



OPEN Exploring multifunctional properties of ternary chalcogenides for advanced energy applications

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We performed a thorough first-principles study of Mg_2TeS and Mg_2TeSe , including structural, electronic, optical, and transport features. Structurally, both compounds have a trigonal R3m structure with different polyhedral designs. Mg_2TeSe shows a larger equilibrium volume, and thermodynamic parameter ($E_{\text{coh}} \approx -3.65$ eV/atom for Mg_2TeS and -3.79 eV/atom for Mg_2TeSe ; $\Delta H_f \approx -2.17$ and -2.53 eV/atom) indicate both are energetically valuable, with Mg_2TeSe relatively more stable. Electronically, these materials are found as direct band gap semiconductors. The WC-GGA underestimated band gaps with values of (≈ 1.49 eV and 1.83 eV), which were then corrected by SOC + TB-mBJ with values of (≈ 2.64 eV and 2.71 eV) for Mg_2TeS and Mg_2TeSe , respectively. Projected density of states indicates valence bands are dominated by Te states and conduction bands by Mg states, and replacing S with Se narrows the band gap while shifting density of states toward the Fermi level. Optically, notable interband responses occur with $\epsilon_1(\omega)$ and refractive index maxima between 5.0 and 5.5 eV, $\epsilon_2(\omega)$ peaks ≈ 5.5 – 5.8 eV, static refractive index ≈ 2.1 , absorption peaking at ≈ 4.0 eV (Mg_2TeS) and ≈ 3.5 eV (Mg_2TeSe), low static reflectivity (~ 0.12), and plasmonic loss peaks near 17.0 and 16.0 eV. The transport results demonstrate modest Seebeck at low T , electrical conductivity $\sigma/\tau \approx 2.27 \times 10^{19}$ and 2.24×10^{19} ($\Omega \cdot \text{m} \cdot \text{s}$)⁻¹ at 300 K, lower lattice thermal conductivity and a greater power factor for Mg_2TeSe , and ZT increasing with temperature to maxima ≈ 0.32 (Mg_2TeS) and 0.24 (Mg_2TeSe) at 1200 K, illustrating Mg_2TeSe 's promise for thermoelectric applications.

Keywords Direct band gap chalcogenides, Optoelectronics, Transport nature, FP-LAPW

Band gap engineering is an important field of study that focuses on adjusting the band gaps of various optical materials for their specific device applications. Mg-based chalcogenides such as MgS , MgSe , and MgTe are wide band gap semiconductors with significant scientific value owing to their extensive uses in optoelectronic and luminous appliances^{1,2}. Some substantial experimental and theoretical studies were carried out on their crystalline phases of rock salt (B1), zincblende (B3), and wurtzite (B4)^{3–5}. At room temperature, MgS and MgSe adopt the B1 configuration⁶; however, other researchers have suggested alternative firm structures for these MgTe -based systems. Investigational research reveals that MgTe crystallizes in the B4 configuration under normal conditions^{7,8} and transforms to the NiAs (B8) structure under high pressure. In theory, Gokoglu et al.⁹ employed the projector augmented wave technique to determine the structures of MgS and MgSe as B1 and MgTe as B8. Drief et al.¹⁰ used the (FP-LAPW) approach to argue that B1 was the most stable structure for all three compounds, MgS , MgSe , and MgTe . The electronic structural and thermodynamic features of magnesium chalcogenide ternary alloys are examined employing first-principles approaches¹¹. The high magnesium-ion mobility of ternary spinel chalcogenides is examined to assess their potential for energy storage applications¹². McKeever et al.¹³ studied the design, features, and functional possibilities of alkali metal and Mg-based ternary chalcogenides for advanced applications. Debnath et al.¹⁴ employed density functional theory to study the structural, elastic, and optoelectronic features of the cubic $\text{Be}_x\text{Mg}_{1-x}\text{S}$, $\text{Be}_x\text{Mg}_{1-x}\text{Se}$, and $\text{Be}_x\text{Mg}_{1-x}\text{Te}$ semiconducting alloys. Khare et al.¹⁵ studied the electronic, optical, and thermoelectric features of sodium and magnesium pnictogen chalcogenides with first-principles calculations. Yaqoob et al.¹⁶ performed an ab initio study on the structural, electronic, and thermodynamic properties of ternary XCo_2S_4 chalcogenides ($X = \text{Mg}, \text{Zn}$). Thangavel et al.¹⁷ used first-principles simulations to explore the ground-state features and structural phase transitions of ternary chalcogenide semiconductors under high pressure. MgGeO_3 and MgSnO_3 , interesting materials are studied for their visible-light-driven energy applications because to their tunable

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structural, electronic, and photocatalytic features, primarily under applied stress¹⁸. Furthermore, substantial direct fundamental band gaps have been seen in the zinc-blende structures of MgS, MgSe, and MgTe^{19–21}. The combination of same-chalcogen diatomic magnesium and Br chalcogenides with varying concentrations could produce several distinct triple amalgams with entirely dissimilar and intriguing physical features. A theoretical study^{22,23} investigates the optoelectronic features of $\text{Be}_x\text{Mg}_{1-x}\text{X}$ (where X = S, Se, or Te) ternary materials. Sajid et al.²⁴ studied indirect band gap semiconductors MgS, MgSe, and MgTe, resulting in the formation of direct band gap semiconductors $\text{MgS}_x\text{Se}_{1-x}$, $\text{MgS}_x\text{Te}_{1-x}$, and $\text{MgSe}_x\text{Te}_{1-x}$ with x values ranging from 0.25 to 0.75. It was observed that both $\epsilon_1(0)$ and $\sigma(0)$ change in distinct directions depending on the dopant concentration. At x = 0.75, the essential points and highest places in the visual spectra of the three compounds shift northward. $\text{MgS}_x\text{Te}_{1-x}$ materials exhibit a broad energy band gap and large stationary dielectric constant values at x = 0, 0.25, and 0.50, making them ideal for optoelectronics and microelectronic devices²⁵. The electronic, optical, and transport properties of MgCdO_2 and MgCdS_2 materials are calculated using the density functional theory calculations²⁶.

Hassan et al.¹¹ used the FP-LAPW approach to analyze the physical, electronic, and thermal nature of the $\text{MgS}_x\text{Se}_{1-x}$, $\text{MgSe}_x\text{Te}_{1-x}$, and $\text{MgS}_x\text{Te}_{1-x}$ compositions. This study overcomes these constraints by employing Boltzmann transport calculations and first-principles density functional theory (DFT) to investigate the impact of chalcogen (S and Se) on the electronic structure, optical, and TE characteristics of these Mg-based systems. Our study reveals that Mg_2TeS and Mg_2TeSe are distinct ordered ternary compounds that crystallize in the R3m structure. These stoichiometries have not been fully investigated using a first-principles approach. The ability of ordered compounds to combine the preferred chemical bonding environment of chalcogen binaries with the increased structural flexibility and tunability offered by ternary ordering, which can result in improved thermodynamic stability and optimized transport behavior, is what drives the choice of these specific stoichiometries and crystal symmetry. Ordered compounds, as compared to random solid solutions, allow predictable site occupation, which makes it possible to investigate the formation energies, band dispersions, and effective mass trends more clearly. Furthermore, by balancing lighter (S/Se) and heavier (Te) chalcogen elements, they can also enhance carrier mobility and introduce phonon scattering paths appropriate for thermoelectric performance. Mg_2TeS and Mg_2TeSe are predicted to provide performance improvements over their binary counterparts. Our present study analyzes a structural theme known to be stable in equivalent chalcogenides and is anticipated to produce a favorable mixture for electronic and thermal transport properties by focusing on the R3m symmetry. The present research shows that S and Se greatly improve the thermoelectric figure of merit by methodically examining band structure modifications, carrier transport improvements, and phonon scattering mechanisms. The findings open the door for the development of next-generation thermoelectric materials while providing vital insights into how focused chemically substituted materials might maximize the relationship between thermal resistance and electrical conductivity. Additionally, providing significant design techniques for improving the effectiveness of Mg-based optoelectronics and thermoelectric devices, the present investigation increases fundamental knowledge and renders them attractive choices for sustainable energy applications.

Computational methodology

All computations in this study were performed with the exceptionally accurate (FP-LAPW + lo) technique, which is applied in the WIEN2k code and built on DFT²⁷. DFT calculates a system's total energy as a function of electron density and solves the Schrödinger equation with only atomic numbers as input parameters, and has become an enormously influential tool for researching the physical and chemical features of an extensive variety of compounds²⁸. DFT was similarly a common approach for researching precise effects that are hard or impossible to identify via testing, as well as forecasting novel materials. It is occasionally used to substitute expensive or impossible-to-complete laboratory experiments. To account for electron correlation and exchange effects, the structural and elastic properties were computed with Wu and Cohen's proposed general gradient approximation (WC-GGA)²⁹. In contrast, electrical features were evaluated using the Tran-Blaha modified Becke-Johnson (TB-mBJ)³⁰. Spherical harmonic functions are amplified to improve the wave function, charge density, and potential of the muffin-tin spheres, while a plane-wave basis set is used in the interstitial area. To obtain appropriately accurate data for the energy junction while calculating eigenvalues, wave functions are extended using a plane-wave basis set in the interstitial region, with an $R_{\text{MT}} \times K_{\text{max}}$ cut-off limit of 7. R_{MT} stands for the minimum muffin-tin radius, while K_{max} represents the highest k-vector value used in the plane-wave expansion. The maximum value chosen to increase the electron density inside these muffin tin spheres was $l = 10$. To mix into the (BZ), we employed a modified tetrahedron method with an $11 \times 11 \times 7$ mesh in k-space. Using the Monkhorst-Pack approach, we obtained 84 k-points in the IBZ. Self-consistent computations were deemed to have converged when the system's total energy stabilized within a 0.0001 R_y range.

Results and discussion

Structure properties

Mg_2TeS exhibits an Enargite-like structure that develops in the trigonal R3m space group (see Fig. 1). These are two unequal Mg^{2+} sites. In that primary Mg^{2+} site, Mg^{2+} bonds with one Te^{2-} and three identical S^{2-} atoms to generate edge-sharing MgTeS_3 tetrahedra. The Mg-Te bond distance was 2.81 Å. Wholly Mg-S bonds were 2.580 Å. In that, another Mg^{2+} site, Mg^{2+} , bonds with three comparable Te^{2-} and one S^{2-} atoms to produce corner-sharing MgTe_3S tetrahedra. All the Mg-Te bonds measure 2.740 Å. That Mg-S bond distance is 2.47 Å. Te^{2-} bonds with four Mg^{2+} atoms, resulting in TeMg_4 tetrahedra, sharing corners with six TeMg_4 tetrahedra and six SMg_4 tetrahedra. S^{2-} connects to four Mg^{2+} atoms that forms SMg_4 tetrahedra, sharing corners alongside six TeMg_4 tetrahedra and six SMg_4 tetrahedra. Mg_2TeSe has a Cu_3AsS_4 -like structure and develops in the triangular R3m space group. A total of two equivalent Mg^{2+} positions. In that first Mg^{2+} site, Mg^{2+} bonds to one Te^{2-} and

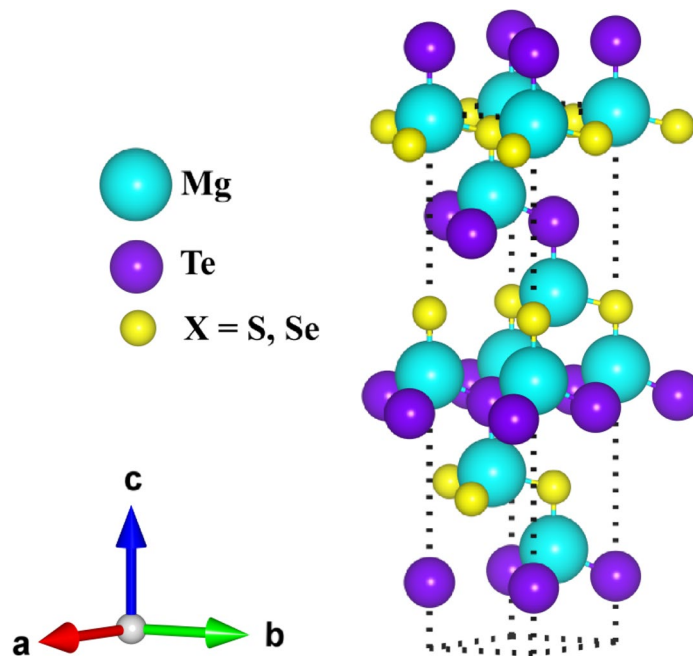


Fig. 1. The calculated crystal structure using VESTA for Mg_2TeX ($\text{X}=\text{S}, \text{Se}$) materials.

Materials	E_{coh} (eV/atom)	ΔHf (eV/atom)	Reference states (for ΔHf)
Mg_2TeS	-3.65 ± 0.05	-2.17 ± 0.05	hcp-Mg, $\alpha\text{-S}_8$, trigonal Te
Mg_2TeSe	-3.79 ± 0.05	-2.53 ± 0.05	hcp-Mg, trigonal Se, trigonal Te

Table 1. The computed cohesive and formation energies (hcp-Mg, $\alpha\text{-S}_8$, trigonal Se, and trigonal Te with reference states).

three identical Se^{2-} atoms, resulting in edge-sharing MgTeSe_3 tetrahedra. The Mg-Te bond length was 2.801 Å. Altogether, Mg-Se bonds are 2.670 Å. In the second Mg^{2+} location, Mg^{2+} bonds with three Te^{2-} and one Se^{2-} atoms, resulting in corner-sharing MgTe_2Se tetrahedra. All Mg-Te bonds range from 2.770 Å. The Mg-Se bond distance was 2.601 Å. Te^{2-} bonds with four Mg^{2+} atoms, resulting in TeMg_4 tetrahedra, which distribute edges with six TeMg_4 tetrahedra and six SeMg_4 tetrahedra. The cohesive energy of a substance indicates the strength of bonding among its constituent atoms, while the formation energy demonstrates its thermodynamic stability with its constituent components. Mg_2TeS possesses slightly smaller cohesive energy (-3.65 eV/atom) than Mg_2TeSe (-3.79 eV/atom), implying stronger bonds. This is probably owing to the greater electronegativity and bonding strength of selenium (Se) compared to sulfur.

The predicted formation enthalpies (ΔHf) for Mg_2TeS (-2.17 eV/atom) and Mg_2TeSe (-2.53 eV/atom) reveal that both materials are exothermic relative to their constituent elemental reference states. This indicates a thermodynamic preference for formation from elements under the chosen reference convention. The uncertainties (± 0.05 eV/atom) are careful predictions based on DFT convergence sensitivity (k-points, cut_{off}). The ΔHf values are per atom and link to the elemental end members given. Mg_2TeSe 's negative E_{coh} and ΔHf suggest a larger overall binding and driving force for formation compared to Mg_2TeS , which renders it intrinsically more favorable in the Mg-Te-Se chemical space. To attain true phase stability, the convex-hull (ΔE_{hull}) of all competing phases in the Mg-Te-S/Se space, such as MgTe, MgSe, MgS, MgX_2 stoichiometries, and reported ternaries, needs to be evaluated in addition to elemental-referenced ΔHf . $\Delta E_{\text{hull}} = 0$ eV/atom implies thermodynamic stability (on the hull), whereas modest positive ΔE_{hull} values (generally $\approx 25\text{--}50$ meV/atom) represent metastability and kinetic accessibility, and greater positive values indicate probable breakdown. Both compounds are appealing possibilities for synthesis, but specific stability judgments need explicit hull construction. The calculated cohesive and formation energies indicate that Mg_2TeS and Mg_2TeSe are thermodynamically advantageous, with negative values reflecting structural integrity and compound stability. When compared to reference states (hcp-Mg, $\alpha\text{-S}_8$, trigonal Se, and trigonal Te) (see Table 1), these materials have low formation energy, indicating that they are resilient against decomposition. Mg_2TeSe , with a greater negative formation energy than Mg_2TeS , is expected to be slightly more stable. Possible competitive phases, including MgS, MgSe, and MgTe binaries, are less favorable, indicating the ternary compounds' strong phase stability. Mg_2TeSe has a lower formation energy (-2.53 eV/atom) compared to Mg_2TeS (-2.17 eV/atom), showing its thermodynamic stability. It demonstrates that substituting sulfur with selenium promotes the structural stability of the compound. Magnesium (Mg) contributed considerably to the stability of both materials by strong electrostatic interactions with chalcogen

atoms, while tellurium (Te), which is larger and less electronegative, influences lattice dynamics and electronic characteristics. The discrepancy in formation and cohesive energies can be caused by differences in atomic size and electronegativity between S and Se. Se, being larger than S, forms slightly longer but stronger connections in this structure, giving greater cohesive energy. Mg_2TeSe is a little more stable than Mg_2TeS , as demonstrated by their negative formation energies. This pattern aligns with the usual behavior of chalcogenides, as Se-based compounds often demonstrate greater stability and bonding interactions than their sulfur counterparts. Mg_2TeSe is anticipated to have greater structural integrity and functional characteristics than Mg_2TeS . Figure 2a,b displays the fluctuation of the whole energy as a function of volume (in atomic units cubed) for two distinct materials, Mg_2TeS and Mg_2TeSe . The curves have a parabolic tendency, as expected of a state equation such as the Birch-Murnaghan or Murnaghan equation, in which the minimum energy is linked to the material's equilibrium volume. The depth and position of the minimum offer provide information about the stability and structural qualities of each material. The Mg_2TeS material has a lower equilibrium volume than Mg_2TeSe , indicating a more compact structure. Mg_2TeS has a lower equilibrium energy than Mg_2TeSe , which suggests that it is more stable. The substitution of selenium (Se) for sulfur (S) results in an increase in volume, which is due to selenium's higher atomic radius. This increase in volume has an impact on bonding interactions, which may modify mechanical and thermoelectric properties. Understanding these distinctions is critical for applications where these materials' structural and electrical properties influence their performance, such as thermoelectric devices.

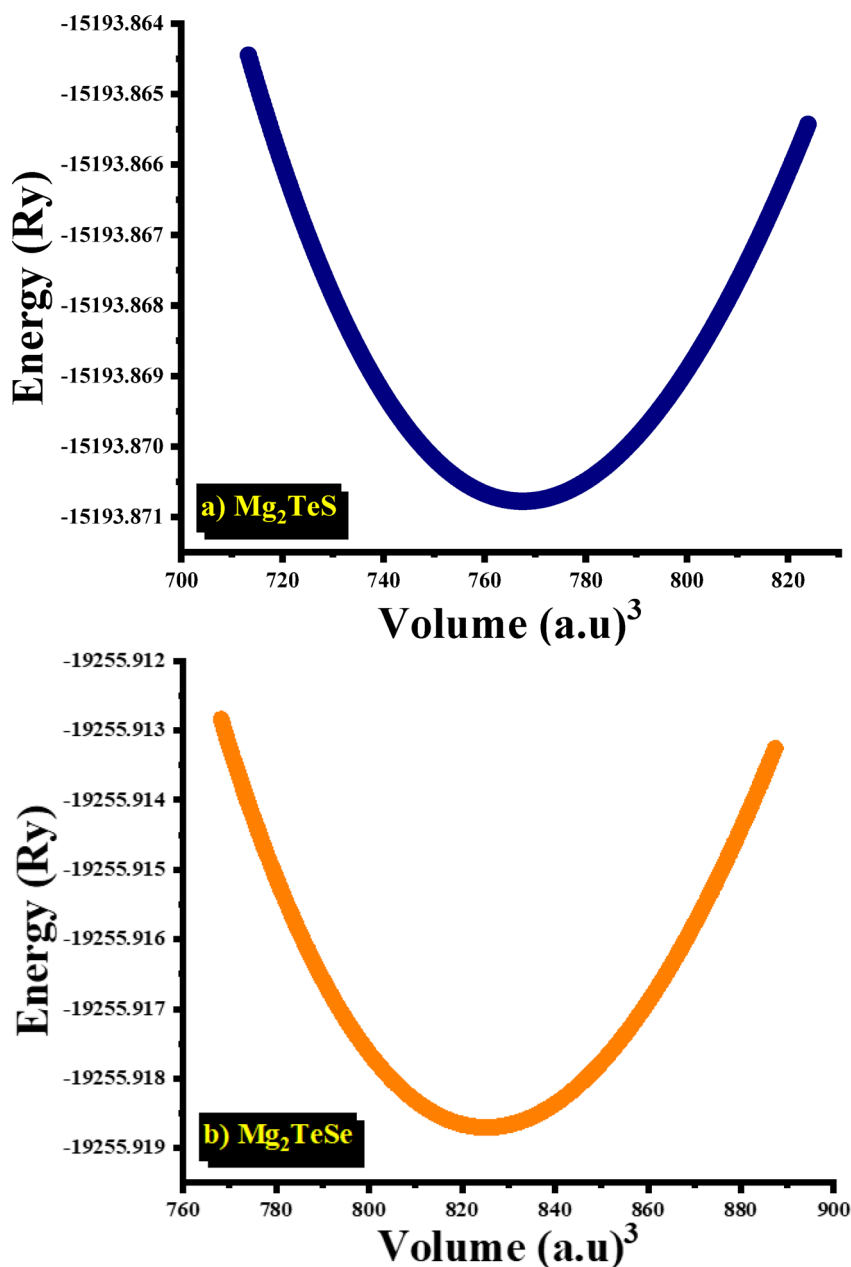


Fig. 2. The optimization curves of (a) Mg_2TeS and (b) Mg_2TeSe materials.

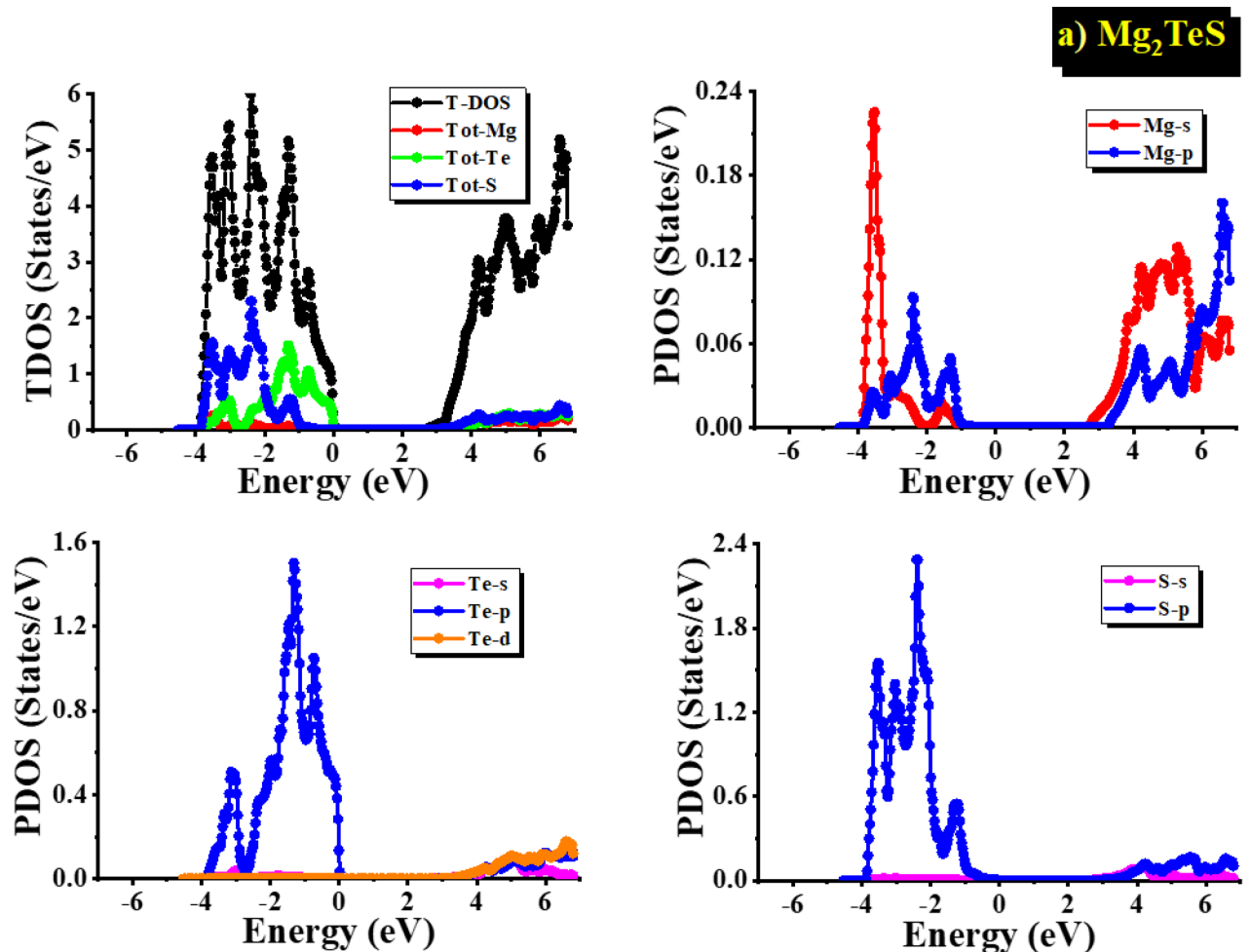


Fig. 3. The total and partial density of states plots of (a) Mg_2TeS and (b) Mg_2TeSe materials.

Electronic properties

Density of states investigations demonstrate how orbital contributions influence the electronic properties of Mg_2TeS and Mg_2TeSe . Orbital interaction affects the effective mass of charge carriers, which explains variances in transport performance. These characteristics have a direct impact on the Seebeck coefficient, carrier mobility, and optical absorption edges, all of which contribute to density of states characteristics throughout transport and optoelectronic effectiveness. Figure 3a,b displays the density of Mg_2TeS and Mg_2TeSe states in that valence band region. The variations in the density of state changes for Mg_2TeS and Mg_2TeSe in the valence band region are mostly caused by changes in the electronegativity, atomic radius, and bonding characteristics of sulfur and selenium. Sulfur has more electronegativity of 2.58 compared with a 2.55 for selenium. This indicates that Sulfur attracted electrons more strongly than Se, resulting in more tightly packed bonding states and a shift in energy levels. As a result, Mg-s and Mg-p contributions move deeper in energy than Mg_2TeSe . The Mg-s contribution is dominant in the -4.0 eV to -3.0 eV range for Mg_2TeS , although it is found at a lower energy series of -3.01 eV to -2.01 eV in Mg_2TeSe . In Mg_2TeS , the stronger Mg-S contact causes more mixing of s and p states at lower energy levels, whereas in Mg_2TeSe , the weaker Mg-Se interaction causes Mg-s and Mg-p states to emerge at larger energy levels. In the CB range, both materials exhibit Mg-s and Mg-p contributions within the $(3.0$ to $6.0)$ eV range. This resemblance occurs because conduction band states are predominantly formed from Mg orbitals, with little effect from the anion S or Se. Te-s states dominate the valence band in Mg_2TeS and Mg_2TeSe materials with energies ranging from -4.01 eV to the Fermi level. Tellurium (Te) is a heavy chalcogen element with a low-energy s orbital. Te is more electropositive than S or Se, hence it has a stronger presence in the VB region. Contributions of Te-s/p/d states in the CB for Mg_2TeS and Mg_2TeSe materials between 3.8 and 6.0 eV. The conduction band states include contributions from Mg-s and Mg-d states, which interact with Te-s, Te-p, and Te-d states to generate hybridized bands. S-s states dominate the valence band contribution in Mg_2TeS 's from $(-4.0$ to $-1.5)$ eV because sulfur's strong attraction to electrons results in more localized states in the lower energy range. In Mg_2TeSe , the Se-s state contributes primarily to the Fermi level from -3.01 eV, showing a shift in energy levels caused by Se's lower electronegativity. This allows the Se-s states to extend to the Fermi level, whilst S states remain deeper. Se has a greater atomic radius compared to S, which impact the bond length and energy overlap between orbitals, bringing the DOS closer to the Fermi level. In that conduction band, states given by

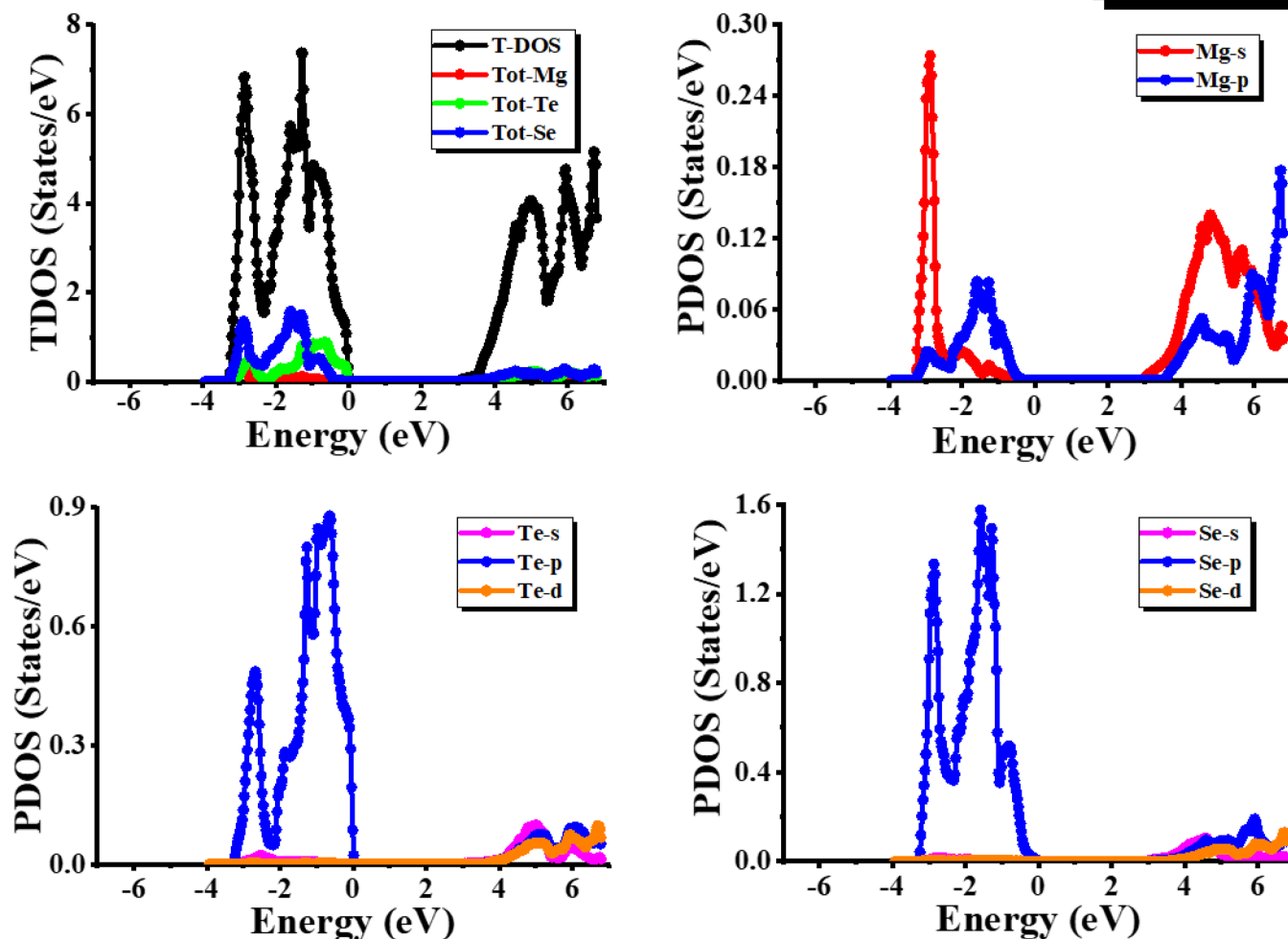
b) Mg_2TeSe 

Fig. 3. (continued)

S-s/p and Se-s/p/d from 3.8 eV to 6.0 eV are mostly owing to contributions from Te-p states that interact with S and Se states. The S-p states provide a major contribution to Mg_2TeS due to higher hybridization with Mg and Te. Because of the weaker binding in Mg_2TeSe , the Se-p and Se-d states stretch further into the conduction band, resulting in more delocalized and dispersed electronic states than S.

Figure 4 illustrates the electronic band structures of Mg_2TeS and Mg_2TeSe , revealing valuable information on their electrical properties. Both materials are semiconducting, with energy gaps that vary depending on the used functional. The TB-mBJ approach, both with and without SOC, yields more accurate estimates than WC-GGA, highlighting the significance of exchange-correlation treatment. The addition of SOC is especially important in Te-containing systems due to how it affects the valence band maximum (VBM) and conduction band minimum (CBM), leading to optical transition thresholds. These band gap properties have significant effects on carrier excitation energies, as well as the materials' potential for optoelectronic and thermoelectric applications. The WC-GGA approach underestimates band gaps, providing 1.49 eV for Mg_2TeS and 1.83 eV for Mg_2TeSe as shown in Table 2. This is a common restriction of semilocal functions. Application of TB-mBJ corrects this underestimation, anticipating 2.86 eV and 2.95 eV for Mg_2TeS and Mg_2TeSe , respectively, resulting in more realistic values. Te-rich chalcogenides have strong relativistic interactions; hence, SOC was specifically incorporated. This leads to slightly smaller gaps of 2.64 eV (Mg_2TeS) and 2.71 eV (Mg_2TeSe). SOC-induced splitting at the valence and conduction band minimizes the band ordering at Γ , leading to a drop of approximately 0.2–0.25 eV in comparison with TB-mBJ. At all levels of theory, Mg_2TeSe displays a narrower gap compared to Mg_2TeS , demonstrating Se's more delocalized p-states and stronger relativistic effects relative to S. Importantly, since WC-GGA underestimates and TB-mBJ slightly overestimates, SOC + TB-mBJ gives a balanced description of the band gap and band dispersion, ensuring accuracy in forecasting optical edges and transport performance. SOC is essential for Te-containing chalcogenides. Chemical substitution (S \rightarrow Se) adjusts the band gap, influencing carrier effective masses and transport characteristics. Thus, the addition of SOC and TB-mBJ provides reliable electronic structural insights, which are vital when analyzing optical absorption and

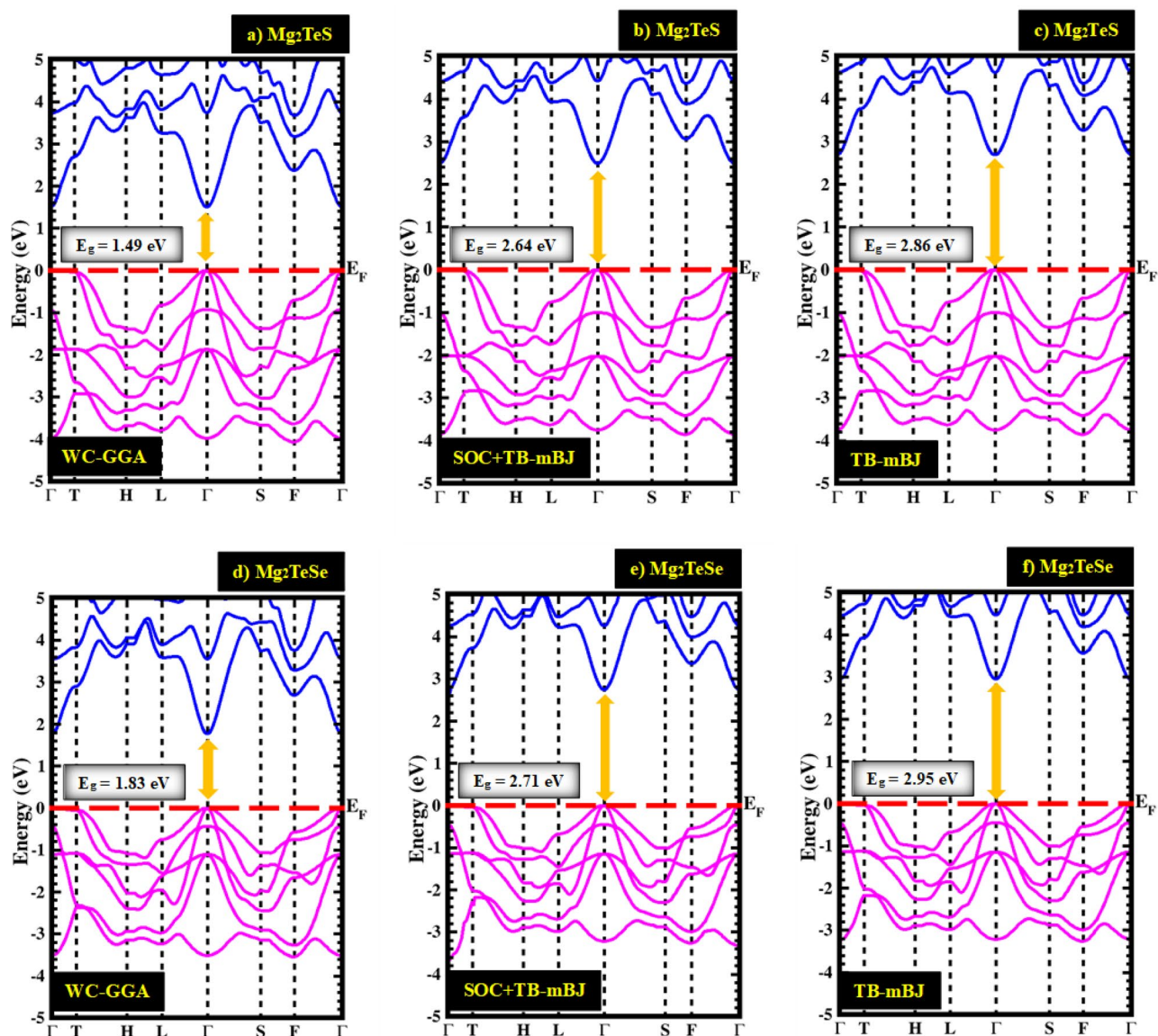


Fig. 4. The electronic band structures of (a–c) Mg_2TeS and (d–f) Mg_2TeSe computed using the WC-GGA, SOC+TB-mBJ, and TB-mBJ functionals, respectively, along the high-symmetry path (Γ -T-H-L- Γ -S-F- Γ). The Fermi level is set at 0 eV.

Materials	WC-GGA (eV)	SOC+TB-mBJ (eV)	TB-mBJ (eV)
Mg_2TeS	1.49	2.64	2.86
Mg_2TeSe	1.83	2.71	2.95

Table 2. The calculated energy band gap values for the Mg_2TeS and Mg_2TeSe materials employing the WC-GGA, TB-mBJ, and SOC+TB-mBJ approaches.

thermoelectric performance. Both Mg_2TeS and Mg_2TeSe have direct band gaps (Γ - Γ), indicating that the (VBM) and (CBM) are at the Γ -point of the Brillouin zone. That property was determined by electronic interactions inside the crystal structure, such as orbital hybridization between Mg, Te, S, and Se atoms. The electrical configuration of magnesium is $[\text{Ne}] 3s^2$. In both Mg_2TeS and Mg_2TeSe , the Mg-s and Mg-p states contribute to the VB and CB. The Mg-s state has a considerable influence in the region from -4.01 eV to -3.0 eV for Mg_2TeS and from -3.0 eV to -2.0 eV for Mg_2TeSe . This shift implies that Mg interacts differently with S and Se due to changes in electronegativity and bonding properties. Mg-s and Mg-p states dominate in both materials between 3.0 and 6.0 eV, demonstrating their importance in conduction. Te's electronic setup is $[\text{Kr}] 4d^{10}5s^25p^4$. It makes a significant contribution to the valence and conduction bands. Te-s contributes -4.0 eV to 0 eV in both materials,

suggesting substantial hybridization with Mg and S/Se. Te-s, Te-p, and Te-d states contribute between 3.8 eV and 6.0 eV, emphasizing their involvement in conduction. In Mg_2TeS , the S-s state contributes to the valence band region from $(-4.01 \text{ to } -1.5) \text{ eV}$, representing a durable bonding linking between S and Mg/Te. In that conduction band, the S-s and S-p states contribute between 3.8 and 6.0 eV. In Mg_2TeSe , the Se-s state contributes to the -3.0 eV Fermi level, indicating that Se hybridizes differently with Mg and Te than S. Se-s/p/d states contribute to the CB between 3.8 and 6.0 eV. The shifting contributions between Mg_2TeS and Mg_2TeSe indicate that Mg_2TeSe has a slightly smaller bandgap than Mg_2TeS , as the Se states are at a higher energy level than the S states. Te-s and Te-p hybridization with Mg and S/Se are more prominent in both cases, but Mg_2TeS has greater Mg-S bonding, shifting the S-s states lower in energy than Se-s in Mg_2TeSe .

Optical properties

Figure 5a depicts the real dielectric constant, $\epsilon_1(\omega)$, which is calculated by the material's ability to split in response to an external electrical field. At first, in both materials Mg_2TeS and Mg_2TeSe , $\epsilon_1(\omega)$ rises as the input photon energy shifts electrons from the valence bands to the conduction bands, improving the material's polarizability. The peaks at 5.0 eV indicate the most essential electronic transitions, and both materials have the highest ability to store electric field energy. At photon energies that exceed 5.0 eV, electrons absorb energy and transition to higher conduction states, leading to increased absorption. This absorption results in energy dissipation rather than polarization, resulting to a significant decrease in $\epsilon_1(\omega)$. When $\epsilon_1(\omega)$ approaches zero or becomes negative at 7.0 eV, both Mg_2TeS and Mg_2TeSe materials behave like metals, with free carriers dominating the optical response over bound electronic transitions. Selenium has a higher atomic radius than sulfur, resulting in less orbital overlap in the valence band. This reduces the DOS around the band margins, slightly limiting the material's capacity to polarize. Figure 5b depicts the imaginary dielectric constant, $\epsilon_2(\omega)$, for Mg_2TeS and Mg_2TeSe materials. The imaginary part of the dielectric function $\epsilon_2(\omega)$ was closely related to the interband optical variations from occupied VB to unoccupied CB states. That threshold energy where $\epsilon_2(\omega)$ begins to increase is linked to the minimal energy necessary for direct optical transitions, which is frequently near the fundamental band gap energy or somewhat higher due to selection rules and density of states effects. Mg_2TeSe has a slightly

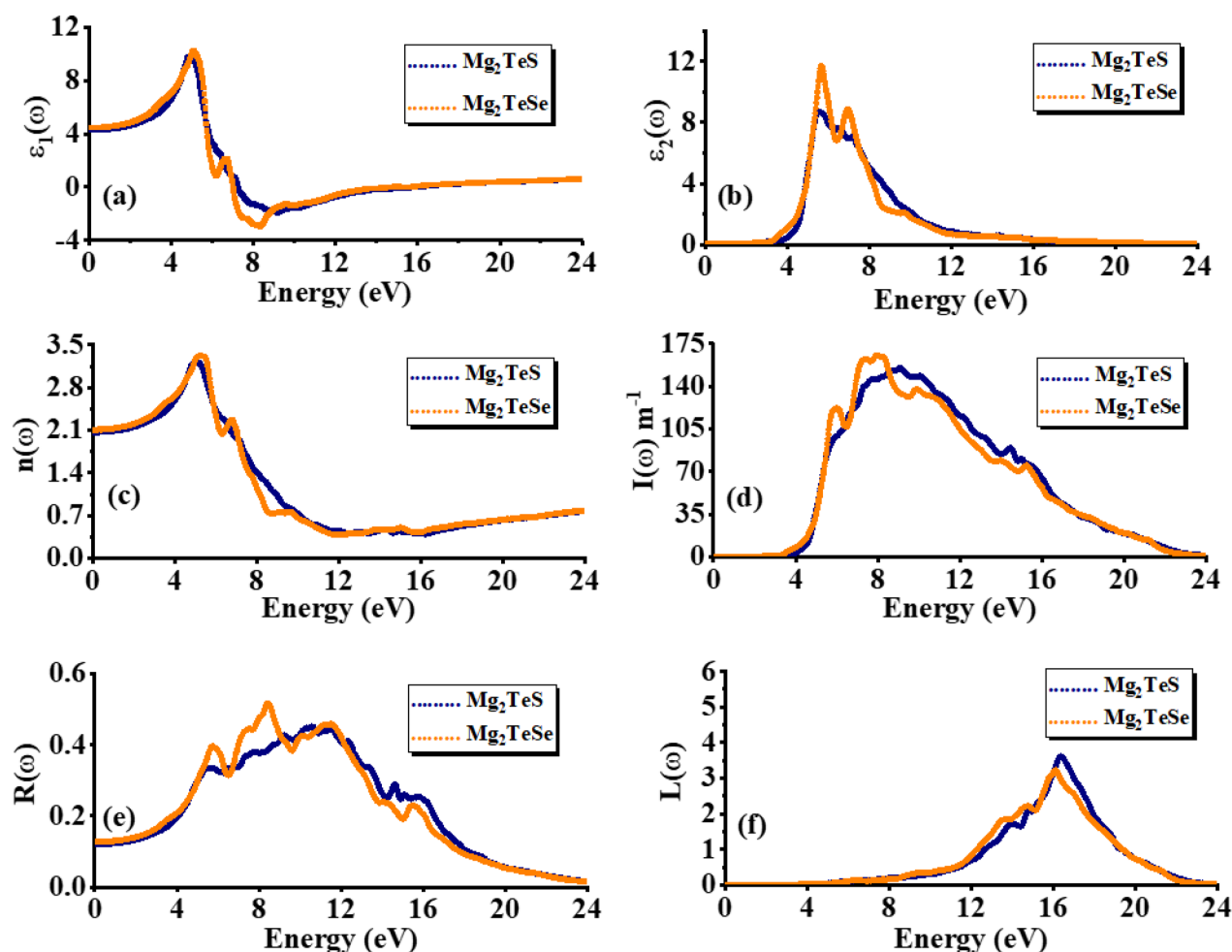


Fig. 5. The calculated (a) real part of the dielectric constant, (b) imaginary part of the dielectric constant, (c) Refractive Index, (d) Absorption coefficient, (e) Reflectivity, and (f) Loss function for Mg_2TeX ($X = \text{S}, \text{Se}$) materials.

lower threshold energy than Mg_2TeS , implying a smaller optical band gap. This is consistent with the general trend that heavier chalcogens (Se rather than S) have smaller band gaps due to weaker bonding and lower energy separation between valence and conduction bands. The peak in $\epsilon_2(\omega)$ occurs at 5.5 eV for Mg_2TeS and 5.8 eV for Mg_2TeSe when the joint density of states (JDOS) and optical transition probabilities are maximum. After reaching the peak, $\epsilon_2(\omega)$ begins to fall as the JDOS lowers at higher energies due to fewer accessible states for transitions. At high photon energies (over 16.0 eV), $\epsilon_2(\omega)$ decreases to zero as the material becomes essentially transparent, and no substantial interband transitions are conceivable within the energy series.

In Fig. 5c, the functioning of the refractive index $n(\omega)$ as a function of photon energy can be clarified through fundamental optical physics concepts about the interactions of electromagnetic waves with the electronic structure of materials. Mg_2TeS and Mg_2TeSe have identical static refractive index values of around 2.1, implying moderate optical density and relationship to low-energy electromagnetic waves. The refractive index $n(\omega)$ increases with photon energy from 0 eV, reaching its peak at 5.0 eV for Mg_2TeS and 5.5 eV for Mg_2TeSe . This rise is mostly caused by electronic interband transitions, in which photons drive electrons from the VB to the CB. That refractive index correlates with the dielectric function $\epsilon_1(\omega)$. A substantial electronic transition occurs at 5.0 eV for Mg_2TeS and 5.5 eV for Mg_2TeSe , resulting in a peak in the $\epsilon_1(\omega)$ and in $n(\omega)$. Beyond the peak, both materials' refractive index $n(\omega)$ drops. Absorption is represented by the $\epsilon_2(\omega)$, which increases strongly at and beyond the peak. Since the refractive index depends on both real $\epsilon_1(\omega)$ and imaginary components of $\epsilon_2(\omega)$, an increase in absorption leads to a lower $\epsilon_2(\omega)$, lowering $n(\omega)$. The Kramers-Kronig relations explain how these real and imaginary parts of the dielectric function interact. When absorption (associated with $\epsilon_2(\omega)$) increases significantly, the real component $\epsilon_1(\omega)$ begins to decrease, resulting in a decrease in $n(\omega)$. The absorption coefficient $I(\omega)$ indicates how strongly a substance absorbs light at various photon energies. Figure 5d illustrates the absorption spectra of Mg_2TeS and Mg_2TeSe , which have unique threshold values of 4.0 eV and 3.5 eV, respectively, and peak intensities followed by a drop. The peak values result from transitions between higher energy levels in the valence and conduction band, which include a high (JDOS) and strong dipole transition matrix element. The maximum absorption occurs at 9.0 eV for Mg_2TeS and 8.0 eV for Mg_2TeSe . These peaks imply strong electronic transitions beyond the basic band gap, where more interband transitions occur. Absorption is heavily dependent on the density of electronic states (JDOS). Furthermore, at very high photon energies, many-body interactions, including electron-electron scattering and electron-phonon interactions, increase. These interactions can cause energy widening and redistribution of optical transitions, resulting in reduced absorption.

Considering the optical properties and electronic transitions in Mg_2TeS and Mg_2TeSe may give insight into the behavior of static reflectivity $R(0)$ and frequency-dependent reflectivity $R(\omega)$. Figure 5e demonstrates that both Mg_2TeS and Mg_2TeSe possess a static reflectivity $R(0)$ value of 0.12, showing that they have a low reflectivity in the long-wavelength (infrared) or zero-frequency limit. This number is determined by the material's dielectric response, specifically the $\epsilon_1(0)$. The reflectance $R(\omega)$ increases with photon energy, peaking at 10.0 eV for Mg_2TeS and 8.0 eV for Mg_2TeSe . These peaks link to strong interband electronic transitions, in which photons of this energy excite electrons in the VB and transport them towards the CB. The reflectivity peaks occur because the dielectric function responds strongly to these photon energies, indicating the onset of significant optical absorption. The shift in the peak energy between Mg_2TeS and Mg_2TeSe can be attributed to differences in their electronic band structures. Mg_2TeS , which contains sulfur (S) with a smaller atomic size and higher electronegativity than selenium (Se), has a wider band gap and requires more photon energy to induce major interband transitions, resulting in a peak at 10.0 eV versus 8.0 eV for Mg_2TeSe . After peaking, $R(\omega)$ falls at higher photon energy. Figure 5f displays the energy loss function. The relationship between $L(\omega)$ and the dielectric function $\epsilon_2(\omega)$ is critical for understanding a compound's plasmonic activity. The onset energy is typically linked to the plasma frequency, which is determined by free carrier density and electron effective mass. The minor difference in threshold energy between Mg_2TeS at 5.5 eV and Mg_2TeSe at 6.0 eV is owing to variances in electronic structures, notably carrier concentration and band structure. The peaks in $L(\omega)$ indicate the most significant energy loss caused by collective plasmon excitations. The largest loss occurs at energy levels of 17.0 eV and 16.0 eV, respectively, because the plasmon resonance requirement is met, indicating that the material responds strongly to external perturbations at these frequencies. The Landau damping effect causes $L(\omega)$ to diminish after reaching its peak.

Transport properties

The Seebeck coefficient (S) shown in Fig. 6a for Mg_2TeS and Mg_2TeSe compounds at temperatures ranging from 100 to 1200 K. The Seebeck coefficient expresses the power produced per unit temperature variation around a compound. At low temperatures (100 K), the carrier concentration is low, and the Seebeck coefficient is predominantly determined by the dominant charge carriers (electrons in this case, because S is negative). Figure 6a shows that at 100 K, the highest Seebeck coefficient values for Mg_2TeS and Mg_2TeSe are $-6.0 \mu\text{V/K}$ and $-9.0 \mu\text{V/K}$, respectively. The higher Seebeck coefficient at this level indicates fewer free carriers and greater energy filtering effects. As the temperature rises (100–1200 K), intrinsic carrier excitation increases, leading to higher total carrier concentrations. The Seebeck coefficient is inversely associated with carrier concentration, resulting in a drop in S . At intermediate temperatures, enhanced phonon scattering affects charge carriers, changing the Seebeck coefficient even further. In strongly substituted semiconductors, ionized impurity and acoustic phonon scattering mechanisms dominate, resulting in a more significant drop in S . The decrease in S up to 900 K is due to both carrier excitation and scattering effects. Thermal excitation increases dramatically as temperatures near 1200 K, resulting in the creation of electrons and holes. This causes conduction, in which electrons and holes contribute oppositely to the Seebeck coefficient. Because of this effect, S has a minimum value of 1200 K, as contributions from both types of charge carriers effectively limit the overall magnitude of S . The observed similarity in Seebeck coefficient values for Mg_2TeS and Mg_2TeSe . At 1200 K, the highest electrical

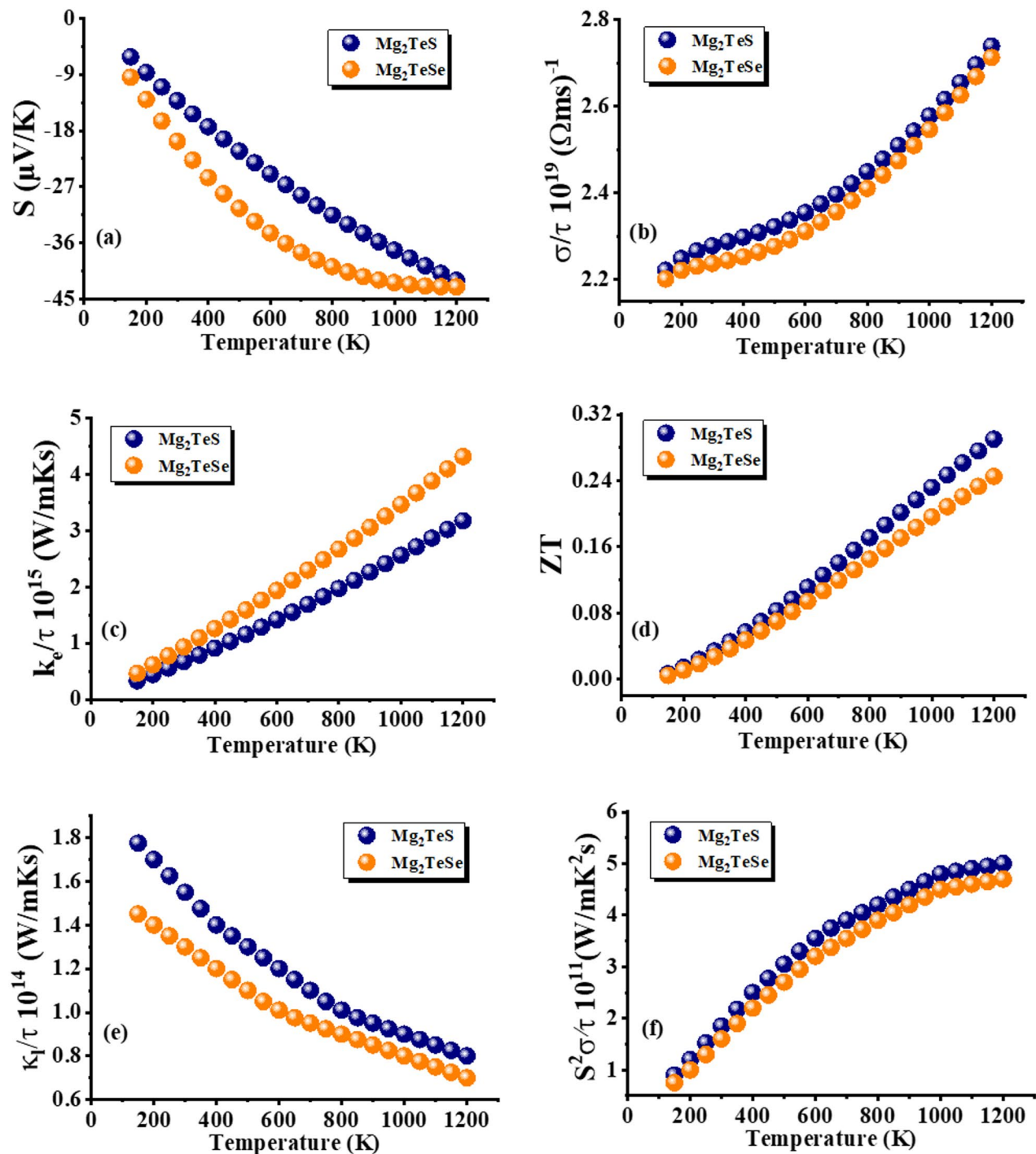


Fig. 6. The computed (a) Seebeck coefficient, (b) Electrical Conductivity, (c) Electronic thermal conductivity, (d) Figure of Merit, (e) Lattice thermal conductivity, and (f) Power factor for Mg_2TeX ($\text{X}=\text{S}, \text{Se}$) materials.

Mg_2TeSe at high temperatures ($-42.0 \mu\text{V/K}$ and $-43.0 \mu\text{V/K}$) indicates that both materials display comparable intrinsic excitation behavior and carrier transport capabilities. In Fig. 6b, both Mg_2TeS and Mg_2TeSe exhibit an increase in electrical conductivity (σ/τ) when the temperature rises from 100 K to 1200 K. Electrical conductivity (σ) is another important characteristic in thermoelectrics. It assesses the material's ability to conduct electrical currents. The conductivity per relaxation time (σ/τ) is displayed against temperature. Both materials exhibit an increase in electrical conductivity with temperature. Mg_2TeS has consistently better conductivity than Mg_2TeSe over the whole range. Mg_2TeS and Mg_2TeSe are most likely semiconductors, which means that their electrical conductivity is very temperature-dependent. The amount of thermally excited charge carriers is low at low temperatures due to the limited energy available to promote electrons over the band gap. The electrons possess sufficient energy to transit from the valence band to the conduction band, boosting carrier concentration and

electrical conductivity. When the temperature rises from 100 K to 1200 K, more electrons are excited around the band gap, resulting in improved carrier concentration and σ . At 300 K, the electrical conductivity values for Mg_2TeS and Mg_2TeSe are virtually identical, indicating equal intrinsic carrier concentrations and effective masses. At 1200 K, the conductivity of both materials improves but remains relatively close, indicating that they have similar band structures and charge transport mechanisms. At around 300 K, the σ/τ values for Mg_2TeS and Mg_2TeSe are 2.27×10^{19} and $2.24 \times 10^{19} (\Omega \text{ m s})^{-1}$, respectively. At 1200 K, the values were 2.78×10^{19} and $2.76 \times 10^{19} (\Omega \text{ m s})^{-1}$ for Mg_2TeS and Mg_2TeSe , respectively.

Figure 6c illustrates a linear rise in electronic heat conductivity (κ_e) for Mg_2TeS and Mg_2TeSe when the temperature rises from 100 K to 1200.01 K. Mg_2TeS and Mg_2TeSe exhibit a linear increase in electronic thermal conductivity (κ_e) from 100 K to 1200 K, owing to the temperature dependence of electrical conductivity (σ) and the Wiedemann-Franz law. At 300 K, Mg_2TeS has a thermal conductivity of $0.5 \times 10^{15} \text{ W m}^{-1} \text{ s}^{-1}$, while Mg_2TeSe has $1.0 \times 10^{15} \text{ W m}^{-1} \text{ s}^{-1}$, indicating that Mg_2TeSe has a greater carrier transport efficiency. At 1200 K, the maximum numbers of κ_e for Mg_2TeS and Mg_2TeSe are 3.0 and $4.5 \times 10^{15} \text{ W m}^{-1} \text{ s}^{-1}$, respectively. This confirms that Mg_2TeSe has higher electronic transport capabilities due to its more conductive structure. Mg_2TeSe has a higher intrinsic electrical conductivity than Mg_2TeS due to differences in band structure and carrier effective masses, as indicated by the κ_e difference between the two. The figure of merit ZT is an important quantity in thermoelectric materials since it dictates how efficiently they convert heat into electricity. Higher ZT values indicate improved thermoelectric performance, which is critical for applications such as waste heat recovery, power generation in spacecraft, and cooling and refrigeration. Fig. 6d illustrates the behavior of the figure of merit ZT for Mg_2TeS and Mg_2TeSe . ZT for both Mg_2TeS and Mg_2TeSe increases approximately linearly from 100 to 1200 K. In semiconductors, when the temperature rises, more charge carriers (electrons or holes) are thermally activated, enhancing electrical conductivity. ZT results in a rising trend in ZT. At high temperatures, both intrinsic carrier excitation and reduced phonon transport improve thermoelectric performance. This leads to a nearly linear increase in ZT. Figure 6d reveals that ZT values at 300 K are 0.05 and 0.03 for Mg_2TeS and Mg_2TeSe , respectively. The greatest figure of merit, ZT values at 1200 K are 0.32 and 0.24 for Mg_2TeS and Mg_2TeSe , respectively. Mg_2TeS has somewhat greater ZT than Mg_2TeSe across the full range. Minor variations in band convergence or (DOS) near the Fermi level between Mg_2TeS and Mg_2TeSe may improve carrier transport characteristics in Mg_2TeS . ZT is projected to grow with temperature as electrical conductivity improves and the material becomes more efficient.

The variation in lattice thermal conductivity (κ_l) with temperature for Mg_2TeS and Mg_2TeSe in Fig. 6e reveals a clear declining trend. This is consistent with the general behavior of crystalline semiconductors, where higher phonon-phonon scattering dominates at high temperatures. At low temperatures, κ_l is higher due to less scattering. Still, as the temperature rises, phonon-phonon Umklapp interactions intensify, leading to a rapid decrease. Mg_2TeS consistently outperforms Mg_2TeSe in terms of κ_l across all temperatures. The lighter atomic mass of sulfur relative to selenium results in stronger bonding and greater phonon group velocities in Mg_2TeS , increasing its heat conductivity. The heavier selenium atoms in Mg_2TeSe increase lattice anharmonicity, increase phonon scattering, and decrease κ_l . Mg_2TeS may have slightly stronger heat conduction, but Mg_2TeSe possesses a greater potential for thermoelectric applications due to its lower inherent κ_l . Mg_2TeS and Mg_2TeSe display a continuous increase in power factor ($\text{PF} = S^2\sigma$) as temperature rises (see Fig. 6f), consistent with thermoelectric semiconductors. At greater temperatures, electrical conductivity (σ) improves because of increased carrier activation, whereas the Seebeck coefficient (S) remains large enough to support PF formation. Mg_2TeSe exhibits greater PF than Mg_2TeS across the temperature range, implying better electronic transport properties. The heavier selenium atom improves band convergence and retains modest conductivity. Mg_2TeS , with lighter sulfur atoms, exhibits stronger bonding but lower band degeneracy, resulting in limited PF values. Mg_2TeSe is the most attractive thermoelectric contender because of its high PF and decreased lattice thermal conductivity (κ_l), which can lead to higher ZT values. Mg_2TeSe exceeds Mg_2TeS in thermoelectric applications because of its greater balance of low κ_l and high power factor.

Conclusions

The present first-principles calculation for Mg_2TeS and Mg_2TeSe yields strong and complementary results of their structural, electronic, optical, and transport studies. structurally both materials crystallize in trigonal R3m shapes with distinct polyhedral motifs and calculated bond lengths ($\text{Mg}-\text{Te} \approx 2.74\text{--}2.81 \text{ \AA}$, $\text{Mg}-\text{S} \approx 2.47\text{--}2.58 \text{ \AA}$, $\text{Mg}-\text{Se} \approx 2.60\text{--}2.67 \text{ \AA}$), Mg_2TeSe exhibits a greater equilibrium volume whereas Mg_2TeS is more compact, and energetic metrics demonstrate negative cohesive energies (E_{coh} : -3.65 eV/atom for Mg_2TeS , and -3.79 eV/atom for Mg_2TeSe) and formation enthalpies (ΔH_f : -2.17 and -2.53 eV/atom), suggesting thermodynamic favorability with Mg_2TeSe slightly greater stable; electronically both materials are direct-gap semiconductors at Γ -point with WC-GGA underestimating the band gaps, and SOC + TB-mBJ giving balanced values. Likewise the Mg and Te orbitals dominating conduction and valence edges respectively and substitution S \rightarrow Se narrows the gap and shifts DOS towards the Fermi level; optically both materials display strong interband responses with $\epsilon_1(\omega)$ and refractive index peaking close to $5.0\text{--}5.5 \text{ eV}$, $\epsilon_2(\omega)$ peaks at $\sim 5.5\text{--}5.8 \text{ eV}$, static refractive index ≈ 2.1 , absorption thresholds at $\sim 4.0 \text{ eV}$ for Mg_2TeS and $\sim 3.5 \text{ eV}$ for Mg_2TeSe , minimal static reflectivity $R(0) \approx 0.12$ and plasmonic loss peaks at ≈ 17.0 and 16.0 eV ; transport computations demonstrate small Seebeck magnitudes at low T, enhancing electrical conductivity with T ($\sigma/\tau \approx 2.27 \times 10^{19}$ and $2.24 \times 10^{19} (\Omega \cdot \text{m} \cdot \text{s})^{-1}$ at 300 K), κ_e and κ_l trends where Mg_2TeSe has smaller lattice thermal conductivity and higher power factor, and ZT increasing with temperature to maxima of ≈ 0.32 (Mg_2TeS) and 0.24 (Mg_2TeSe) at 1200 K, making Mg_2TeSe a promising thermoelectric candidate because to its favorable PF/ κ_l balance.

Data availability

The datasets used and/or analysed during the current study are available from the corresponding author on reasonable request.

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Declarations

Competing interests

The authors declare no competing interests.

Additional information

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