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Can a simple topological-constraints-based model predict the initial dissolution rate of borosilicate and aluminosilicate glasses?

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Tuning glass composition to obtain targeted properties generally relies on empirical approaches. However, a deep understanding of the physical and chemical mechanisms linking glass composition to its structure and properties would enable developing reliable predictive models. Indeed, although empirical models are usually able to interpolate composition–property relationships within a given compositional envelope, they often fail at extrapolating predictions far from their training domain. Here, as an alternative route to empirical models, we show that a structural descriptor based on the number of topological constraints per atom can be used to predict the initial dissolution rate of aluminosilicate and borosilicate glasses after being parameterized on different families of glasses (specific series of borosilicate glasses). Sixteen glasses belonging to these families were studied and their initial dissolution rates were determined at 90 °C and $\text{pH}^{90^\circ\text{C}} = 9$, covering rates spanning over 5 orders of magnitude. The model based on topological constraints was trained based on seven select borosilicate glasses ($R^2 = 0.997$) and used to predict the dissolution rate of nine additional borosilicate and aluminosilicate glasses. We show that, provided that corrections are made for high alkali content glasses that dissolve incongruently (preferential release of Na), the model gives reasonable predictions, even far from its training domain.

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INTRODUCTION

Borosilicate and aluminosilicate glasses are widely used in our daily life as well as in industry^{1,2}. Tuning their properties for a targeted application, i.e., glass design, requires a deep understanding of the relationships between their composition, structure, and properties³. For instance, in the nuclear industry, borosilicate glasses are designed to immobilize radioactive wastes^{4–6}. Optimizing their chemical durability is of primary importance to ensure the safety of the waste disposal. In the glassware and pharmaceutical industries, both borosilicate and aluminosilicate glasses are designed to contain liquid that must not be contaminated by glass components^{7,8}. In nature, aluminosilicate glasses are massively produced by volcanoes and oceanic ridges⁹. Their dissolution controls the budget of some key elements in the oceans¹⁰.

Glass alteration is a complex phenomenon involving surface reaction with water, transport of species toward both the glass surface and the bulk solution, condensation and precipitation reactions¹¹. None of the models developed to date can predict the dissolution rate of a multicomponent glass just on the basis of its chemical composition. Two main reasons account for that: (i) for a given cation M of the glass, the energy barrier for the hydrolysis of a M–O bond depends on the state of protonation of the bridging O along with the M–O bond distance, the O–M–O bond angle, and local structural environment^{12,13}. The bond distances and bond angles are generally in wide distribution in a glass. (ii) The medium range order can impact the transport and the reactivity of water molecules. The large number of variables make it almost

impossible for a direct prediction from first principles data such as reaction energy barriers alone, at least to date.

To address such difficulties, topological constraint theory (TCT) provides a simplified framework to predict the properties of glasses based on the topology of their atomic network^{14–16}. Recently, this approach has been used to predict the dissolution rate of silicate minerals and glasses under varying pH conditions^{17–22}.

In this study we investigated the capability of a structural descriptor relying on the number of topological constraints per atom to predict the initial dissolution rate of borosilicate and aluminosilicate glasses. We selected a series of borosilicate glasses with the same Si/B, Si/Na ratios as the international simple glass (ISG), as well as additional glasses that are less and more polymerized, including B-free glasses (see the Methods section for more details). Among the tested glasses, three compositions are above the percolation threshold, that is, Na network modifiers can leach out prior to matrix dissolution, thereby leading to the formation of a Na-depleted hydrated silica layer that undergoes hydrolysis²³. Experimentally, the initial dissolution rates were measured at 90 °C and pH 9 to ensure that the dissolution process is rate-controlled by the hydrolysis of the silicate network. Therefore, rates were measured from Si release into the solution. The structural descriptor used herein is the number of constraints per atoms, n_c , which is derived from topological constraint theory^{14,16,24}. The calculation of n_c relies on simple rules derived from previous studies^{25–28}. Following a machine learning approach²⁹, the model was trained with seven borosilicate glasses belonging to a restricted domain (training set), while its

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predictions were tested on nine other glasses with compositions and dissolution rates that are far from the training range (test set). It is shown that the model provides reasonable predictions, except for glasses that dissolve incongruently.

RESULTS AND DISCUSSION

Experimental results

Table 1 displays the composition and some characteristics of the studied glasses. All the glasses are found to be homogeneous. Three high alkali content glasses, NSAC19, NSAC21, and NSAC35 have a ratio $\Sigma\text{Alcalis}/\Sigma\text{Cations}$ of 0.34, 0.38, and 0.49, respectively. These values are greater than the percolation threshold (0.31), as shown by Devreux and Kolb²³. All the other glasses are below this threshold.

Experimental results of the leach tests are displayed on Fig. 1; Table 2. For all the tested glasses, a linear release of Si is observed, which signals that the matrix dissolution proceeded at a constant rate. As shown in Table 2, the pH did not significantly evolve during the tests—except for the glasses whose dissolution is the most incongruent (NBS36/21 and NSAC35). For these glasses, an increase in pH up to 9.5 caused by ion-exchange was noted—despite the addition of nitric acid during the test. The fraction of altered glass, *FAG*, given at the end of the tests in Table 2 remained low, yielding to very small surface correction. For all glasses, the *y*-intercepts are close to zero (except NBS36/21), which suggests that the glasses dissolved at the same rate since the beginning of the reaction. The case of NBS36/21 is peculiar because of its high dissolution rate. The fact that the *y*-intercept is not close to zero is due to the uncertainty on the slope.

For 11 glasses (NBSA, NBSAC, NBSACZ, NBSAZ, NBSC, NBSCZ, NSACO, NSAC17, NSAC19, NSAC21, and NSAC35), the dissolution solutions were also analyzed by ICP-OES. Results are presented in SI 1. Overall, analyses of the first eight of these glasses show that the dissolution of the borosilicate glasses is congruent (i.e., all glass components are dissolved at the same rate—except Zr for Zr-bearing glasses, which was not detected in solution) and the rate values derived from these analyses are in fair agreement with those determined from UV-Visible spectrophotometry analyses. Conversely, the three high Na aluminosilicate glasses whose compositions are above the Na percolation threshold²³—NSAC19, NSAC21, and NSAC35—dissolved incongruently. For those compositions, a slight (NSAC19), significant (NSAC21), and large (NSAC35) preferential release of Na was noticed. This phenomenon leads to the formation of a Na-depleted Al-and-Si-rich layer on the surface of the glass. When calculating the glass dissolution rate according to Si release, one actually determines the dissolution rate of this hydrated and potentially reorganized silicate alternated layer. This will be further discussed below.

Altogether, the high degree of dilution of the leaching solution, the linearity of the Si release, the low *y*-intercept, and the congruency of the dissolution for most of the tested materials ensure that glass dissolved at the highest dissolution rate in the tested conditions, it is acceptable to derive the initial dissolution rate r_0 from a linear regression of NL(Si) vs. time. Results of this calculation are given in Table 2.

The following observations can be made:

- Depending on glass composition, r_0 varies over more than 5 orders of magnitude, which, to the best of our knowledge, represents the largest span of glass dissolution rates ever tested.

Table 1. Analyzed compositions and glass properties. N, B, S, A, C, and Z refer to Na, B, Si, Al, Ca, and Zr, respectively. Glasses labeled with (*) were used to train the model, the others to test the model. Glasses labeled with (p) are percolating, as their alkali content is higher than 0.3 (see Devreux and Kolb²³). When applicable, the first number indicates the molar percentage of Na and the second the molar percentage of B₂O₃.

Name	Other name in the literature	Composition (mol%)							Melting T (°C)	T_g (°C)	Density (g cm ⁻³)	B4
		SiO ₂	B ₂ O ₃	Na ₂ O	Al ₂ O ₃	CaO	ZrO ₂	Li ₂ O				
<i>Borosilicate glasses</i>												
NBS14/18 ^(*)	CJ1 ^a	67.8	18.0	14.2					1500	570	2.451	66
NBSA ^(*)	CJ2 ^a	64.9	17.3	13.7	4.1				1450	510	2.405	48
NBSAC ^(*)	CJ3 ^a	61.2	16.3	12.8	3.9	5.8			1400	510	2.471	53
NBSACZ ^(*)	CJ4 ^a , ISG ^b	60.1	16.0	12.7	3.8	5.7	1.7		1400	510	2.500	48
NBSAZ ^(*)	CJ7 ^a	63.8	17.0	13.4	4.0		1.8		1400	510	2.505	41
NBSC ^(*)	CJ8	63.6	17.0	13.4		6.0			1400	510	2.505	66
NBSCZ ^(*)	CJ9 ^a	62.5	16.7	13.1		5.9	1.8		1350	550	2.547	63
NBS12/28	NBS17-24 ^c	60.5	27.7	11.6					1250	540	2.462	43
NBS36/21	NBS35-19 ^c	43.2	20.7	36.2					1100	470	2.537	63
NBS31/15	NBS29-13 ^c	54.2	15.0	30.9					1250	505	2.538	78
<i>Aluminosilicate glasses</i>												
NSAC19 ^(p)		55.3		19.0	9.9	13.9		1.9	1450	610	2.591	
NSAC17		48.6		17.0	20.1	12.3		1.9	1500	580	2.569	
NSAC21 ^(p)		57.4		21.3	5.9	15.4			1350	580	2.592	
NSAC0		57.3			5.9	36.8			1500	580	2.790	
NSAC35 ^(p)		58.1		34.9	6.9				1350	580	2.522	
NSA	Albite glass ^d	75.0		12.5	12.5				1650	530	2.340	

Note that the glasses NBS12/28, NBS36/21, and NBS31/15 are close but not exactly the same as those studied by Pacaud et al.³⁷. B4 represents the fraction of four fold coordinated B in the glass, determined by MAS NMR spectroscopy. Annealing was conducted at *T_g* + 20 °C.

^aGin et al.³².

^bGin et al.⁴.

^cPacaud et al.³⁷.

^dPerez et al.³⁸.

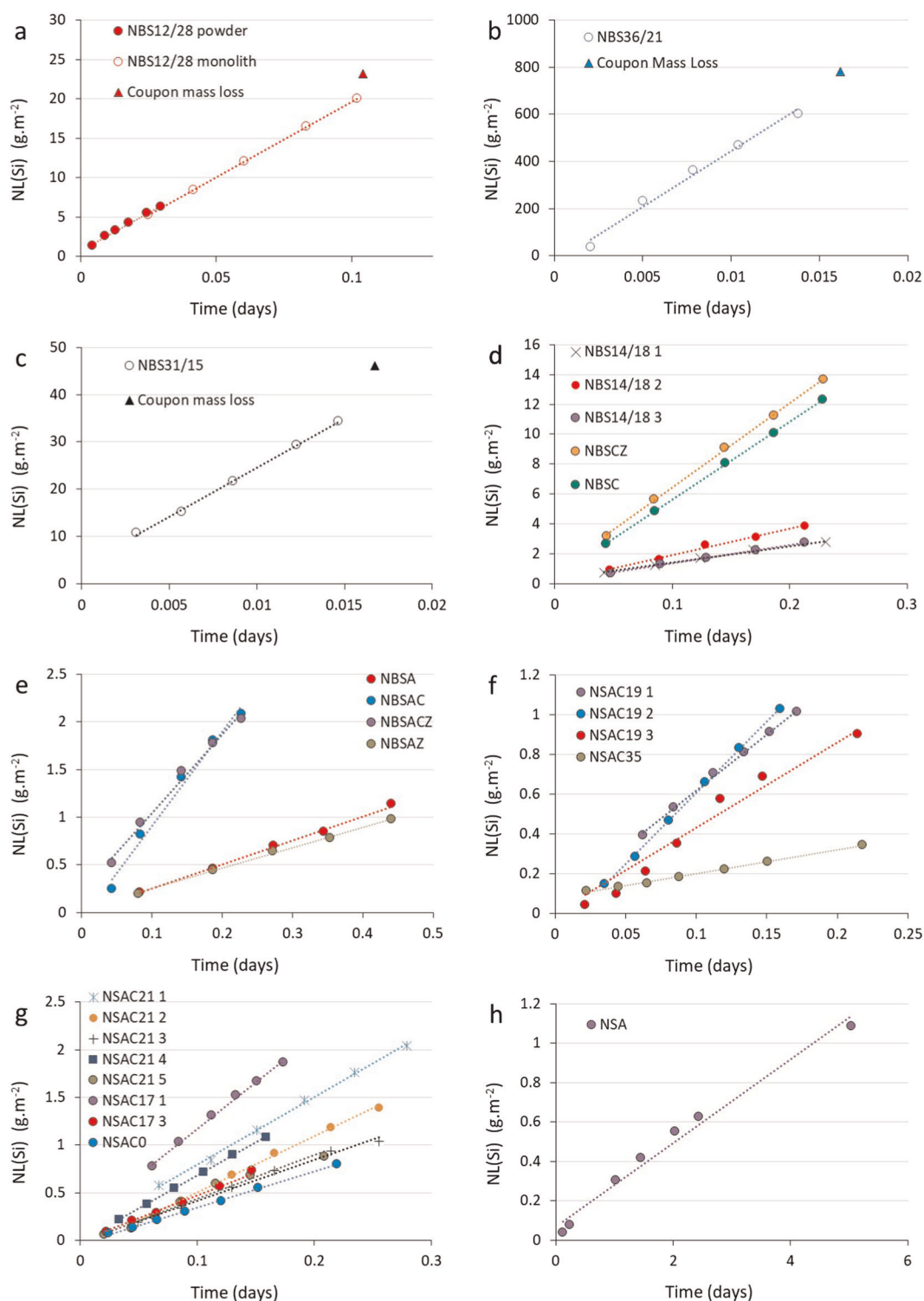


Fig. 1 Results from leaching tests. Time dependence of normalized mass loss based on Si release for **a** NBS12/28, **b** NBS36/21, **c** NBS31/15, **d** NBS14/18, NBS CZ, NBS C, **e** NBSA, NBSAC, NBSACZ, NBSAZ, **f** NSAC19, NSAC35, **g** NSAC21, NSAC17, NSAC0, **h** NSA. Solid symbols refer to tests conducted with powder, whereas empty symbols are used for monoliths. **a–c** Mass loss of the coupon at the end of the experiment (triangle) and normalized mass losses of Si.

- For NBS12/28, a comparison between powder and monolith was made to evaluate the hypothesis relative to the reactive surface area (Fig. 1a). That surface evaluation for the monolith was indeed based on simple but accurate geometric considerations (length, width and thickness were measured with a caliper), but that of the powder remained uncertain because of the complex,

non-spherical shape of glass particles. It is found that, r_0 of the monolith and r_0 of the powder whose reactive surface area is a geometric one are similar within uncertainties. Hence, this result validated the choice of the geometric surface area (instead of that determined by gas adsorption) for the glass powders used in the dissolution testing, as suggested by previous studies^{30,31}.

Table 2. Results of the initial dissolution rate measurements (r_0) obtained by linear regression. Fraction of altered glass (FAG) and pH are given at the end of the test. Uncertainty on the pH is 0.1 unit. Congruency between Na and Si is calculated at the end of the test. n.d. not determined.

Glass	Test #	FAG	Congruency (Na/Si)	Final pH ^{90 °C}	Parameter considered for r_0 calculation	r_0 (g m ⁻² d ⁻¹)	Ln(r_0)	y-intercept (g m ⁻²)	R ²
NBS12/28	1	<0.01	1.1 ± 0.1	8.9	Si	192 ± 60	5.3	0.4	1.000
	1				Mass loss	223 ± 45	5.4		
	2	0.26		9.0	Si	202 ± 60	5.3	0.6	0.995
NBS36/21	1	0.24	1.2 ± 0.1	9.5	Si	47,370 ± 14,360	10.8	−31.2	0.986
					Mass loss	49,048 ± 9809	10.8		
NBS31/15	1	0.02	1.1 ± 0.1	9.1	Si	2070 ± 620	7.6	3.8	0.999
		Mass loss			2756 ± 551	7.9			
NBS14/18	1	0.06	n.d.	9.0	Si	12.0 ± 3.6	2.5	0.2	0.999
	2	0.08		Si	17.7 ± 5.3	2.9	0.1	0.989	
	3	0.07		Si	12.2 ± 3.7	2.5	0.1	0.999	
NBSA	1	0.03	1.1 ± 0.1	8.9	Si	2.6 ± 0.8	0.9	−0.02	0.997
NBSAC	1	0.04	1.0 ± 0.1	8.9	Si	9.9 ± 3.0	2.3	−0.08	0.986
NBSACZ	1	0.09	1.1 ± 0.1	9.0	Si	8.2 ± 2.5	2.1	0.2	0.990
NBSAZ	1	0.02	1.0 ± 0.1	8.9	Si	2.2 ± 0.6	0.8	0.04	0.997
NBSC	1	0.24	1.0 ± 0.1	8.9	Si	52.2 ± 15.7	4.0	0.4	1.000
NBSCZ	1	0.26	1.1 ± 0.1	8.9	Si	56.4 ± 17.0	4.0	0.8	0.999
NSAC19	1	0.08	1.2 ± 0.1	8.8	Si	5.6 ± 1.7	1.7	0.05	0.998
	2	0.02		9.0	Si	7.2 ± 2.2	2.0	−0.1	0.999
	3	0.02		9.1	Si	5.5 ± 1.7	1.7	−0.12	0.984
NSAC17	1	0.14	1.0 ± 0.1	8.8	Si	9.8 ± 2.9	2.3	0.2	0.997
	3	0.02		9.0	Si	5.0 ± 1.5	1.6	−0.03	0.996
NSAC21	1	0.16	1.4 ± 0.1	8.8	Si	7.4 ± 2.2	2.0	0.1	0.998
	2	0.11		9.0	Si	6.1 ± 2.2	1.8	−0.1	0.998
	3	0.03		9.0	Si	4.5 ± 1.4	1.5	0.0	0.992
	4	0.02		9.0	Si	7.2 ± 1.4	2.0	−0.01	1.000
	5	0.02		9.1	Si	4.6 ± 1.4	1.5	−0.03	0.974
NSAC0	3	0.02		9.1	Si	3.8 ± 1.3	1.3	−0.03	0.999
NSAC35	1	0.01	145 ± 10	9.4	Si	1.2 ± 0.4	0.15	0.08	0.997
NSA	1	0.03	n.d.	8.9	Si	0.26 ± 0.05	−1.3	0.02	0.995

One plausible explanation of this result is that the specific surface area measured by Brunauer, Emmet, and Teller (BET) method which usually gives a surface typically 2–3-fold greater than the geometric surface) takes into account the nanoscale roughness, which vanishes during dissolution.

- The values of r_0 determined from the mass loss of the coupons NBS12/28, NBS36/21, and NBS31/15 at the end of the experiments are in good agreement with the solution data (Fig. 2a–c). This gives credit to the rate determination.
- Reproducibility of r_0 measurement was studied for NBS14/18, NSAC17, NSAC19, and NSAC21 for which tests were performed 3, 2, 3, and 5 times, respectively. Slight, non-impactful variations of the protocols were applied, such as the change in the glass powder size fraction or the change of the operator (tests on NSAC21 were performed by three different operators). For the four tested glasses, the obtained values fall within uncertainties. Although the number of tests is not sufficient to perform a robust statistical analysis, nonetheless these sets of experiments confirm that the uncertainty of 30% on r_0 taken in this study is reasonable.
- The r_0 value obtained for NBS14/18, NBSA, NBSAC, NBSACZ, NBSAZ, NBSC, and NBSZ are 2–6 times higher than that reported by Gin et al.³² in similar conditions. The main reason is that the release rates in the earlier report³² were normalized to the BET surface area of the glass powder. This can explain a factor 2–4.

However, a factor 5.5 and 6.6 are calculated for NBSC and NBSZ, respectively. As these two glasses have the fastest dissolution rates of this set of glasses, it is possible that their rates were underestimated in the previous study due to an insufficient agitation of the solution. Indeed, it has been observed that agitation is a key parameter when measurements are conducted in static (no leachant renewal) conditions.

- As noted above, glasses NSAC19, NSAC21, and NSAC35, whose composition are above the Na percolation threshold²³, dissolved incongruently, with part of Na being released much faster than Si. According to their bulk composition (high Na content as modifier), NSAC35 should dissolve faster than NSAC0, NSAC17, NSAC19, and NSAC21, but, among these glasses, it seems to be the more durable. The most likely explanation is that, r_0 , which is determined from Si release, corresponds to the dissolution rate of the Na-depleted hydrated layer (in agreement with the large deviation to congruency).

Enumeration of the topological constraints

We calculated the number of constraints per atom n_c for all the glasses considered herein by enumerating the number of bond-stretching (BS) and bond-bending (BB) constraints created by each element. Table 3 shows the number of BS and BB constraints created by each type of atomic species. Most of these values are

derived from the coordination state of each atom. In details, Si and Al atoms are associated with four BS (i.e., with the four surrounding O atoms) and five BB constraints (i.e., the number of independent angles that need to be fixed to define the tetrahedral angular environment). Similarly, 3-fold coordinated B atoms (B^{III}) are associated with three BS and three BB constraints,

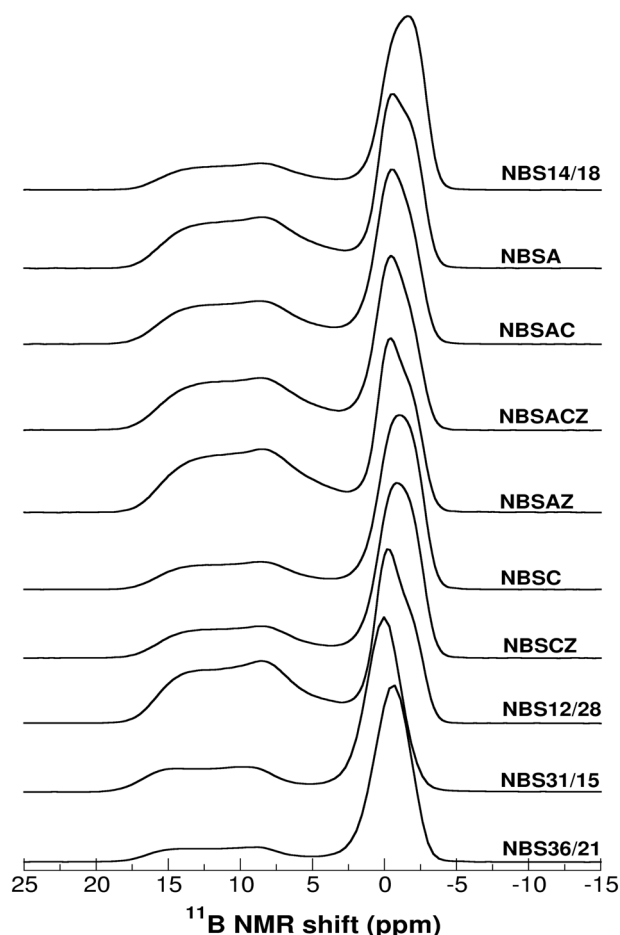


Fig. 2 ^{11}B MAS NMR spectra of all borosilicate glasses investigated in this study. Spectra are normalized to the B4 peak (centered around 0 ppm).

Table 3. Number of bond-stretching (BS) and bond-bending (BB) constraints created by each atomic species present within the glass network. Note that, although each BS constraint is necessarily associated with a bond between a cation and an O atom, the BS constraints are for convenience here fully associated with the cations.		
Atomic species	BS	BB
Si	4	5
B^{III}	3	3
B^{IV}	4	0
Al	4	5
Zr	6	0
Na	1	0
Li	1	0
Ca	2	0
BO	–	1
NBO	–	0

whereas 4-fold coordinated B atoms (B^{IV}) are associated with four BS constraints. However, in contrast to the case of the B^{III} atoms, no angular BB constraint is counted for B^{IV} atoms. This can be understood from the fact that 4-fold coordinated B species need to be charge-compensated (e.g., by Na or Ca cations), which, in turn, destabilizes their angular constraints. Similarly, only radial BS constraints are attributed to Zr atoms since their angular environment is not as well defined as that of Si and Al atoms—which suggests the absence of any underlying BB constraint. Based on previous studies, the number of BS constraints associated with the network-modifying species (e.g., Na, Li, and Ca) are taken as their valency (i.e., 1 for Na and Li and 2 for Ca) rather than their geometric coordination numbers^{25,27,28}. No BB constraints are counted for network-modifying species due to the ionic, non-directional nature of the bonds they form^{25,26}. In addition, bridging oxygen atoms are associated with one BB constraint. In contrast, due to the ionic and non-directional nature of the bonds created by the network-modifying species, no BB is counted for the non-bridging oxygen atoms^{25,26}. Table 4 shows the average number of constraints per atom n_c of all the glasses considered herein. Overall, we find that most glasses are isostatic ($n_c \approx 3$) or slightly flexible ($n_c < 3$), in agreement with the fact that stressed-rigid systems ($n_c > 3$) typically show a poor glass-forming ability¹⁵.

Parameterization of the TCT model

We first investigate whether the forward dissolution rate (r_0) of the silicate glasses considered herein can be predicted from the knowledge of the number of constraints per atom (n_c). To this end, we first focus only on seven borosilicate glasses, also called CJ series (see Tables 1, 4). This choice is motivated by the fact that, ultimately, we aim to assess whether our TCT-based model can extrapolate predictions of dissolution rates for new unknown glasses that are not included within the training set (see below).

Table 4. Number of BS and BB per atom, and total number of constraints per atom (n_c) in the glasses considered herein. The glasses indicated by a star are used to train the TCT model (i.e., obtain the two fitting parameters in Eq. 6), while the other glasses are used to test the predictions of the model. Glasses labeled with * were used to train the model, the others to test the model.			
Glass	BS	BB	n_c
<i>Glasses used to train the model (training set)</i>			
NBS14/18*	1.28	1.71	2.99
NBSA*	1.28	1.82	3.11
NBSAC*	1.28	1.73	3.01
NBSACZ*	1.29	1.74	3.03
NBSAZ*	1.29	1.83	3.11
NBSC*	1.27	1.63	2.90
NBSCZ*	1.28	1.62	2.91
<i>Glasses used to test the model (test set)</i>			
NBS12/28	1.28	1.73	3.01
NBS36/21	1.16	1.17	2.32
NBS31/15	1.19	1.32	2.51
NSAC19	1.21	1.63	2.85
NSAC17	1.27	1.86	3.14
NSAC21	1.18	1.53	2.71
NSAC0	1.27	1.65	2.92
NSAC35	1.14	1.52	2.66
NSA	1.31	2.15	3.46

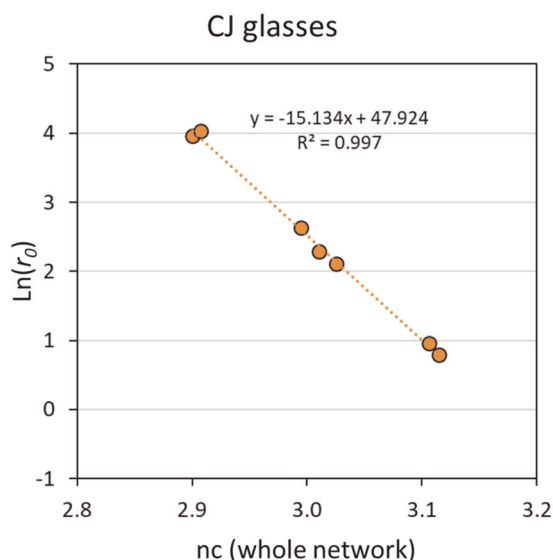


Fig. 3 Forward dissolution rate as a function of the number of constraints per atom (n_c) for the 7 borosilicate glasses selected to train the model (training set, CJ series, see Table 1). The data are fitted by Eq. 1. The standard deviation on the slope is 0.356.

Figure 3 shows the forward dissolution rate r_0 of the CJ glasses as a function of the number of constraints per atom n_c . Overall, we observe a very good correlation between r_0 and n_c , namely, r_0 decreases exponentially with n_c . This echoes previous findings¹⁷, wherein it was proposed that the dissolution rate in dilute conditions is controlled by the topology of the atomic network as:

$$r_0 = r_{n_c=0} \exp\left(-\frac{n_c E_0}{RT}\right), \quad (1)$$

where $r_{n_c=0}$ is a constant that corresponds to the barrier-less dissolution rate of a completely depolymerized material (for which $n_c = 0$) and that depends on the solution chemistry (e.g., pH) and E_0 is the energy barrier that needs to be overcome to break a unit atomic constraint. Here, we find $E_0 = 45.7 \pm 1.1$ kJ/mol, which is fairly comparable (albeit larger) to the values previously-obtained for silicate glasses (25.5¹⁷, 24.7^{21,22}, 23.9¹⁸, and 23 ± 5 kJ/mol³³) but differs from that obtained for aluminoborate glasses (6.9 kJ/mol²⁰).

This relationship between dissolution rate and number of constraints per atom was explained as follows (see ref. 17). Starting from $n_c = 0$ (i.e., which would correspond to a fully depolymerized material), each new constraint per atom effectively reduces the dissolution kinetics by increasing the associated activation energy needed for bond rupture¹⁷. In details, it was proposed that n_c serves as an indicator of the elastic resistance of the atomic network, which tends to resist the reorganization or deformation of the network that would occur upon dissolution¹⁷. For instance, hydrolysis requires the formation of larger intermediate over-coordinated species (5-fold coordinated Si or three-fold coordinated O), which imposes some local stress (and strain) on the network¹¹. The resulting activation energy takes the form of the strain elastic energy that is applied by the rest of the network to resist the creation of this local defect³⁴. The topological model captured by Eq. 1 then assumes that this strain elastic energy is governed by the local number of constraints per atom n_c , since each constraint acts as a little spring connecting the atoms and, hence, characterizes the local stiffness of the atomic network³⁵. This picture echoes previous results from density functional theory, wherein the activation energy associated with the hydrolysis of bridging oxygen atoms was shown to increase with the network connectivity³⁶.

Predictions of the TCT on new unknown glasses

We now assess whether the TCT-based model trained based on the seven borosilicate glasses can predict the dissolution rate of the other non-CJ borosilicate and, also, aluminosilicate glasses tested herein (i.e., the test set). This aims to check whether, in addition of properly interpolating the dissolution rate of the “training” glasses, our model can extrapolate predictions far from its training set for unknown glasses that were not used during its training. It should be noted that the CJ series corresponds to a small training set for the model, both in terms of samples number (7 out of 16 glasses) and dissolution kinetics—since the dissolution rate of the CJ glasses ranges over about 1.5 order of magnitude, while that of the entire set of glasses spans over 5.5 orders of magnitude.

Figure 4a shows the comparison between the measured and predicted dissolution rates of the non-CJ glasses used herein as test set. Overall, we find that, despite being trained based on only a narrow range of dissolution rates (see orange domain in Fig. 4), our TCT-based model offers reasonable predictions of the dissolution rates of the non-CJ borosilicate glasses (NBS series, open circles). In contrast, we observe that the level of agreement between the measured and predicted dissolution rates of the aluminosilicate glasses (NSA series, filled circle) is significantly lower than in the case of the borosilicate glasses (see Fig. 4a). As noted above, some of these glasses exhibit an incongruent dissolution, with a preferential release of Na cations. As discussed in the following, such incongruity needs to be accounted for in the TCT model to reconcile the measured and predicted dissolution rate data. The root mean square relative error (RMSRE) was calculated for the 9 tested glasses according to Eq. 2:

$$\text{RMSRE} = \frac{1}{N} \sqrt{\sum_{i=1}^N \left(\frac{r_{\text{cal}} - r_{\text{exp}}}{r_{\text{exp}}} \right)^2}, \quad (2)$$

where N is the number of glasses, r_{cal} the calculated rate and r_{exp} the measured rate. In this case RMSRE is 4.63.

Refined TCT model accounting for dissolution incongruity

As noted above, the NSAC19, NSAC21, and NSAC35 glasses that are not well described by our TCT model exhibit some preferential release of Na cations upon dissolution, which leads to the formation of a Na-depleted (and, hence, Al- and Si-enriched) layer on the surface of the glass. Based on this observation, we now assess whether the dissolution rates of these glasses is controlled by the network topology of their Na-depleted layer rather than that of their initial pre-dissolution bulk structure. To this end, we estimated the composition of the surface layer based on the equivalent thicknesses of the Si, Al, and Na species (see Table 5).

Table 5 shows the corrected number of constraints per atom for the NSAC19, NSAC21, and NSAC35 glasses, recalculated based on their modified compositions. As expected, we find that the corrected n_c values are higher than those obtained from the bulk compositions, which echoes the fact that the preferential leaching of the Na atoms induces a repolymerization (and, hence, rigidification) of the network of the surface layer. Interestingly, we find that, by accounting for these corrected n_c values, our TCT-based model offers significantly improved predictions of the dissolution rates of the NSAC19 NSAC21. Nevertheless, we still observe a large discrepancy between the predicted and measured dissolution rates for the NSAC35 glass. The fact that the predicted rate is much lower than the measured one suggests that the repolymerization of the silicate network following the release of Na is incomplete. For the percolating glasses, further investigation is required to better understand the chemical and structural modifications of the reacting surface.

By using the corrected n_c values, we find that the RMSRE of the TCT-base predictive model decreased from 4.63 to 2.45. Further, if

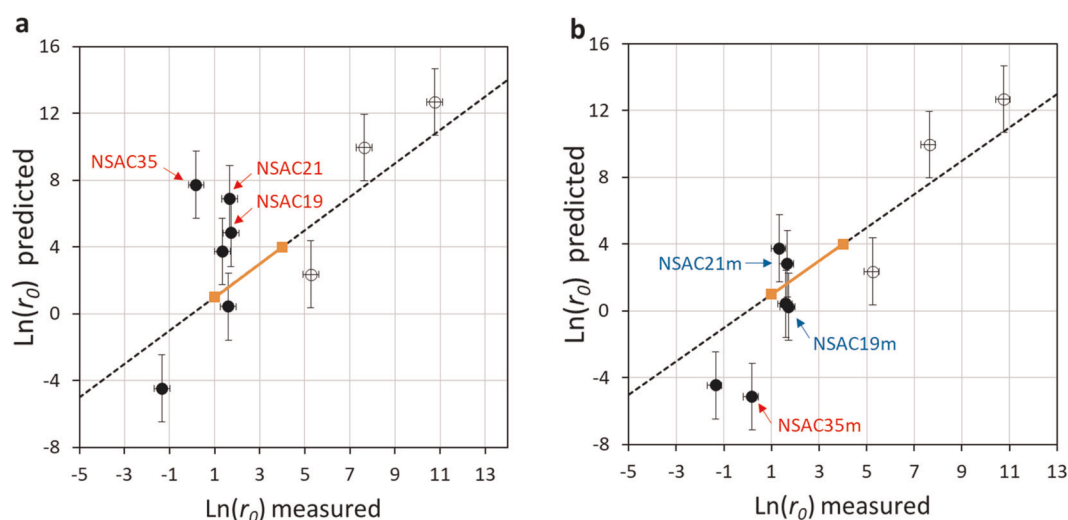


Fig. 4 Comparison between the measured initial dissolution rates and those predicted by our TCT-based model (Eq. 1) parameterized based on the CJ series of glasses (whose range of dissolution rate is indicated in orange). Open circles and filled correspond to borosilicate glasses and aluminosilicate glasses, respectively. The black dashed line is the $y=x$ identity function, indicative of a perfect agreement between measured and predicted data. The two panels present the predictions from our model by using as input **a** the bulk glass compositions and **b** the modified compositions of the Na-depleted glasses for the NSAC19, NSAC21, and NSAC35 glasses (percolating glasses) given in Table 5. The red labels highlight the glasses for which the dissolution rate is not properly predicted by the TCT-based model. Error bars are calculated as follow: $\pm 30\%$ on measured r_0 (-0.36 and $+0.26$ on $\ln(r_0)$ values), ± 2 on calculated $\ln(r_0)$ values to account for errors on glass composition.

Table 5. Corrected compositions, number of BS and BB per atom, and total number of constraints per atom (n_c) of the Na-depleted layers forming on the surface of the NSAC19, NSAC21, and NSAC35 glasses. As a network modifier, Li is here assumed to follow the same behavior as Na.

Name	Corrected composition					BS	BB	n_c
	SiO ₂	Na ₂ O	Al ₂ O ₃	CaO	Li ₂ O			
NSAC19m	62.1	11.1	11.1	15.6	0.0	1.28	1.88	3.15
NSAC21m	67.8	7.0	7.0	18.2		1.28	1.87	3.15
NSAC35m	80.8	9.6	9.6			1.31	2.19	3.51

the NSAC35 glass is excluded from the prediction, the *RMSRE* decreased from 0.57 (with the bulk composition of NSAC19 and NSAC21 glasses) to 0.37 with the Na-depleted composition of these two glasses. This last number means that the model can predict the initial dissolution rate of a new borosilicate or aluminosilicate glass dissolving congruently with a relative error of $e^{0.37}$, i.e., 45%. This error is close to the experimental error (30%).

In summary, the TCT-based model developed gives reasonable predictions of the initial dissolution rate of borosilicate and aluminosilicate glasses, given the conditions that the unknown glasses are homogeneous and dissolve congruently, or slightly incongruently (composition close to the percolation threshold). For glasses that do not meet these restrictions, we proposed a simple way to estimate their dissolution rate, but further investigations are needed to refine the model, especially for flexible networks ($n_c < 3$).

METHODS

Glasses

Ten sodium borosilicate glasses and six aluminosilicate glasses were selected for this study. The first three glasses displayed in Table 5 have been subject to previous investigations by Gin et al.³², Pacaud et al.³⁷, and Perez et al.³⁸. Note that NBSACZ corresponds to the International Simple Glass (ISG)⁴, which has been subject to many studies since 2013³⁹. Details

about the elaboration conditions can be found in the above-mentioned references. All these glasses of this study were prepared following the classical melt-quench route. Analytical grade carbonate or oxide powders were melted at the temperature indicated in Table 5. To guarantee a good homogeneity, after quenching, the resulting glass was crushed and melted a second time at the same temperature. After the second batch, the glass was annealed for 3 h at $T_g + 20$ K. The fractions of 4-fold coordinated boron (B4) of the borosilicate glasses obtained from ¹¹B magic angle spinning (MAS) nuclear magnetic resonance (NMR) as detailed elsewhere^{40,41}. The glass composition were analyzed by inductively coupled plasma-optical emission spectroscopy (ICP-OES) after caustic fusion (NaOH-KNO₃ and lithium tetraborate) of glass powders.

Glass powders were prepared following the classical method of grinding, sieving, and ultrasonically cleaning in acetone and ethanol. The absence of fine particles was verified by scanning electron microscopy (SEM). Rectangular shape coupons of NBS12/28, NBS36/21, and NBS31/15—the less durable glasses of the series—were also prepared by cutting and polishing at various grades up to a diamond suspension of 0.05 μ m, in order to obtain a surface roughness of the order of a few nm. No water was used during the preparation of the powders and monoliths of the studied glasses.

The ¹¹B MAS NMR spectra of the borosilicate glasses were collected on a Bruker AVANCE II 500WB spectrometer operating at a Larmor frequency of 160.14 MHz (magnetic field 11.72 T) using a 4 mm (outer diameter of the ZrO₂ rotor) Bruker (boron-free) CPMAS probe. The powder samples were spun at a frequency of 12.5 kHz. A recycle delay of 2 s and a pulse length of 1 μ s (tip angle of about 20°) were used to ensure quantitiveness of the spectra (i.e., homogeneous excitation of BO₃ and BO₄ species, independently of their quadrupolar interactions). Data processing occurred via an in-house code (for details see Angeli et al.⁴⁰), including the correction of the center band from the contribution of $n = 0$ spinning sideband coming from the satellite transitions.

Dissolution experiments

The initial dissolution rate, r_0 , of each glass was measured in static mode, at the temperature of 90 °C, and in a solution with initial pH^{90 °C} adjusted at 9. These conditions ensured that glass dissolution is controlled by the hydrolysis of the covalent bonds (i.e., Si–O–M with M = Si, Al, B, or Zr). Hence, the release of Si is here used to calculate the glass dissolution rate. Experiments were conducted in perfluoroalkoxy (PFA) vessels with volume of 250, 500, or 1000 mL. These vessels each come with a cap equipped with two small openings for solution sampling and pH control. The choice of the glass-surface-to-solution-volume ratio, S/V , resulted in a tradeoff

Table 6. Test conditions for each initial dissolution rate measurement conducted herein. S_{geo} is the geometric surface area of the glass powder, M the mass of the glass powder, V the volume of the leaching solution, and t the duration of the test.

Glass	Test #	Glass fraction powder (μm) or monolith	S_{geo} (cm^2)	M (g)	V (L)	S/V (cm^{-1})	t (h)
NBS12/28	1	Monolith	5.08	1.292	0.485	0.010	2.4
	2	40–63	37.6	0.080	0.999	0.038	0.7
NBS36/21	1	Monolith	6.18	1.986	1.017	0.006	0.4
NBS31/15	1	Monolith	5.51	1.721	1.009	0.005	0.4
NBS14/18	1	100–125	19.9	0.095	0.231	0.086	5.5
	2	100–125	42.0	0.200	0.488	0.086	5.1
	3	63–125	51.2	0.197	0.488	0.105	5.1
NBSA	1	100–125	41.6	0.198	0.490	0.085	10.6
NBSAC	1	100–125	42.0	0.200	0.496	0.085	5.5
NBSACZ	1	40–63	37.6	0.080	0.496	0.076	5.7
NBSAZ	1	100–125	43.4	0.207	0.497	0.087	10.6
NBSC	1	100–125	22.2	0.106	1.000	0.022	5.5
NBSCZ	1	100–125	21.6	0.103	0.999	0.022	5.5
NSAC19	1	20–40	132	0.165	0.490	0.269	4.1
	2	100–125	54.4	0.259	0.488	0.111	3.8
	3	100–125	54.6	0.260	0.495	0.110	5.2
NSAC17	1	20–40	87.9	0.110	0.488	0.180	4.1
	3	100–125	54.4	0.259	0.486	0.112	5.2
NSAC21	1	20–40	69.9	0.087	0.509	0.137	6.7
	2	20–40	69.4	0.087	0.478	0.145	6.2
	3	63–125	66.8	0.262	0.483	0.138	6.2
	4	100–125	54.8	0.261	0.493	0.111	3.8
	5	100–125	54.8	0.261	0.490	0.112	5.0
NSAC0	1	100–125	49.8	0.262	0.487	0.102	5.3
NSAC35	1	100–125	54.6	0.260	0.483	0.113	5.2
NSA	1	50–100	88.3	0.276	0.482	0.183	12.1

between the need of a sufficient amount of glass (50 mg) to reduce the uncertainty of the sampling and an upper limit of concentration in solution above which the silica released by the glass reduces the glass dissolution rate. This limit, above which the affinity of network dissolution is impacted, depends on the glass composition and must be verified experimentally by following both the linearity of the Si release and the congruency of the dissolution by calculating the ratio $\text{NL}(\text{Na})/\text{NL}(\text{Si})$ (see the definition of NL below). The dimensions given in Table 6 were chosen based on preliminary experiments (not shown here).

A typical dissolution experiment was conducted, as detailed in the following. A large magnetic bar of 3-to-5 cm long was placed in the reactor. The onset solution was prepared with 18.2 M Ω cm deionized water, heated to $(90 \pm 2)^\circ\text{C}$. The pH was adjusted to 9 ± 0.05 with LiOH 1 M. Time zero is set when the glass was poured in the leaching solution. From this moment, the glass always remained in suspension in the solution thanks to a quick agitation of the magnetic bar. The magnetic stirring system consisting of large square plate with 3 or 9 independent spots were placed in the oven. For the short duration tests (<1 h), samplings of 1–5 mL each were taken without removing the reactor from the stirring spot. A precise timer was used so that the samplings were made with a precision of 5 s. For the longer tests, the reactors were removed from the oven for sampling. They stayed outside of the oven for less than 1 min per sampling. The most soluble glasses were tested with large coupons to make sure that the reactive surface did not change much during the course of the experiment. In that case, the coupon was inserted into a Teflon[®] basket hung with Teflon[®] tapes in the center of the reactor. In this configuration, the Reynolds number—a dimensionless number indicating the flow pattern—was estimated to be >2000 , a value characteristic of a turbulent flow at the glass surface. Solution samplings were carried out with a 5 mL syringe. Samples were filtrated at 0.45 μm . Generally 5 or 6 samplings were carried out at regular intervals. For some tests, a few more samples of 1 mL each were taken and acidified with HNO_3 0.5 M for ICP-OES analyses. The pH was controlled at the end the test, except for the

glasses that dissolve incongruently. In this case the pH was regularly adjusted to the target value by addition of small quantities of HNO_3 0.5 N.

Si concentrations were determined by colorimetry with a Merck Spectroquant kit and a Cary Varian UV-visible spectrophotometer at a wavelength of 820 nm (concentration range: 0.05–5 mg L^{-1}). For some tests, extra samplings were also analyzed by ICP-OES (Thermo Scientific ICAP 6300 Duo) to confirm the data and get insight into the stoichiometry of the dissolution reaction. For the tests performed with coupons, the mass loss was determined after rinsing, drying and weighting the altered coupon.

Based on these tests, the forward dissolution rate r_0 was calculated by linear regression of the normalized mass losses of Si, $\text{NL}(\text{Si})$.

$$r_0 = \frac{d(\text{NL}(\text{Si}))}{dt}, \quad (3)$$

where $\text{NL}(\text{Si})$ was calculated allowing for the variations in the fraction of altered glass (FAG), the variation in volume of the leaching solution, and the variations in the reactive surface area of the glass according to a shrinking core model in spherical geometry, using the following equations:

$$\text{NL}(\text{Si})_n = \frac{3}{S_{\text{geo}}} \left[1 - (1 - \text{FAG}_n)^{1/3} \right], \quad (4)$$

$$\text{FAG}_{n=1} = \frac{C(\text{Si})_{j=1} \cdot V_0}{m \cdot x_i}, \quad (5)$$

$$\text{FAG}_{n>1} = \text{FAG}_{j-1} + \frac{\Delta C(\text{Si}) \cdot V_j}{m \cdot x_i}, \quad (6)$$

where n refers to the sample number, S_{geo} is the geometric surface area per gram of starting material, m the mass of glass, x_{Si} is the mass fraction of Si in the glass, V_0 the initial volume of the solution and $C(\text{Si})_j$ the concentration of Si in the j th sample. According to previous studies^{30,31}, the geometric surface area was considered to better represent the actual

reactive surface as compared to the BET specific area. S_{geo} was calculated as follow:

$$S_{\text{geo}} = \frac{6}{\rho \cdot \phi_m}, \quad (5)$$

where ρ is the glass density and ϕ_m the mean diameter of the glass powder. Although S_{geo} is a rough estimation of the reactive surface area of the glass powder, Fournier et al.³⁰ demonstrated that it is an acceptable approximation.

Uncertainty on r_0 was estimated according to the work conducted on ISG³⁰. A value of $\pm 30\%$ is taken in our study, accounting for errors propagation and reproducibility.

Under the selected T and pH conditions, glasses were supposed to dissolve congruently. But it appeared that some highly depolymerized glasses released Na^+ ions preferentially, thereby leaving a Na-depleted silica-rich material subject to hydrolysis. Glass dissolution was considered as non-congruent when $\text{NL}(\text{Na})/\text{NL}(\text{Si}) > 1.1$.

Table 6 summarizes the experimental conditions for each glass dissolution test.

TCT model

Based on the dissolution and structural data obtained in the present study, we assessed whether the topology of the atomic network of the silicate glasses considered herein can be used as a structural metric to predict (and extrapolate) their dissolution rate. To this end, we adopted the TCT framework^{14–16}. In this framework, atomic networks are considered as mechanical trusses, wherein some nodes (the atoms) are connected to each other via some constraints (the chemical bonds)^{15,16}. By simplifying complex disordered networks into simpler mechanical trusses, TCT captures the important network topology while filtering the second-order structural details of the atomic network that are unlikely to significantly affect the dissolution kinetics^{15,24}.

In atomic networks, relevant topological constraints comprise the 2-body radial bond-stretching (BS) and 3-body angular bond-bending (BB) constraints, which keep the bond distances and bond angles fixed around their average values, respectively. Based on Maxwell's criterion⁴² and a mean-field enumeration of the constraints, the mechanical stability of the network then depends on the balance between the number of constraints per atom (n_c) and the number of degrees of freedom of the network (i.e., 3 per atom). Based on this balance, TCT classifies the atomic networks as (i) flexible when $n_c < 3$, (ii) stressed-rigid when $n_c > 3$, and (iii) isostatic when $n_c = 3$.

In fully-connected networks made of covalent bonds (wherein all the topological constraints are active), the number of BS and BB created by a given atom are given by $\text{CN}/2$ and $2\text{CN}-3$, where CN is the coordination number¹⁴. However, it has been shown that certain weaker constraints (i.e., ionic bonds) can be either active or thermally-broken based on the temperature^{25,43}—for instance, weak ionic Si–O–Na bond-bending constraints are broken even at room temperature and, hence, are ignored from the present enumeration (see Table 3).

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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AUTHOR CONTRIBUTIONS

S.G., M.B., and J.D. supervised the study. S.G., N.B., and M.T. performed the leaching experiments. T.C. and F.A. performed the NMR analyses. M.W., X.L., L.D., J.M.D., J.D., N.B., M.T., S.G., and M.B. contributed to the modeling part. All the authors helped on paper editing.

COMPETING INTERESTS

The authors declare no competing interests.

ADDITIONAL INFORMATION

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