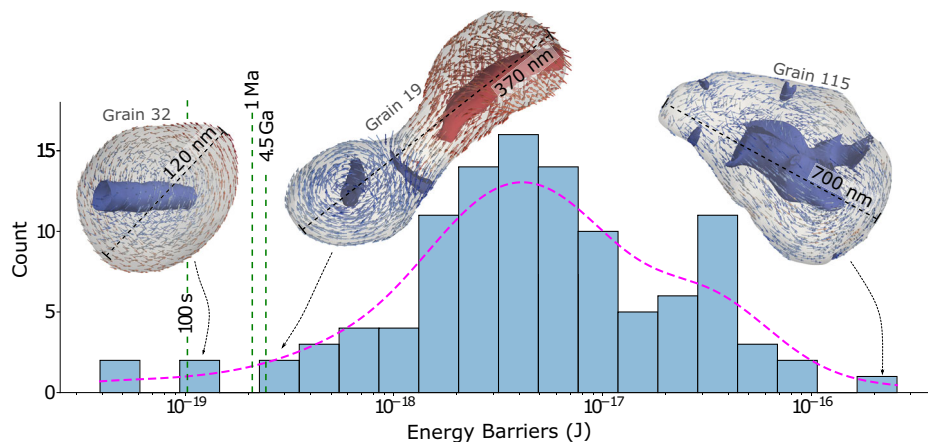

minimum was observed along the MEP, we subdivided the path at the new intermediate minimum and searched the grain for a new MEP. In this way, we obtained the energy barriers only for the lowest energy LEM state. In this study, we have chosen not to investigate the stability of higher energy (and thus less abundant) states we encountered. The energy barriers from the MEP were converted into magnetisation relaxation times (τ) using the Néel Arrhenius (Equation (9)).

In Fig. 4 we show a spectrum of energy barriers, where the vast majority of grains yield relaxation times that far surpass the age of the Solar System. The "eternal" stability includes SD, SV, and MV states, the latter having the highest energy barriers. However, four grains have small τ values. Grain 32 ($\epsilon = 0.78$, $P_1 = 122$ nm, $P_1/P_3 = 1.27$), for example, yields a single vortex configuration (Fig. 4), but our simulation indicates that thermal energy would overcome magnetic energy in $\tau \approx 3$ h. The other three grains are also elongated but of grain sizes close to our tomography pixel size (e.g., Grain 113, $\epsilon = -0.35$, $P_1 = 49$ nm, $P_1/P_3 = 1.21$). Their relaxation times are mostly instantaneous (Fig. 4), which points out that not only size but morphology, is critical in determining domain stability for such small grain sizes.

As stated, when a particle assumes a multiplicity of possible domain states, the issue regarding which of the LEM states is the more likely can be resolved in the presence of a clear energy minimum, as observed in Fig. 3c, e. However, some grains may exhibit more complex behaviour, where the LEM states yield distinct Mr but similar energies. Boltzmann probability distribution of states (p_i, Equation (8)), shows that for a small number of states at a given temperature, even a small difference of 2% in magnetic energy (e.g., Grain 25 in Supplementary File, Fig. S4) between the lowest energy LEM state and other states will result in a ≫99.99% occupancy rate of lowest energy state. However, the prevalence of a given state is sometimes also a function of temperature, with the most favoured domain state changing on heating or cooling. We discuss below the case of SV/SD grains with LEM states of similar energies and distinct magnetisations. We intend to investigate how the magnetic energy of these states evolves with an increase in thermal energy, up to the Curie temperature of magnetite. Our observations indicate that the balance between magnetic and thermal energy will also depend upon both the grains' size and morphology. The SV behaviour can be classified into three groups. The first corresponds to the

Fig. 4 | Compilation of the computed magnetic energy barriers for each of the lowest energy LEM states across a minimum energy path to its anti-parallel state, using the Nudged-Elastic-Band method[12,45]. This energy barrier is then applied to the Néel-Arrhenius[8] equation to calculate the relaxation time (at 20 °C) for the transition τ from one domain state to another. The magenta curve represents the density of the state's distribution. The vertical dashed (green) lines correspond to τ for 100 seconds, 1 million years, and 4.5 billion years. Most of the states exhibit stabilities that far surpass the age of the Solar System (as seen in the MV states for Grains 19 and 115). However, a minority of them, such as Grain 32, are unstable magnetic recorders, representing the magnetically unstable zone (MUZ) between the transition of the SD to the ESV state. The colours shown for the arrows within the grains (as well as the vortex structures) have the same meaning as the examples shown in Fig. 3 (see colour bar for helicity). Calculations were performed assuming magnetite as the mineral phase.

well-behaved grain, where a single type of domain state will prevail up to the Curie temperature (Supplementary File, Fig. S4). An example is Grain 25 ($\epsilon = 0.43$, $P_1 = 270$ nm, $P_1/P_3 = 3.03$), where p_i indicates that a flower state (of higher magnetisation and lower energy) will prevail over the other competing SV states. The second group represents grains where the energy of one state dominates at lower temperatures, but the magnetic energy becomes similar to other LEM states as the temperature increases (Fig. 5a, b). For Grain 68 ($\epsilon = 0.60$, $P_1 = 124$ nm, $P_1/P_3 = 1.53$), e.g., a single vortex state (Fig. 5b) dominates until 450 °C but thereafter p_i becomes equally distributed between the other domain states, indicating that any of these states with distinct Mr could be assumed. Finally, the third group behaves poorly. In these grains, the magnetic energies of different domain states are almost indistinguishable with increasing temperature (Fig. 5c, d). For grain 48 ($\epsilon = 0.07$, $P_1 = 91$ nm, $P_1/P_3 = 1.17$), up to ~300 °C there is a frequent redistribution of domain states (Fig. 5d'), and for T above 300 °C p_i is equally occupied by the three different states.
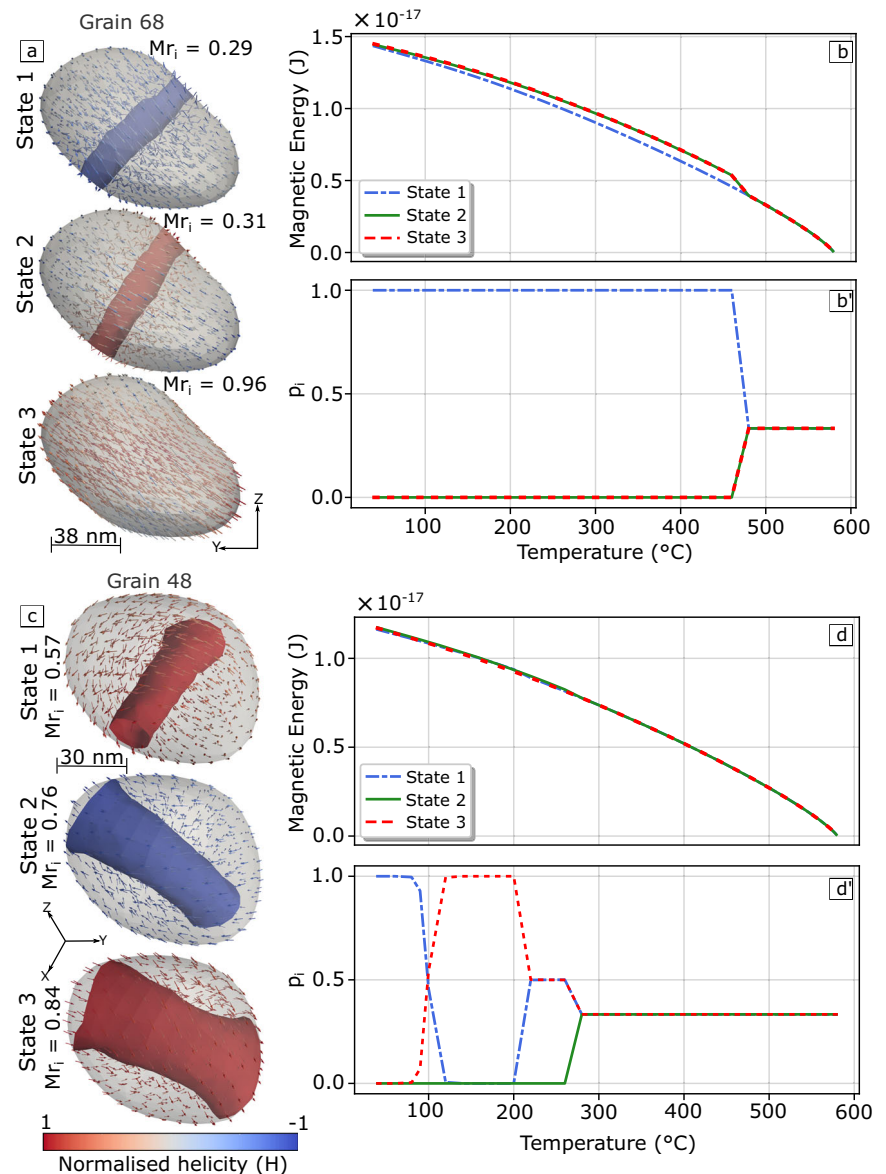
We have also modelled the hysteresis loops and backfield curves for each of the studied grains (see "Methods"), accounting for shape anisotropy effects by running models in different field directions and averaging their results. In terms of normalisation, the LEM grain's magnetisation (Mr) differs from those obtained from the saturation of remanence (Mrs) (see Figs. 6, 7). Both of these represent the zero-field remanence. However, Mrs is determined from hysteresis loop averaged over different applied field directions, while Mr is obtained through an energy minimisation starting from a random initial guess. An important effect of averaging over distinct field directions is that saturation (i.e. complete alignment of the magnetisation in the direction of the applied field) at a given field strength will strongly depend on the field direction with respect to the magnetic anisotropy axes of the grain. A particle's anisotropy is often controlled by its morphology, which then determines how easily a grain becomes magnetically saturated. Therefore, we consider the saturation parameter of magnetic hysteresis, Ms, as the corresponding value of magnetisation for each averaged curve at 250 mT. We apply boxplot statistics to discuss some of the magnetic properties in terms of all grains. As also highlighted in the previous subsection, magnetite and maghemite properties are very similar and produce practically indistinguishable results (Fig. 6). To avoid redundancies, we henceforth discuss only the properties of magnetite.

Except for a few outliers, the Ms is essentially the same as the theoretical one for magnetite (0.99 ± 0.01). Mrs/Ms span from 0.0035 to 0.70, whereas only SD and SV states occupy values greater than 0.5. Discrepancies emerge when comparing Mr/Ms with Mrs/Ms. There is an important influence of the field direction in the whole averaged loop, which can generate very

different curves with distinct Mrs for each field direction (Fig. 7a, c). For a monodispersion of SD grains whose data is sampled from field directions uniformly distributed over the sphere, we would expect Mrs/Ms to be $\gtrsim 0.5$. For grains whose minimum energy models yield Mr/Ms $\gtrsim 0.5$, the resulting Mrs/Ms from the simulated random distribution of grains can be 50% smaller (Supplementary File, Fig. S5a, b). The difference is even greater for particles whose Mr/Ms $\lesssim 0.5$, which can result in Mrs/Ms up to 80% smaller than the magnetisation of its lowest LEM (Fig. 7). This effect increases with grain size, the larger grains being able to accommodate a larger number of domain states each with a distinct remanence, but this effect is consequently averaged during the field-dependent magnetic experiments or numerical simulations of random distributions of such grains. Bulk coercivities (Bc) span a large interval (0.64−80.59 mT, Fig. 6), most of them within expected values for magnetite[1] (11.41 ± 11.86 mT). The coercivity of remanence (Bcr) obtained from the backfield curves is also within the expected range (46.27 ± 25.32 mT), but several grains present higher values (e.g., Fig. 7b), some of these being greater than 100 mT. These high Bcr values were also reported by Williams et al.[46] for highly prolate and slightly oblate grains. In our case, we observe these anomalous Bcr values for varying degrees of both prolateness and oblateness.

The remanence (Mrs/Ms) and the coercivity (Bcr/Bc) ratios are important indicators of magnetic domain states[47]. Nikolaisen et al.[24] have also explored nanotomographic data of iron oxide inclusions in silicates to micromagnetically model hysteresis and backfield parameters. We plot their results alongside our own in Fig. 8, where we further explore coercivity and remanence ratios by making use of the bilogarithmic Day plot (Bcr/Bc vs Mrs/Ms)[47,48], as well as the Néel's diagram (Mrs/Ms vs Bc)[8] and its sister plot (Mrs/Ms vs Bcr). The Day plot carries markings of conventional divisions[47,48] for SD (Mrs/Ms $\geq$ 0.5, Bcr/Bc $\leq$ 2), PSD ($0.5 >$ Mrs/Ms $> 2 \times 10^{-2}$, $5 >$ Bcr/Bc > 2) and MD (Mrs/Ms $> 2 \times 10^{-2}$, Bcr/Bc > 5) states (Fig. 8a). These limits, as well as the interpretation of such parameters, have been questioned[11,49] to be non-representative of the many processes that can lead to variations of such ratios. We keep the Mrs/Ms fields simply as guides to the eye. On the Day plot, we have found two well-defined clusters: for the first one, SD grains and some SV grains group near Mrs/Ms = 0.5; for the second one, grains follow a linear trend, $y = (−0.765 \cdot x) − 0.682$, $R^2 = 0.93$. The smallest grains (100 nm$\leq$) are within the first cluster (Fig. 8a). The grains aligned along the linear trend, which includes both SV and MV states, extend from the original PSD down to the MD region. Besides such an obvious mismatch with the traditional PSD field, some SV states exhibit extremely high Bcr/Bc ratios (Fig. 8a), especially associated with larger grains. When all of the backfield and

Fig. 5 | Multiplicity of domain states for grains of magnetite. States with similar energies but distinct magnitudes of magnetisation and their temperature dependence are explored. In the first example (**a**), States 2 and 3 exhibit slightly higher energy with a temperature increase (**b**). The Boltzmann probability (p_i, Equation (8)) demonstrates that State 1 will prevail over most of the evaluated temperature range (b'). However, after reaching a certain temperature threshold (approximately 450 °C), the probabilities of these domain states to occur become equal. In the example in (**c**), this effect is more problematic, as the energies of the states remain practically the same throughout the entire range of temperatures (**d**), leading to swapping of probabilities between the states (d') up to nearly 300 °C, from which the p_i becomes equally distributed.

hysteresis are averaged together, our sample produces averaged ratios of Mrs/Ms = 0.117 and Bcr/Bc = 2.45, which falls within the original PSD field of the Day plot (Fig. 8a).

On Néel's diagram (Fig. 8b), the same clusters are also present, which is expected since they share the same ordinate axis. Bc of the first cluster has a range of values, but the other grains show a linear increase of remanence with the bulk coercivity, $y = (1.215 \cdot x) - 2.282$, $R^2 = 0.91$. This relationship is inversely proportional to the coercivity of remanence (Fig. 8c) for which, although more dispersed, Bcr increases as the remanence ratio decreases, $y = (-1.212 \cdot x) + 0.619$, $R^2 = 0.56$. For all the properties here discussed, there is no clear relationship between a magnetic property and the respective elongation parameter of a grain. However, even for these irregularly shaped grains, there is an apparent correlation between the magnitude of Bcr and the grain size. When we put together experimental data[48,50–60] and the results of our models, despite a large spread of values, the coercivity of remanence increases to maximum at grain sizes between 600−700 nm (Fig. 8d).

As shown in Fig. 8, the parameters obtained in our models align well with those of Nikolaisen et al.[24]. Both datasets exhibit similar clusters, although there is greater dispersion in their models. One notable difference is that we do not observe a tendency of MV states in the upper left of the Day

plot (Fig. 8a). Instead, they are distributed along the trend line we described earlier and are particularly associated with larger grain sizes.
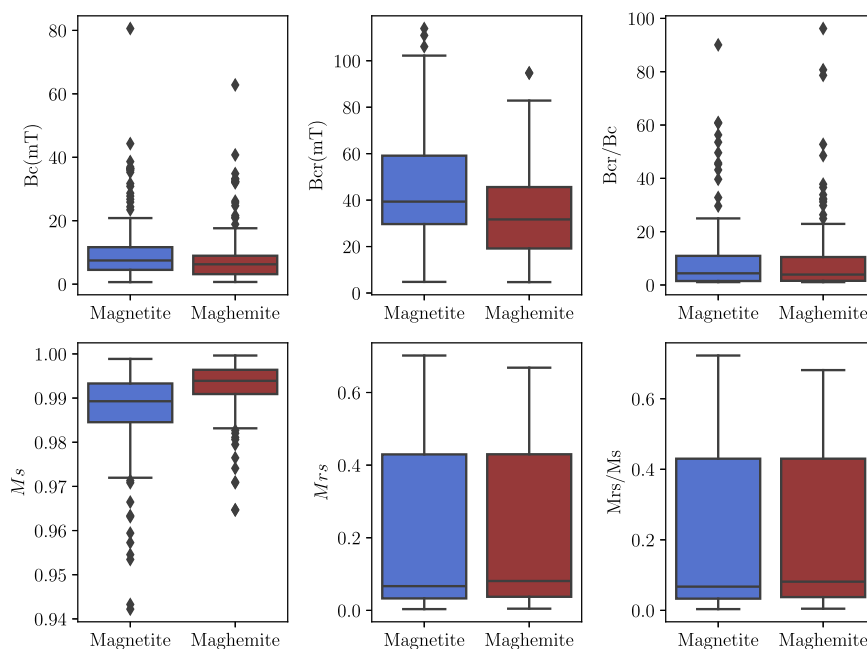
Discussion
On the magnetic properties of natural nanoscopic grains
Although not surprising, an important aspect of our results is that the magnetic properties of magnetite and maghemite, as demonstrated in Fig. 6, as well as their domain states, are practically indistinguishable at ambient temperatures. The challenge of differentiating between these two magnetically soft minerals can be addressed through the use of temperature-dependent experiments[1], which are proven to be essential for properly interpreting environmental magnetism data and inferring exogenous processes[7], but often expose the samples to chemical or domain state change.

Mrs/Ms and Bcr/Bc ratios derived from magnetic hysteresis and backfield curves can be characteristic of an entire assemblage of grains. It is natural, therefore, that various processes impact the comparison of these ratios in the Day plot[47,48]. Such processes include mixtures of magnetic minerals with distinct coercivities, and/or mixtures of grains in distinct domain states[61,62], as well as surface oxidation, mineral stoichiometry, and the intrinsic magnetic properties of each grain[49]. Nevertheless, our data demonstrates that for both magnetite and maghemite (Fig. 8a), two well-

Fig. 6 | A compilation of parameters obtained from the magnetic hysteresis loops and backfield curves for magnetite (blue) and maghemite (brown) is presented using boxplot statistics. These parameters correspond to averaged curves obtained for each grain in twenty different directions (refer to "Methods" for details). Bc represents the bulk coercivity, Bcr is the coercivity of remanence, Ms indicates the magnetisation saturation of the averaged loop at the maximum field, and Mrs is the remanence of saturation. Black diamonds are statistical outliers. As illustrated, magnetite and maghemite exhibit practically indistinguishable properties.

defined clusters exist. One is occupied by higher remanences (solely featuring SD and SV states), and the other displays a linear trend cutting across the Day plot towards lower remanence ratios and higher coercivity ratios. The Day plot trend we observe for SV grains closely follows that found in idealised grains by Williams et al.[46], although, for our irregular grains, we do not observe a well-defined correlation with grain shape. As grain sizes increase, so does the internal demagnetising field[9,15], until it grows sufficiently strong to collapse into a lower energy domain state. Lower energy domain states often imply a decrease in remanence, which we observe in our analysis with the increase in Bcr (Fig. 8b). Our data also suggests a peak for Bcr with the increase of grain size around $600-700$ nm (Fig. 8d), aligning considerably with experimental data of grains with distinct morphologies and sizes[48,50-60]. This same trend is followed by the data from Nikolaisen et al.[24], which strengthens our belief[46] that Bcr should progressively increase from grain sizes around 100 nm up to a few hundred nanometres, and then progressively decrease as MV states appear.

In our simulations, the influence of superparamagnetic (SP) grains is not resolved. The combination of all grains in hysteresis and backfield curves suggests that a high quantity of SP particles could potentially decrease Mrs/Ms and increase Bcr/Bc[47]. Careful interpretation of these diagrams is necessary. However, with well-established magnetic mineralogy supported by other analyses such as thermal demagnetisation of synthetic remanences, thermomagnetic curves, first-order reversal curves (FORCs), and chemical/imaging analyses, the Day plot, Néel's diagram, and related plots can provide useful insights.

Magnetic hysteresis, including FORCs[63-65], heavily rely on the Mrs/Ms to infer field-induced states and not remanence states. One of our crucial observations is that unless the grains are SD, the true remanence of a grain will be potentially underestimated. While this may not be a significant concern for very fine particles exhibiting SD-like behaviour (Mrs/Ms $\gtrsim 0.5$), it can become a pronounced phenomenon for larger grain sizes. Experimentally, magnetic hysteresis, backfield curves, isothermal remanence curves (IRMs), and FORCs are performed using a fixed field direction. As illustrated in Fig. 7, the applied field's direction can induce variable magnetic properties due to the grains' shape anisotropy. For a population of irregular grains randomly oriented, changing the field direction may not significantly decrease this effect because rocks might have millions of magnetic grains. However, for materials with a well-oriented magnetic fabric (e.g., inclusions in minerals, and highly deformed rocks), conducting these measurements in variable

field directions (or changing sample orientation) might enhance the determination of Mrs.

Temporal and thermal stability of irregularly shaped grains
The capacity of magnetic minerals to retain their remanence over geological time-scales is crucial for planetary studies, as rock-magnetic recordings provide information on Earth's evolution, such as tectonics[2], the timing of inner core nucleation[6], and even the early stages of solar nebula development[66]. Néel's theory[8] has long been employed to demonstrate that SD grains can retain their remanence over billions of years. Although this domain state is highly stable, it spans only a very limited range of sizes, and most terrestrial and extraterrestrial magnetic materials will contain a much broader range of grain sizes.

Nagy et al.[12] have calculated the temporal stability of equidimensional truncated octahedron grains of magnetite ($80-1000$ nm) in the SV state and have demonstrated that, except for grains between 80 and 100 nm, their stability surpasses the age of the Solar System. Our calculations for non-euhedral morphologies, which are more realistic for oxide grains in most natural systems, generally align with this interpretation (Fig. 4), demonstrating that most SV and MV grains can also retain eternal stability at environmental temperatures. Nagy et al.[12] also pointed to a magnetically unstable zone (MUZ) for grain sizes between 80 and 100 nm, for which the relaxation times are near instantaneous at room temperature. In the MUZ for magnetite, the SV domain state is aligned with the hard magnetisation axis (HSV), while large SV grains align their magnetisation with the easy magnetic anisotropy axis (ESV). Wang et al.[13], have shown that within the MUZ ($68-100$ nm) the grains' evolution proceeds as SD $\rightarrow$ HSV $\rightarrow$ ESV. For such, grains within the MUZ were shown to occupy about 20nm for euhedral and also for rounded particles[18,67]. Four of our modelled grains within the MUZ size range proposed by Nagy et al.[12] are unstable at room temperature, e.g. Grain 32 (Fig. 4) with an elongation axis of 122nm. Furthermore, several of the grains (with variable morphology) that we studied have P_1 within the proposed range dimensions of the MUZ (e.g., Grain 135: $\epsilon = -0.93$, $P_1 = 80$ nm, $P_1/P_3 = 1.39$ | Grain 48: $\epsilon = 0.07$, $P_1 = 91$ nm, $P_1/P_3 = 1.17$), and yet they are highly stable. Therefore, we suggest that the transition of SD to HSV (consequently at the onset of the MUZ) is strongly affected by the morphology of the grain.

Figure 3 further highlights that a multiplicity of domain states may occur in one or more temperature intervals and that the likelihood of a grain being able to nucleate multiple domain states increases with grain size. This
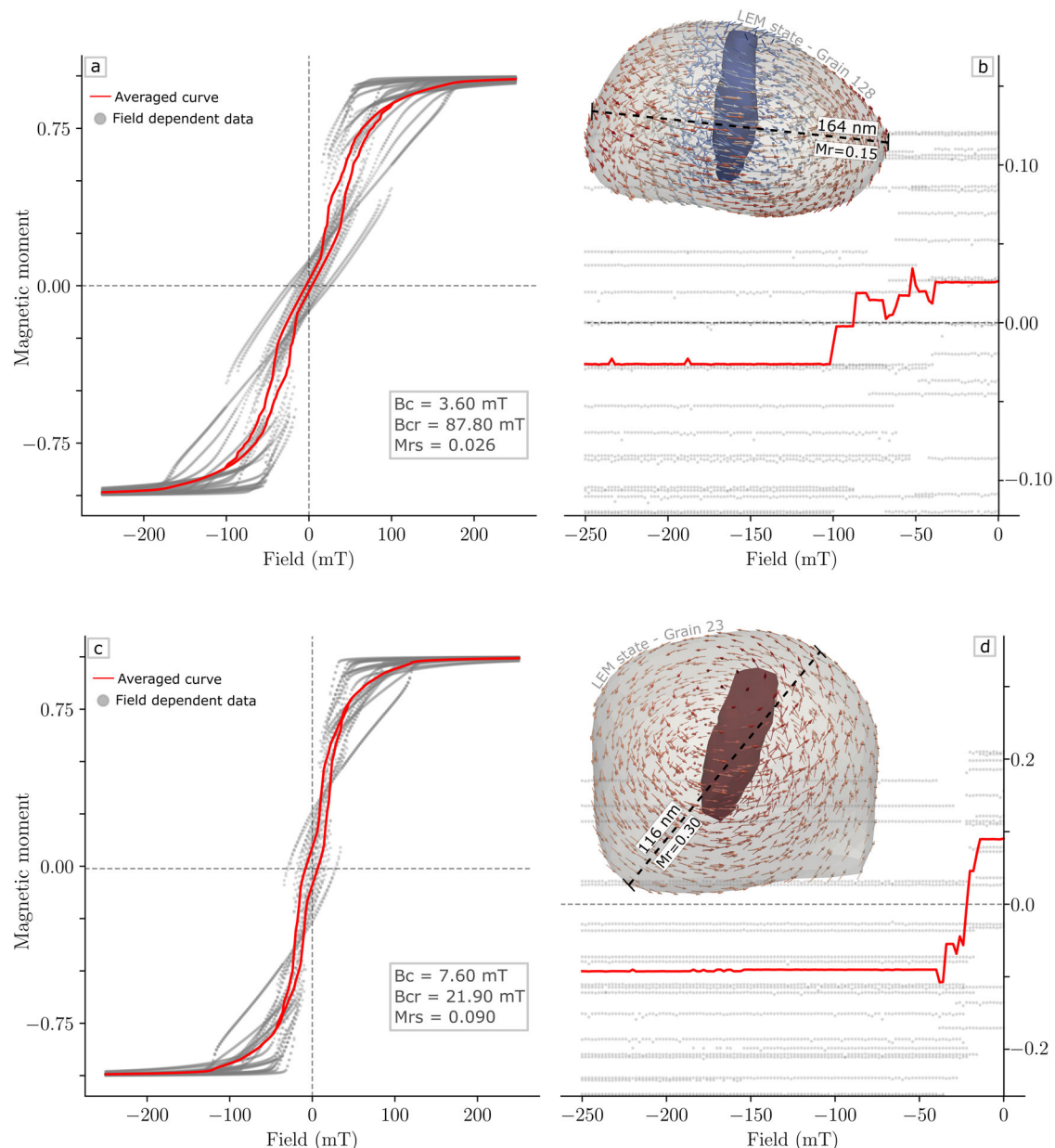
Fig. 7 | Field-dependent magnetic properties of irregularly shaped magnetite grains and the impact of shape anisotropy in various field directions. Examples of magnetic hysteresis (**a**, **c**), backfield curves (**b**, **d**), and their parameters (for magnetite) are shown. The grey dots represent the field-dependent data, and the red curves depict their averages. Notably, for both types of simulated exp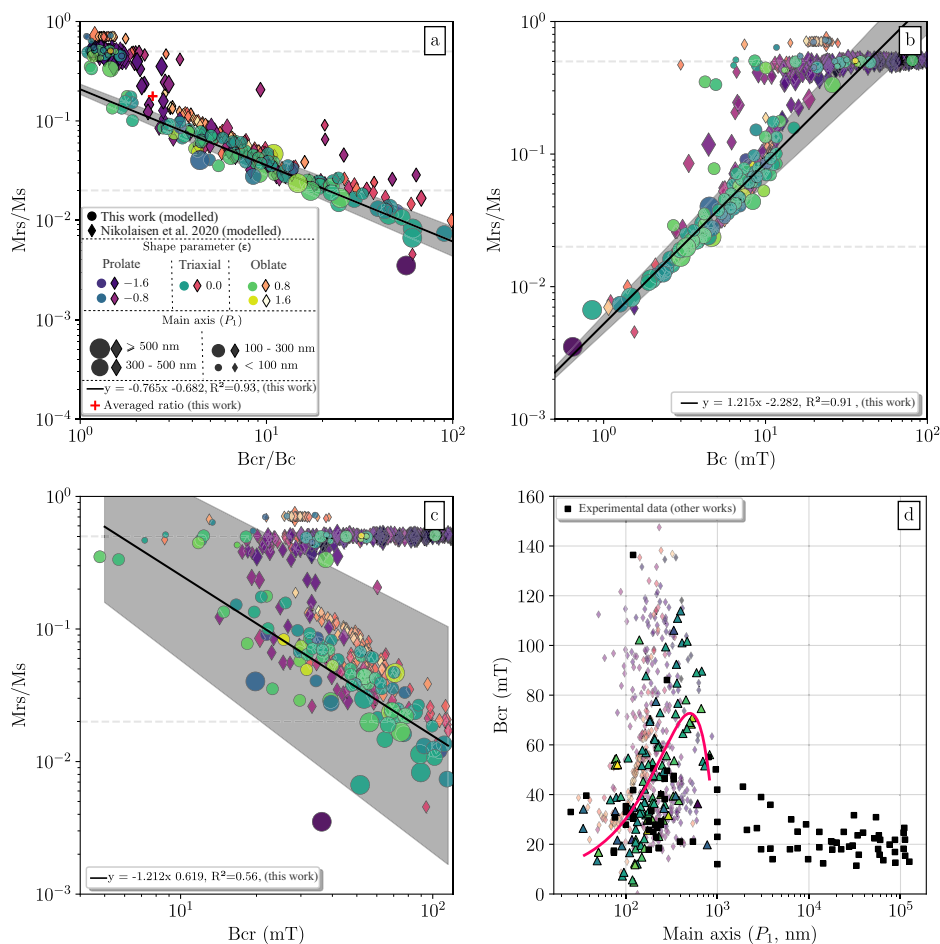eriments, different field directions result in distinct curves as a result of the grain's shape anisotropy. The particles situated at the upper side of the backfield curves (**b**, **d**) correspond to the LEM states obtained at zero field. Here, we highlight how the Mr of these states might differ from the Mrs of magnetic hysteresis (compare the Mrs values within the boxes in (**a**) and (**c**) with the respective Mr values within the grains).

is a particular problem for the determination of palaeointensities which are often performed using a stepwise cycle of heating, where the original remanence (a thermal remanence, TRM) in any temperature interval is replaced by laboratory-induced partial thermal remanence (pTRM) in a known field[68,69]. An important assumption in these experiments is that the magnetic recorders in the sample obey the so-called Law of Reciprocity, which states that a magnetic grain demagnetises (unblocks) and re-magnetises (blocks) at the same temperature i.e. ($T_{ub} = T_b$)[68,70,71], which is only valid for the original SD theory of Néel. When multiple domain states are possible in the same grain, thermal cycling may produce a pTRM with grains now occupying very different domain states with different thermal stabilities, such that $T_{ub} \neq T_b$. This issue has been discussed by Nagy et al.[14]. In their models, using a euhedral magnetite grain (100 nm, with 30% of elongation along [100]), they not only point to a multiplicity of domain

states but also to a preference for a given state as temperature changes, especially as a function of the cooling ratio. A similar effect has been identified by Tauxe[71] where "fragile" magnetic remanences behaved differently during stepwise demagnetisation and remagnetisation after samples "aged" by sitting in various storage fields over many months. This time-induced effect is equivalent to the pure thermal effect described by Nagy et al.[14], which would be caused by the multiplicity of possible domain states.

We now suggest this situation might affect a much broader range of grain sizes, and be highly dependent on grain morphology. Any failure of blocking and unblocking reciprocity, as well as the often large change in a grain's magnetisation, will make it impossible to obtain reliable paleomagnetic intensities. In exploring the multiplicity of domain states that co-exist with similar magnetic free energies for grains of irregular shape we observed this same problem. Grains whose behaviour is dominated by one

Fig. 8 | Trends in magnetic hysteresis and back-field parameters. Circles represent modelled data from this work, while diamonds represent data from Nikolaisen et al.[24]. **a** Remanence (Mrs/Ms) and coercivity (Bcr/Bc) ratios are compared in the bilogarithmic Day plot[47,48]. Our data show two distinct clusters: the first, located near Mrs/Ms ≈ 0.5, and the second, following a linear trend (line with shaded extension representing the α95). For (**a**), (**b**), and (**c**), the circles and diamonds are coloured according to their shape parameter (ϵ). The size of the circles and diamonds represents the length of the main axis of a grain, and the red cross (in a) indicates the average ratio of all modelled grains from this work. Neél's diagram[8] (**b**) and its sister plot (**c**) depict linear tendencies with confidence areas. Both plots reveal similar clusters, showing that remanence increases with coercivity (Bc) but decreases as the coercivity of remanence (Bcr) increases. In plot (**d**), Bcr values obtained in our models (triangles) are compared with their respective grain sizes, while the squares represent experimental data[48,50–60]. A third-order polynomial fit (red line) serves as a guide, revealing a trend where Bcr peaks around 600−700 nm before decreasing, consistent with experimental findings. There is also good agreement between the modelled parameters of Nikolaisen et al.[24] (diamonds) and this work.

or two states of significantly different magnetic energies over a large range of temperatures are likely to provide good paleointensity results up to a certain critical temperature where their energies become comparable. Above such temperature threshold, any of the possible domain states could be assumed as the probability is equally distributed (Fig. 5b'). The exact occupancy of the different domain states will be dependent on the thermomagnetic history of the sample. Repeated thermal cycling through such a critical temperature is expected to shift the overall distribution of domain states within the sample, deviating from the initial distribution that carried the original (geological) recording of the geomagnetic field. Thus, thermal cycling and differential heat/cool rates are likely to further exacerbate this issue[14]. It is possible that grains exhibiting the two dominant state behaviour (Fig. 5b') could in some instances be an alternative explanation to high temperature palaeomagnetic experimental failure that is often attributed to chemical alteration[72]. Grains with more complex behaviour (Fig. 5d'), characterised by a constant rebalancing of probabilities, are expected to yield unreliable thermally dependent paleomagnetic and paleointensity data, similar to the findings presented by Nagy et al.[14].

Magnetic grains whose domain states are either truly SD or ESV but far from such transition zones (mostly grains $\gtrsim$ 200 nm) are likely to be the most stable magnetic recorders, and also the ones for which palaeomagnetic information is less affected by thermal cycling. That is probably because the mechanism for magnetic state transitioning of ESV grains is the structure coherent rotation[12], which (as well as for SD grains) requires a uniform rotation of all of the magnetic moments associated with the grain. Furthermore, because domain state transitions seem to imply several complications in the magnetic properties of grains, there should be an equal dedication to studying grains within the ESV → MV transition.

Methods
Sample preparation

The sample used in our research is a Neoproterozoic cap carbonate rock, part of the Guia Formation, which spreads over the Amazon craton and the Paraguay belt (central-West Brazil). These rocks have been targets of palaeomagnetic studies and are suggested to carry pervasive evidence of authigenic growth of secondary magnetic grains as a result of low-temperature ($<T_c$) chemical processes[36,73]. Recently, Bellon et al.[35] performed a mineralogical, microscopic, and magnetic analysis on remagnetized carbonate rocks from South America. We have chosen a thin-section sample from their data set that has shown remarkable amounts of micrometric/ nanometric iron oxides to build continuous work. Preparation of the microscopic pillar was acquired by firstly coating the thin section with carbon and sequentially cutting a $\approx 18 \times 40$ µm pillar using a FIBSEM Helios 600i TFS FIB-SEM (at the Scientific Center for Optical and Electron Microscopy - ScopeM, EHT Zürich). Because the pillar sample represents only an infinitesimal part of the macroscopic thin section, the pillar was prepared in a region that had been chemically mapped for iron oxides through both SEM-EDS and synchrotron-based X-ray Fluorescence/X-ray Absorption Near Edge Spectroscopy (XRF/XANES)[35]. Lastly, the pillar was mounted on a PXCT OMNY-pin[74] using a nanomanipulator.

Synchrotron-based ptychographic X-ray computed nano-tomography (PXCT)

PXCT was performed at the cSAXS (coherent small-angle X-ray scattering) beamline of the Swiss Light Source at the Paul Scherrer Institute (PSI, Villigen, Switzerland). For the acquisition, we used the flOMNI setup[28,75], a photon energy of 6.2 keV, and we placed the sample downstream of the focal spot defined by a Fresnel zone plate (FZP). This energy was chosen due to

the major mineral constituent being calcite ($CaCO_3$), which results in nearly 50% of transmission in the middle of the sample for a pillar of 20 μm. Scans were performed in a Fermat spiral pattern[76] with a field of view of 37×10 μm, and coherent diffraction patterns were collected with an Eiger 1.5 M detector[77] positioned 5.229 m downstream of the sample. We acquired 650 projections at different incidence angles of the beam from the sample, ranging from 0 to 180°. During the data collection, we estimate that a dose of 5.6×10^8 Gy was delivered to the sample. Reconstruction of ptychographic projections were performed with the PtychoShelves package developed by the Coherent X-ray Scattering group at PSI[78], using a combination of the difference map algorithm[79], followed by the maximum likelihood algorithm[80]. This resulted in images with a pixel size of 34.8 nm. Phase images were treated with the removal of offset and linear terms and were further aligned in the vertical and horizontal directions with a subpixel precision method[81,82]. Tomographic reconstructions were finally performed by applying a filtered back projection[81,82]. Using Fourier shell correlation (FSC)[83], we estimated that the average 3D half-pitch resolution of the whole 3D dataset is 89 nm. This resolution reflects the specimen's overall average. The limited quantity of high-density magnetite particles could be imaged with better resolution due to their contrasting density with the surrounding material. This is evidenced by tracing profiles across the carbonate matrix and the iron oxide grains (Supplementary File, Fig. S2) and calculating the half-pitch resolution using the 25–75% criterion[84], resulting in resolutions between approximately 52 and 87 nm, with a mean resolution of 73.95 ± 11.77 nm. More details about the PXCT experimental setup, data collection, and reconstruction can be found in the Supplementary File (Supplementary Methods 1).

Segmentation and processing of tomographic data

Distinguishing from traditional X-ray microscopy techniques, X-ray ptychography provides images of the complex-valued transmissitivity of the specimen, where the real part is related to the absorption and the imaginary part with the phase shift of the X-rays. In combination with tomography, PXCT provides the 3D distribution of the full complex index of refraction $n(\tilde{\mathbf{r}})$[27]:

$$n(\tilde{\mathbf{r}}) = 1 - \delta(\tilde{\mathbf{r}}) - i \cdot \beta(\tilde{\mathbf{r}}), \qquad (1)$$

where $\delta(\tilde{\mathbf{r}})$ and $\beta(\tilde{\mathbf{r}})$ are obtained from the tomographic reconstruction using the phase and the absorption images, respectively. The phase shift of X-rays is related to refraction, which describes the change in the direction of the X-rays, it is strongly associated with the material density, composition, and internal structure, while absorption of X-rays is related to the local structure and composition environment of an adsorbing atom, apart from its density. In our paper, we rely on the $\delta(\tilde{\mathbf{r}})$ reconstructed tomography to recover the morphology and segment different mineral constituents of the pillar due to its higher resolution compared to the $\beta(\tilde{\mathbf{r}})$ tomogram. Nevertheless, we compare that data with $\beta(\tilde{\mathbf{r}})$ reconstruction to refine our interpretation. The quantitative $\delta(\tilde{\mathbf{r}})$ values obtained at each voxel are converted to electron density $n_e(\tilde{\mathbf{r}})$ as[85]:

$$n_e(\tilde{\mathbf{r}}) = \frac{\delta(\tilde{\mathbf{r}})k^2}{r_0 2\pi}, \qquad (2)$$

where $k = (2\pi/\lambda)$, λ is the X-ray wavelength and r_0 is the Thomson scattering length. In order to compare with our data, we can use the theoretical relation between the mass density of a given material $\rho(\tilde{\mathbf{r}})$ and its $n_e(\tilde{\mathbf{r}})$ as[86]:

$$\rho(\tilde{\mathbf{r}}) = \frac{n_e(\tilde{\mathbf{r}}) \cdot A}{N_A \cdot \phi}, \qquad (3)$$

where A is the molar mass, N_A is Avogadro's number, and ϕ is the total number of electrons in a molecule of the material.

After converting the $\delta(\tilde{\mathbf{r}})$ values to electron density (Equation (2)), we calculated the histogram distribution of all voxels in the tomogram to

segment the distinct populations composing the sample (Supplementary File, Fig. S1c). Before segmenting the data, we first deal with salt-and-pepper noise (maximum/minimum intensity voxels randomly distributed throughout the image[87]) by applying a three-dimensional Gaussian filter to the data (assuming an isotropic $\sigma = 1$, centred at each voxel). Data segmentation was acquired by processing the natural breaks in the histogram distribution and using them as thresholds after stripping away the air response. Based on the n_e distribution, five classes have been defined (Supplementary File, Fig. S1d). The n_e slices were reclassified into binary files, assigning true for the iron oxides and false for all of the other materials. Binary files were then imported to the software Dragonfly to generate stereolithographic data (STL file) of each iron oxide grain. Even aware that filtering would be able to deal with salt-and-pepper noise, we have removed particles represented by a single voxel, to give more robustness to our models.

To systematically acquire information on the morphology of the iron oxides we have applied a Principal Component Analysis (PCA) on their spatial distribution. Firstly, we export the STL files as a Cartesian coordinate cloud of points (x, y, and z) describing the external morphology of the particle. Sequentially, we use a Python script to calculate the convex hull[88] of each set of coordinates of a given particle. A convex hull is the smallest possible convex shape that encloses a given set of points, forming a polygon that connects the outermost points by ensuring that all of its internal angles are less than 180°[89]. We then performed a PCA[90], to get the eigenvectors (main directions) and eigenvalues (their magnitudes) of a covariance matrix of standardised variables. Sequentially, we have projected the original convex hull vertices onto the space defined by the principal components and calculated the size of the hull along the main directions. In this case, the maximum variance component P_1 represents the maximum elongation axis, P_2 is the intermediary one and P_3 is the minimum variance component (short axis). To more broadly evaluate the morphology of the particles in our sample, we use the shape parameter (here called ϵ) of Nikolaisen et al.[24] by using our main components achieved through the PCA analysis:

$$\epsilon = \log\left(\frac{P_1 - P_2}{P_2 - P_3}\right), \qquad (4)$$

for which triaxial morphologies (all of the main axes have different dimensions) will have $\epsilon \approx 0$, the more positive ($\epsilon \gg 0$) more oblate is the grain, and the more negative ($\epsilon \ll 0$) more prolate is the grain.

Micromagnetic modelling

In micromagnetic models, physical processes and their respective energies are evaluated mathematically through a continuous function, by assuming that at a given spatial volume the magnetisation is an average of discrete physical sources of magnetism, and that such volume is representative of the individual atomic behaviour of the averaged atoms[10,91,92]. To solve the local energy minimum (LEM) for each of the iron oxides identified in our tomography, we rely on the open-sourced software package MERRILL[10]. This software uses linear tetrahedral finite elements to describe the geometry of a particle and solve the LEM stable states minimizing the free energy of a magnetic system $E = \overrightarrow{\mathbf{H}}_{\text{eff}} \cdot \overrightarrow{\mathbf{M}}$, for which the total effective field ($\overrightarrow{\mathbf{H}}_{\text{eff}}$) is[10]:

$$\overrightarrow{\mathbf{H}}_{\text{eff}}(\overrightarrow{\mathbf{M}}) = \overrightarrow{\mathbf{H}}_{\text{exg}}(\overrightarrow{\mathbf{M}}) + \overrightarrow{\mathbf{H}}_{\text{ans}}(\overrightarrow{\mathbf{M}}) + \overrightarrow{\mathbf{H}}_{\text{Zmn}}(\overrightarrow{\mathbf{M}}) + \overrightarrow{\mathbf{H}}_{\text{dmg}}(\overrightarrow{\mathbf{M}}), \qquad (5)$$

where $\overrightarrow{\mathbf{M}}$ is the magnetization vector, $\overrightarrow{\mathbf{H}}_{\text{exg}}$ the exchange field, $\overrightarrow{\mathbf{H}}_{\text{ans}}$ the anisotropy field, $\overrightarrow{\mathbf{H}}_{\text{Zmn}}$ the Zeeman field, and $\overrightarrow{\mathbf{H}}_{\text{dmg}}$ is the demagnetizing field. We have used the software Cubit to build the tetrahedral meshes of each particle (previously exported as a STL file). To ensure that our finite element meshes were fine enough to resolve the spatial variation of the magnetisation within the geometry of each grain we determined the maximum element size as dependent on their exchange length I_e[43]. I_e of magnetite (Fe_3O_4) is ≈ 9 nm at environmental conditions of temperature and pressure, and slightly larger than that near its T_c[10]. The exchange length of maghemite (γFe_2O_3) is slightly larger than magnetite's, so it is not an issue to

assume 9 nm as a maximum element size for both mineralogies. We emphasize that the 9 nm resolution required by the micromagnetic model is solely a material-related requirement and is not related to the resolution of particle morphology. However, finer meshes could be utilized in cases where the grains are exceptionally small. Magnetic parameters of these minerals are set as in Table 1.

For any micromagnetic experiment performed through MERRILL, we can achieve a visualisation of the magnetic energy within the particles by performing simple mathematical operations to better illustrate the finite element solutions. We have achieved that through the open-sourced software Paraview[93]. Firstly, we calculate the curl of the magnetization $\vec{\mathbf{M}} = M_x\hat{i} + M_y\hat{j} + M_z\hat{k}$, which is basically its vorticity ($\vec{\omega}$), as:

$$\vec{\omega} = \nabla \times \vec{\mathbf{M}}. \tag{6}$$

Sequentially, we calculate the projection of $\vec{\omega}$ onto $\vec{\mathbf{M}}$, which is the normalized helicity ($\vec{\mathbf{H}}$) shown in our figures, as:

$$\vec{\mathbf{H}} = \frac{\vec{\mathbf{M}} \cdot \vec{\omega}}{\| \vec{\omega} \|}. \tag{7}$$

When starting from random initial orientations, LEM calculations might reach slightly different products resulting from local minima. We calculate fifty (50) different LEM models for every grain at 20 °C and then harvest the states with the lowest minimised energies to reach the most stable magnetic domains (here called r). Upon categorising the states by their energies and magnetisation intensity/direction, we can determine the probability (p_i) associated with a particular state. This probability is expressed as a function of the state's energy and the system temperature, in the presence of other states, utilising a normalised Boltzmann probability distribution:

$$p_i = \frac{\exp\left(-(\varphi_i - \lambda_j)\right)}{\sum_j^r \exp\left(-(\varphi_j - \lambda_j)\right)}. \tag{8}$$

Here, $\varphi_i = \frac{E_{Mi}}{k_B \cdot T}$, where E_{Mi} represents the magnetic energy (in J) of the state under consideration; k_B is the Boltzmann constant (1.3806×10^{-23} m$^2 \cdot$ kg $\cdot$ s$^{-2} \cdot$ K^{-1}); and the temperature of the system, denoted as T (in K). Additionally, λ_j is defined as $\min(\varphi_j)$. To ascertain the probability (p_i) under varying temperatures, we conducted LEM minimisations for selected examples. In this process, each of the r-states served as the initial solutions. The temperatures ranged from 40−579 °C, with intervals of 20 °C up to 500 °C, followed by intervals of 10 °C up to 570 °C, and finally, 1 °C increments up to 579 °C.

To assess the temporal stability of magnetic particles at environmental temperatures, we employed the Nudged-Elastic-Band method[12,45]. Initially, we sampled the minimum energy state of a given particle, and inverted the direction of magnetisation, resulting in two opposite (mirrored) domain states. This method was then utilised to determine the magnetic energy (called energy barrier) required for the transition from one domain state to the other. For that, we simply gather the energy difference between the global maximum and minimum of the pathway. Subsequently, we have used this energy to calculate the relaxation time (τ) for each grain through the Néel-Arrhenius[8] equation as follows:

$$\tau = C \cdot \exp\left(\frac{Em}{k_B \cdot T}\right), \tag{9}$$

where $C = 10^{-9}$s is a frequency factor, and T is fixed at 293.15K.

Magnetic hysteresis were evaluated from -250 mT to 250 mT in 2 mT steps, while backfield curves were evaluated from 0 to -250 mT using the same field steps, as this range covers the expected coercivity of such magnetic minerals. In our magnetic hysteresis simulations, we assess the magnetisation of a material under the influence of an applied magnetic field. The process initiates with saturation magnetisation (Ms) in a specific field direction, achieved at the maximum applied field. Subsequently, the field is gradually reduced to zero, resulting in the remanence of saturation (Mrs) at zero field. Following this, a magnetic field in the opposite direction (negative) is induced, where the field eventually causes the magnetisation to be zero (which is the coercivity, Bc), ultimately reaching the saturation point again. Backfield curves follow a similar process with a slight modification. The sample is first saturated, starting at zero field (Mrs). The field is then increased in steps, and before moving to a new step, it is decreased to zero. The remaining remanence is recorded, and as the remanence approaches zero, the coercivity of remanence (Bcr) is determined. To put it simply, magnetic hysteresis involves measuring magnetisation under the influence of a magnetic field, while backfield curves are influenced by a magnetic field, but the field is "turned off" during the actual "measurement" of the magnetisation. In our simulations of magnetic field-dependent experiments, the grain's shape can create anisotropic properties due to easy/hard magnetisation axes. To account for this, we simulate different magnetic field orientations by sampling a field-dependent magnetic property F_i from random 3D coordinates (drawn from a Fibonacci sequence) on a unit sphere as:

$$\iint_s f(x, y, z)\, ds \approx \sum_{i=1}^{20} \frac{F_i}{20}. \tag{10}$$

Here (Equation (10)), $f(x, y, z)$ evaluates the magnetic property F_i, and the integral over the surface s is approximated by the sum over all samples. Because increasing the number of samples improves the approximation, we have run field-dependent experiments in twenty ($n = 20$) random directions for every grain.

Data availability
Besides the Supplementary File, all of the data related to this research is preserved at Zenodo[44] and can be publicly accessed from the same repository. The data is subdivided into folders, including the meshes used in our simulations (.pat files) and the MERRILL scripts, together with any other relevant file. We are also providing the averaged hysteresis and backfield curves of each grain.

Code availability
The results reported here were achieved through MERRILL[10], an open-sourced code for micromagnetic modelling of tetrahedral finite element meshes. Installation, guide tutorials and courses are available at https://blogs.ed.ac.uk/rockmag/.

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Author contributions

U.D.B. performed sample preparation, data collection, processing, and analysis of tomography data, and conducted and interpreted the numerical models. W.W. contributed to running numerical models and supervising the project. R.I.F.T. conceived and supervised the overall project. A.D. was involved in collecting and processing tomography data. D.G. provided project supervision. All authors have actively contributed to the preparation and review of this manuscript.

Competing interests

The authors declare no competing interests.

Additional information

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