

# Bridging photocatalysis and artificial intelligence to maximize CH<sub>4</sub> and CO production from CO<sub>2</sub> reduction using synthesized g-C<sub>3</sub>N<sub>4</sub>/TNTAs photocatalysts

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1        **Bridging photocatalysis and artificial intelligence to**  
2        **maximize CH<sub>4</sub> and CO production from CO<sub>2</sub> reduction**  
3        **using synthesized g-C<sub>3</sub>N<sub>4</sub>/TNTAs photocatalysts**

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17        **Abstract**

18        The photocatalytic CO<sub>2</sub> conversion into value-added chemicals such as CH<sub>4</sub>  
19        and CO is a highly promising sustainable approach to meet rising energy  
20        demands while mitigating atmospheric CO<sub>2</sub> levels. This study investigates the  
21        prediction and optimization of CH<sub>4</sub> and CO production using tree-based  
22        machine learning (ML) models applied to g-C<sub>3</sub>N<sub>4</sub>/TiO<sub>2</sub> nanotube arrays  
23        (TNTAs) photocatalysts for gas-phase CO<sub>2</sub> conversion. To predict the  
24        photoconversion rates of CO<sub>2</sub> into CH<sub>4</sub> and CO, several tree-based ML  
25        algorithms, including AdaBoost, Bagging, CatBoost, Decision Tree, Extra  
26        Trees, Gradient Boosting, HistGradientBoosting, LightGBM, RandomForest,  
27        and XGBoost were employed. The production of CH<sub>4</sub> and CO (μmol/cm<sup>2</sup>) were  
28        designated as the target outputs, while input parameters included catalyst  
29        **exposed** surface area, initial concentration of CO<sub>2</sub>, feed pressure, light power,

30 and irradiation time. The performance of ML algorithms was appraised using  
31 five statistical metrics. Bayesian optimization was employed to fine-tune the  
32 hyperparameters of the machine learning model algorithms. Among the  
33 evaluated models, CatBoost (CB) performed the most accurately, with  $R^2 =$   
34  $0.9887$  (training) and  $R^2 = 0.9883$  (test) for  $\text{CH}_4$  production and  $R^2 = 0.9885$   
35 (training) and  $R^2 = 0.9874$  (test) for  $\text{CO}$  production. Feature importance  
36 analysis and SHAP plots highlighted the significant influence of irradiation  
37 time and catalyst **exposed** surface area on the production efficiency of both  
38 products. Additionally, the input parameters were systematically optimized  
39 using CB model predictions, which were validated against experimental data  
40 and achieved almost similar prediction. These results support the  
41 effectiveness of ML-directed modeling in maximizing  $\text{CO}_2$  conversion  
42 efficiency and revealing the potential of data-driven strategies in steering  
43 photocatalytic technology.

44 **Keywords:** Photocatalytic  $\text{CO}_2$  conversion; g- $\text{C}_3\text{N}_4/\text{TiO}_2$  nanotube arrays  
45 (TNTAs); Machine learning (ML); CatBoost (CB).

## 46 1. Introduction

47 The dependency on fossil fuels is progressively increasing worldwide for  
48 energy production, which results in escalating releases of greenhouse gases  
49 (GHGs), including  $\text{CO}_2$  thus striking a serious and inevitable threat to the  
50 environment and sustainable future. The production of solar fuels, which  
51 harness the plentiful sunlight, is one of the most auspicious routes for  
52 renewable energy production. A sustainable and realistic solution to the  
53 present energy crisis and environmental issues can be a photocatalytic  $\text{CO}_2$   
54 reduction (PC- $\text{CO}_2\text{R}$ ) approach. During the reduction process,  $\text{CO}_2$  is usually  
55 converted into  $\text{C}_1$  (one-carbon) and  $\text{C}_{1+}$  (multi-carbon) compounds solar fuels  
56 such as  $\text{CO}$ ,  $\text{CH}_4$ ,  $\text{CH}_3\text{OH}$ ,  $\text{C}_2\text{H}_4$  and  $\text{C}_2\text{H}_5\text{OH}$  [1-3]. The utilization of reliable  
57 and effective photocatalysts as well as appropriate reaction conditions are  
58 crucial for enhancing the production of solar fuels.

59        Semiconductor photocatalysts are the most auspicious candidates for the  
60 photoinduced CO<sub>2</sub> reduction [4,5]. The most investigated UV light-active  
61 photocatalyst is TiO<sub>2</sub> owing to its non-toxicity, photo-chemical stability, and  
62 availability [6,7]. Anodic TiO<sub>2</sub> in the form of nanotube arrays (NTAs) have  
63 drawn an ample amount of attention as prospective photocatalysts to  
64 overcome its inherent wide bandgap constraint [8-11]. Still, TNTAs require  
65 modification to reduce the rate of recombination of photoexcited charges and  
66 enhance performance under the exposure of visible light. Graphitic carbon  
67 nitride (g-C<sub>3</sub>N<sub>4</sub>) synthesized from earth-abundant elements, is another widely  
68 used semiconductor photocatalyst owing to its diverse hierarchical  
69 structures, outstanding photochemical stability and charge transfer  
70 efficiency [12]. Despite these benefits, the rapid charge carrier  
71 recombination rate and relatively broad bandgap usually prevent it from  
72 being effective as a standalone photocatalyst. The development of a robust  
73 heterojunction between TNTAs and g-C<sub>3</sub>N<sub>4</sub> is one of the most practical ways  
74 to lessen the recombination of photogenerated charge carriers and enhance  
75 the visible light sensitivity of pure TNTAs and g-C<sub>3</sub>N<sub>4</sub> [13,14]. Besides the  
76 properties of photocatalytic materials, the photocatalytic reaction conditions  
77 also significantly affect the efficiency of PC-CO<sub>2</sub>R. Therefore, to achieve  
78 practical applications of photocatalytic CO<sub>2</sub> reduction, it is essential to  
79 optimize photocatalytic settings and find out the most influential parameters.

80        Across a wide range of scientific fields, machine learning (ML) has  
81 become a potent tool that facilitates precise predictions directed by  
82 leveraging data-driven different algorithms, effective optimization, and a  
83 deeper understanding of complicated phenomena [15-17]. In recent times,  
84 many ML techniques, such as regression, neural network, and decision tree-  
85 based models, have often been used to design photocatalyst materials,  
86 optimize process parameters and predict photocatalytic reduction efficiency.  
87 For example, Zhang and Xu [18] employed a gaussian process regression  
88 (GPR) model to optimize the bandgaps of doped-TiO<sub>2</sub> photocatalysts

89 considering various structural and morphological attributes as input  
90 parameters. In another study, the partial least-squares (PLS) ML algorithm  
91 was used for the virtual design of rare-earth-metal-doped  $\text{TiO}_2$  photocatalyst  
92 materials [19]. Li and coworkers [20] combined ML and rigorous  
93 experimental investigation to discover photo-active molecular organic  
94 photocatalysts. In a similar type of study, Tao et al. [21] utilized different tree-  
95 based and neural network-based ML algorithms to discover new visible light-  
96 active perovskite photocatalyst materials. Recently, Yurova and colleagues  
97 [22] optimized the synthesis conditions to achieve optimal properties of g-  
98  $\text{C}_3\text{N}_4$  photocatalysts applying multiple tree-based ML algorithms. To forecast  
99 bandgap and photo-adsorption characteristics of emerging metal-organic  
100 frameworks (MOFs) materials, Jose and co-workers [23] employed diverse  
101 regression tree-based models. More straightforward and low-dimensional  
102 descriptors were found to be more effective in the low data regime than  
103 higher-dimensional descriptors, which were appropriate for handling large  
104 amounts of datasets. The scholarly community increasingly employs tree-  
105 based ML models to build photocatalyst materials because of their precision  
106 in predictions and capacity to handle substantial amounts of data.

107 Beyond the design and discovery of photocatalytic materials, applying  
108 different ML algorithms to predict photocatalytic efficiency is well supported  
109 by extensive literature. Researchers are increasingly applying machine  
110 learning techniques to improve the accuracy of predicting photocatalytic  
111 pollutants removal, detection, and energy production. For instance, Liu and  
112 coworkers [24] applied four ML models including linear regression (LR),  
113 random forest (RF), XGBoost (XGB) and LightGBM (LGBM) to predict the  
114 degradation efficiency of different organic dyes over doped- $\text{TiO}_2$   
115 photocatalysts. The LGBM model with the best credibility ( $R^2 = 0.898$ )  
116 suggested irradiation time as the most crucial parameter to enhance  
117 degradation efficiency. Most recently, PC removal efficiency of methylene  
118 blue (MB) dye was optimized using ten diverse tree-based ML algorithms over

119 synthesized  $\text{CuWO}_4@ \text{TiO}_2$  composite [25]. Among all utilized models, they  
120 reported HistGradientBoosting (HGB) as the best-suited model with  $R^2$  value  
121 of 0.992 at testing stage to achieve 98.99 % prediction efficiency of MB. To  
122 predict the photocatalytic (PC) degradation efficiency of tetracycline (TC)  
123 antibiotics in wastewater using metal-organic framework (MOF)-based  
124 photocatalysts, Salahshoori et al. [26] implemented an ensemble of ML  
125 models. Among these, the hybrid GAPSO-LSSVM model demonstrated  
126 superior accuracy and reliability in forecasting TC photodegradation  
127 performance. In a related study, Javed et al. [27] utilized a comprehensive  
128 dataset derived from  $\text{TiO}_2$ -based photocatalysts to predict the photocatalytic  
129 degradation activity of airborne pollutants, evaluating a total of 13 distinct  
130 ML algorithms for this purpose. The XGBoost (XGB) model outperformed  
131 other models as robust and effective in predicting degradation efficiency. The  
132 dual-functional performance including detection and degradation of organic  
133 pollutants of Ag nanoparticles (NPs)-decorated ZnO nanorods (NRs) coated  
134 by  $\text{SiO}_2$  nanofibers (NFs) was predicted to be using different ML-assisted  
135 algorithms [28]. The integrated k-nearest neighbors (KNN) model  
136 demonstrated 90.8 % accuracy in quantitative categorization and 92.3 %  
137 precision in qualitative detection. To design the synthesis of carbon quantum  
138 dots (CQDs) photocatalysts and predict their pollutant detection  
139 performance, Kakhki and Mohammadpoor [29] utilized multiple regression  
140 algorithms. The most favorable values of performance indicator features  
141 were found in the XGB model.

142 Compared to the PC degradation rate and the prediction of pollutants in  
143 contaminated sources, the application of ML algorithm techniques to forecast  
144 photocatalytic energy production is insufficient. Most studies focused on  
145 using secondary data to predict the energy generation efficiency of PCs. Tao  
146 et al. [21] collected 160 perovskite-based visible photocatalysts data points  
147 from 43 experimental literature to predict  $\text{H}_2$  evolution rate (HER). They  
148 employed four distinct ML algorithms namely support vector regression

149 (SVR), gradient boosting regression (GBR), backpropagation artificial neural  
150 network (BPANN), and random forest (RF). The BPANN model demonstrated  
151 the highest  $R^2$  (0.9740 for the testing data. Recently, Haghshenas and his  
152 team [30] utilized 971 secondary data points to forecast the PC HER using  
153 modified-TiO<sub>2</sub> photocatalysts. Among the five reaction conditions studied,  
154 photon flux emerged as the influential factor to control HER. Saadetnejad  
155 and colleagues [31] utilized decision trees (DT) and random forest (RF) to  
156 predict the PC-CO<sub>2</sub>R rate. They collected 281 liquid-phase and 268 gas-phase  
157 data points from 80 experimental literature and found that the DT ML  
158 algorithm was robust in forecasting CO<sub>2</sub> reduction efficiency with 80 %  
159 accuracy. While the RF model showed superior performance in predicting the  
160 liquid-phase CO<sub>2</sub> reduction rate with 79 % precision. Similar findings were  
161 also observed to predict PC-CO<sub>2</sub>R over MOFs-based photocatalysts [32]. In a  
162 separate study, Liu and coworkers [15] applied an RF model with various  
163 pretreatment strategies to prepare the surfaces of TiO<sub>2</sub> for predicting the  
164 liquid-phase CO<sub>2</sub> reduction through the photocatalytic process. The light  
165 irradiation method demonstrated the highest effectiveness in enhancing the  
166 HCOOH production rate compared to all other pretreatment strategies  
167 evaluated. However, there are very limited ML studies predicting  
168 photocatalytic CO<sub>2</sub> reduction efficiency, especially for the gas-phase, which  
169 is still at a rudimentary stage level. The intricate system of interdependent  
170 variables that drive the gas-phase PC-CO<sub>2</sub>R process has an impact on several  
171 performance indicators. Different machine learning algorithms can handle  
172 large, complex and uncertain data sets to investigate comprehensive implicit  
173 relationships among various parameters, apply relevant details from the  
174 experimental data points, and produce reliable forecasting models through  
175 data extraction and evaluation.

176 This work is a groundbreaking addition to the gas-phase PC CO<sub>2</sub> reduction  
177 and production of CH<sub>4</sub> and CO products, and optimizes the reaction  
178 conditions to get maximized CO<sub>2</sub> conversion by applying the ML approach  
179 over g-C<sub>3</sub>N<sub>4</sub>/TNTAs composite. **Despite the growing body of literature on g-**

180  $C_3N_4$ /TNTAs composites, most studies focus on pollutant degradation, where  
181 mass transfer limitations, solvent effects, and scavenger dominate  
182 photocatalytic efficiency. The gas-phase photocatalytic  $CO_2$  reduction  
183 remains significantly underexplored for this heterostructure by using the ML-  
184 driven optimization framework, which representing a key knowledge gap this  
185 work tries to fill. A total of ten tree-based ML algorithms were employed with  
186 precisely optimized hyperparameters to confirm the robust predictions. Five  
187 significant factors were taken into consideration as input parameters to  
188 forecast the rates of  $CH_4$  and  $CO$  production: catalyst exposed surface area,  
189 initial concentration of  $CO_2$ , feed ( $CO_2 + H_2O$ ) pressure, light power and  
190 irradiation time. The features importance and robustness of the best model  
191 were assessed by using the SHapley Additive exPlanations (SHAP) and  
192 Gaussian noise technique. The determination of optimal input parameters by  
193 differential evolution (DE) optimization considering real-life scenarios and  
194 experimental validation provides insightful information for the practical  
195 implementation of photocatalytic  $CO_2$  reduction.

196

## 197 **2. Materials and methods**

### 198 2.1. Synthesis and characterization of g- $C_3N_4$ /TNTAs photocatalyst

199 The two-step anodization method was used to synthesize the  $TiO_2$   
200 nanotube arrays (TNTAs) [11]. The detailed synthesis procedure along with  
201 the required chemicals and materials is described in **Texts S1** and **S2**. The  
202 overall procedure employed to synthesize TNTAs photocatalysts is shown in  
203 **Fig. S1a**. The g- $C_3N_4$  nanosheets was prepared from melamine powder using  
204 the calcination technique and used as a co-catalyst with TNTAs [33]. The g-  
205  $C_3N_4$ /TNTAs composite was constructed by a facile dispersion method, as  
206 mentioned in a previous study [34]. In this process, pure TNTAs foils were  
207 submerged in 250 mL beakers containing a separately prepared g- $C_3N_4$   
208 methanol solution (0.1 g of g- $C_3N_4$  dispersed in 50 mL methanol), followed by  
209 sonication for 15 minutes to ensure uniform deposition and subsequent  
210 drying at 100 °C for 12 hours. The g- $C_3N_4$  loading was standardized across

211 all samples by depositing 0.1 g of g-C<sub>3</sub>N<sub>4</sub> onto 4 cm<sup>2</sup> of TNTAs, yielding a  
212 nominal surface loading of 25 mg/cm<sup>2</sup>. Although the exact weight percentage  
213 of g-C<sub>3</sub>N<sub>4</sub> was not measured due to the absence of pre- and post-deposition  
214 mass measurements, an estimated value of ~18 wt.% was derived based on  
215 Ti foil thickness of 0.25 mm. The physical, chemical and optical properties of  
216 the synthesized photocatalysts were examined by Field Emission Scanning  
217 Electron Microscopy (FESEM), X-ray diffraction (XRD), Photoluminescence  
218 (PL) and Ultraviolet-visible Diffuse Reflectance Spectroscopy (UV-Vis DRS).  
219 The detailed specifications of the characterization tools are provided in **Text**  
220 **S3**.

## 221 2.2. Photocatalytic experiments

222 The photocatalytic (PC) CO<sub>2</sub> reduction performance of the synthesized  
223 materials was systematically evaluated in a gas-solid photoreactor (**Fig.**  
224 **S1b**). Specifically, the g-C<sub>3</sub>N<sub>4</sub>/TNTAs heterostructured photocatalysts were  
225 assessed under a range of operational parameters to determine their  
226 influence on CO<sub>2</sub> conversion efficiency. These parameters included  
227 photocatalyst exposed surface area (4, 8, 12, and 16 cm<sup>2</sup>), initial CO<sub>2</sub>  
228 concentration (10, 30, 50, and 100 vol%), total feed pressure of the CO<sub>2</sub> +  
229 H<sub>2</sub>O vapor mixture (100, 200, 300, and 400 mbar), incident light intensity  
230 corresponding to lamp powers of 100, 200, 300, and 400 W, and irradiation  
231 duration (1, 2, 3, and 4 h). To simulate realistic gas compositions, varying  
232 CO<sub>2</sub> concentrations were balanced with inert (Ar, N<sub>2</sub>) and oxidizing (O<sub>2</sub>)  
233 gases. Irradiation was provided by a 500 W adjustable xenon (Xe) arc lamp  
234 equipped with a bandpass filter to deliver a wavelength range of 365–720 nm,  
235 simulating visible–near-UV solar irradiation. The light source was positioned  
236 directly above the reactor to ensure uniform illumination. Prior to each  
237 experiment, the reactor was purged with high-purity N<sub>2</sub> for 30 minutes to  
238 eliminate residual atmospheric gases and establish an inert baseline  
239 environment. During the photocatalytic runs, the reactor chamber was  
240 maintained at a controlled temperature of 298–303 K via a closed-loop water

241 cooling system to minimize thermal effects on reaction kinetics. A series of  
242 control experiments were also performed to confirm that the gaseous  
243 products is mainly contributed by the photocatalytic reduction of CO<sub>2</sub> rather  
244 than through the photodecomposition of organic residues on the surface of  
245 photocatalysts. The control experiments were conducted under three  
246 conditions: (i) in the absence of light but with photocatalyst and CO<sub>2</sub>/H<sub>2</sub>O  
247 flow, (ii) without photocatalyst but under light irradiation with CO<sub>2</sub>/H<sub>2</sub>O flow,  
248 and (iii) without H<sub>2</sub>O vapour but with photocatalyst, CO<sub>2</sub> flow, and light  
249 irradiation. At predetermined time intervals, gaseous products generated  
250 from the photocatalytic reduction were extracted from the reactor outlet  
251 using a calibrated suction pump and stored in pre-evacuated gas sampling  
252 bags for subsequent analysis. Quantitative determination of the gaseous  
253 products was performed using a Shimadzu GC-2014 gas chromatograph (GC)  
254 equipped with both a flame ionization detector (FID) and a thermal  
255 conductivity detector (TCD), enabling simultaneous detection of  
256 hydrocarbons and permanent gases. The primary reduction products  
257 identified were methane (CH<sub>4</sub>) and carbon monoxide (CO), with trace  
258 amounts of hydrogen (H<sub>2</sub>) occasionally observed. Product concentrations  
259 were quantified in micromoles (μmol) by correlating peak areas from the  
260 chromatograms with calibration curves generated from standard gas  
261 mixtures of known composition. Finally, the product formation rate (yield  
262 rate) was calculated using Eq. (1), providing a standardised metric for  
263 comparing photocatalytic activity across different experimental conditions.

264

$$\text{Rate of product yield } (\mu\text{mol}/\text{cm}^2) = \frac{\text{Amount of products in } \mu\text{mol}}{\text{Exposed surface area of photocatalysts } (\text{cm}^2)} \quad (1)$$

### 265 2.3. Data collection and analysis

266 Data is vital for constructing any machine learning models, because the  
267 size, quality, and diversity of datasets greatly affect the accuracy and  
268 reliability with which models can forecast performance [35]. This work is

269 based on two broad datasets, each with 1024 reproducible experimental data  
270 points, on predicting CH<sub>4</sub> and CO production efficiencies using g-C<sub>3</sub>N<sub>4</sub>/TNTAs  
271 composite as photocatalysts. These two datasets were developed very  
272 carefully by controlled experimental setup and thus are consistent and  
273 reliable. The five most crucial above-mentioned photocatalytic factors were  
274 employed to investigate the product yield rate during gas-phase PC-CO<sub>2</sub>R.  
275 The experimental datasets were preprocessed to address inconsistencies,  
276 normalize the variables, and prepare the dataset for machine learning  
277 algorithms. The normalization of the data was conducted to reduce the  
278 overfitting and simplify complex computations according to Eq. (2) [36].

$$\text{Normalized value } X_{\text{norm}} = \frac{X_i - X_{\text{min}}}{X_{\text{max}} - X_{\text{min}}} \quad (2)$$

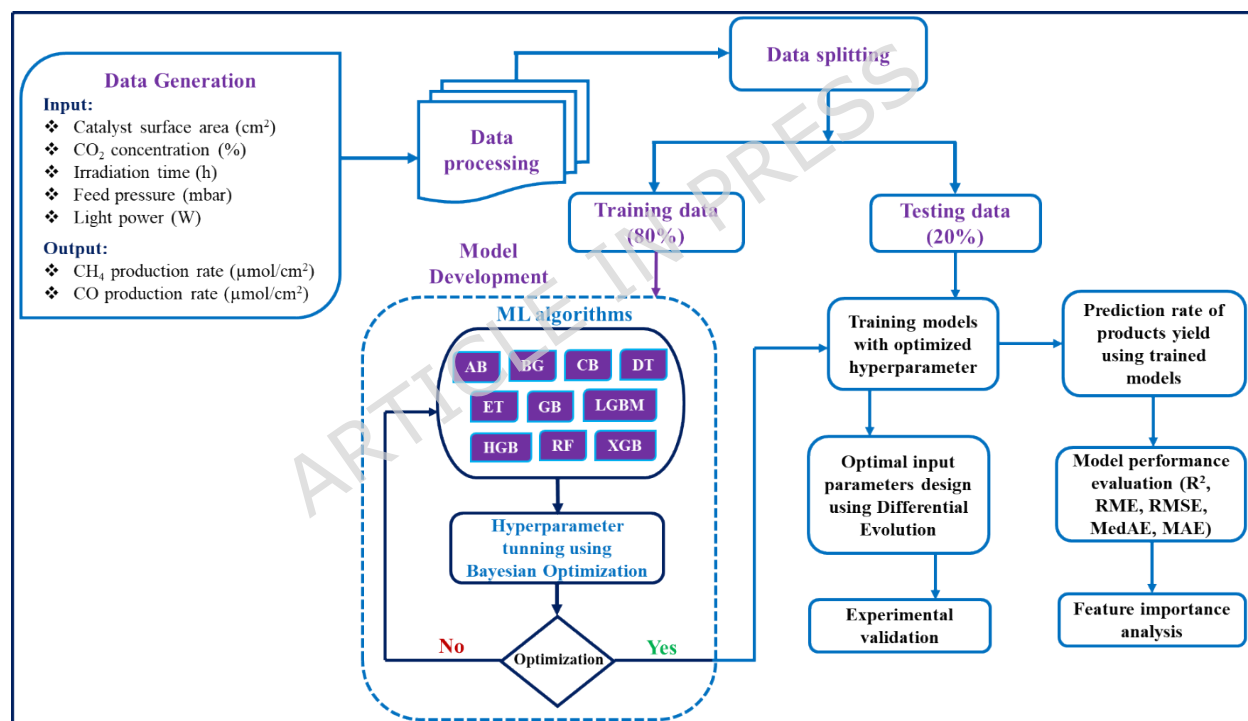
279 In the above equation,  $X_i$  represents any data,  $X_{\text{min}}$  and  $X_{\text{max}}$  correspond  
280 to minimum and maximum values.

#### 281 2.4. Machine learning models

282 In the present study, ten distinct tree-based machine learning (ML)  
283 algorithms were employed to predict the photocatalytic CO<sub>2</sub> reduction  
284 performance of the synthesized materials. These models encompassed  
285 AdaBoost (AB), Bagging, CatBoost (CB), Decision Tree (DT), Extra Trees (ET),  
286 Gradient Boosting (GB), HistGradientBoosting (HGB), LightGBM (LGB),  
287 Random Forest (RF), and Extreme Gradient Boosting (XGB). All ML  
288 implementations were carried out using the Scikit-learn library within the  
289 Python programming environment, executed on the Google Colab  
290 computational platform [37]. A comprehensive schematic illustrating the  
291 overall ML modeling workflow is provided in **Fig. 1**, while detailed  
292 descriptions of each algorithm's theoretical underpinnings and  
293 implementation specifics are elaborated in Supplementary **Text S4**. The  
294 dataset was partitioned into training and testing subsets, with approximately  
295 80% of the data allocated for model training and the remaining 20% reserved  
296 for testing performance evaluation. This stratified split ensured a robust

297 assessment of each model's generalization capability on previously unseen  
 298 data. Model performance was rigorously evaluated using a suite of  
 299 quantitative metrics, as summarized in **Table 1**. These metrics were  
 300 formulated based on standard regression evaluation criteria, where  $y_i$   
 301 denotes the experimentally measured (actual) value,  $\hat{y}_i$  represents the  
 302 corresponding model-predicted (estimated) value,  $\bar{y}$  signifies the mean of the  
 303 observed values, and  $n$  corresponds to the total number of data points in the  
 304 test set. This systematic approach facilitated a comparative analysis of  
 305 predictive accuracy, robustness, and reliability across all ten tree-based ML  
 306 models.

307



308

309 **Fig. 1.** The illustration of the comprehensive process involved in machine  
 310 learning (ML) modeling.

311

312

313

314

315

316

317 **Table 1.** Evaluation matrices to evaluate the performance of given ML  
318 models.

<b>Evaluati on Metric</b>	<b>Description</b>	<b>Formula</b>	<b>Best Result</b>
R <sup>2</sup>	Coefficient of determination	$R^2 = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2}$	1 (perfect prediction)
MSE	Mean squared error	$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$	0 (perfect prediction)
RMSE	Root mean squared error	$MSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2}$	0 (perfect prediction)
MAE	Mean absolute error	$MAE = \frac{1}{n} \sum_{i=1}^n  y_i - \hat{y}_i $	0 (perfect prediction)
MedAE	Median Absolute Error	$MedAE = \text{median}( y_i - \hat{y}_i )$	0 (perfect prediction)

319

## 320 2.5. Hyperparameter tuning and models interpretation

321 The hyperparameter setting in machine learning models has a direct and  
322 considerable impact on the model's prediction performance [38]. Thus,  
323 hyperparameter adjustment of utilized models is an essential step toward  
324 ensuring model resilience and prediction accuracy. Bayesian optimization  
325 was applied in the tuning of each model's hyperparameters using efficient  
326 probabilistic methods of searching in hyperparameter space, such as the  
327 Gaussian process (GP). This results in faster convergence, reducing  
328 computational costs compared to conventional search methods [39]. The  
329 optimal hyperparameter values for all 10 models of CH<sub>4</sub> and CO production  
330 rates prediction were computed, and the resulting values are presented in

331 **Tables S1 and S2.** Subsequently, all the Bayesian optimization models were  
332 trained in the training and evaluated using the testing dataset.

333 When predicting a target variable, the analysis of feature importance is a  
334 study of uncertainty that interprets the model performance by determining  
335 the relative value of each feature in a dataset. This analysis ensured that the  
336 selected features effectively captured all the necessary elements influencing  
337 photocatalytic efficiency and enhanced model reliability [27,40]. The relative  
338 importance of all the input parameters on photocatalytic CO<sub>2</sub> reduction were  
339 also determined using feature importance analysis. The most widely used  
340 SHapley Additive exPlanations (SHAP) analysis was also performed to  
341 examine the impact of input features on the predictive performance of the  
342 top-performing models. The Differential Evolution (DE) algorithm was used  
343 to optimize the input parameters to get maximum production rates of CH<sub>4</sub>  
344 and CO using the predictive values of outperformed models. This approach  
345 has been instructive not only for prediction efficiency but also for improving  
346 experimental settings to attain real-life applications of photocatalytic CO<sub>2</sub>  
347 reduction. Experimental validation was performed after getting the optimal  
348 conditions for input features. The effectiveness of the top-performing model  
349 was assessed using a Gaussian noise method [41].

### 350 **3. Results and discussion**

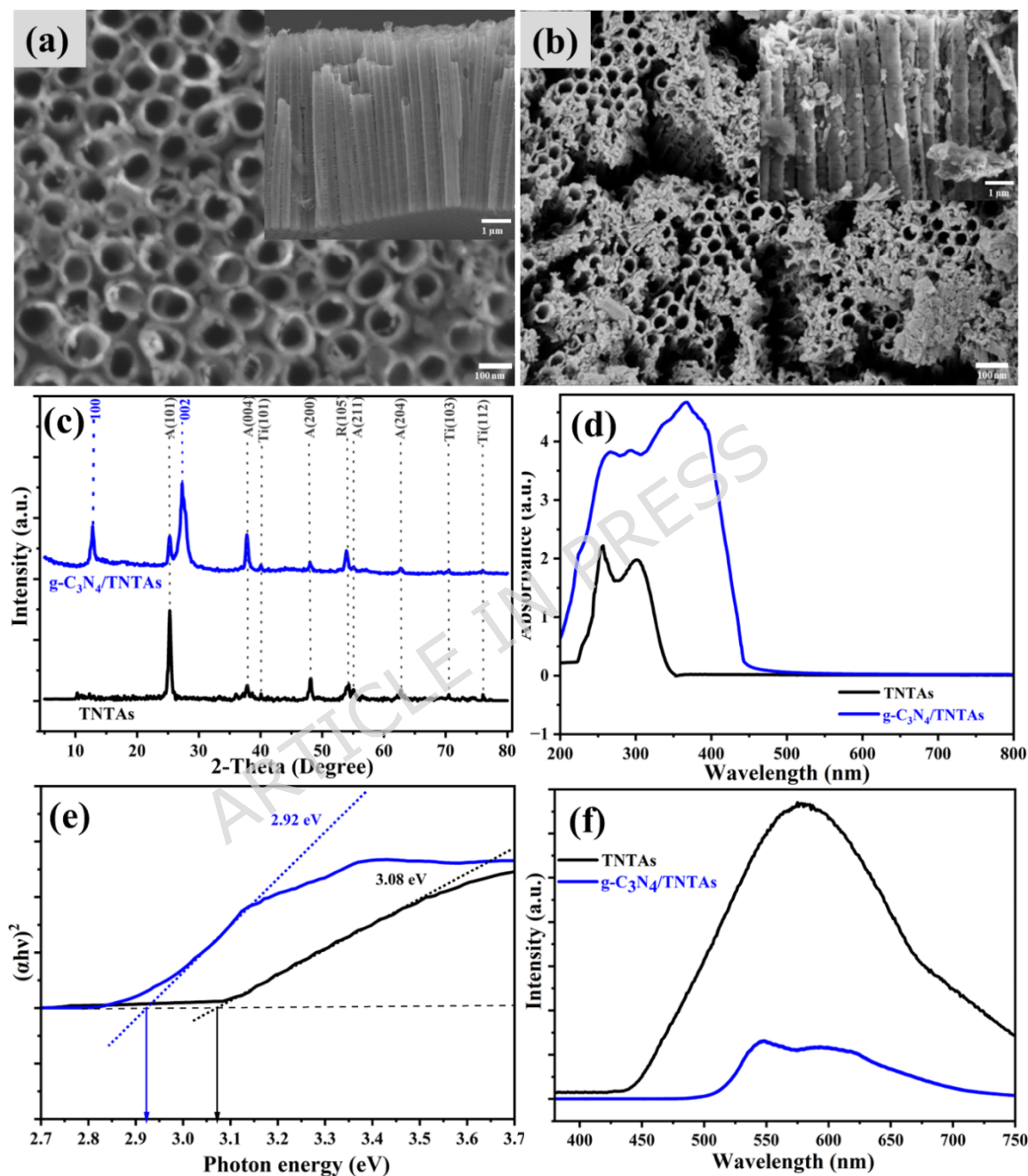
#### 351 **3.1. Physicochemical analysis of g-C<sub>3</sub>N<sub>4</sub>/TNTAs**

352 The morphological characteristics of both pristine TiO<sub>2</sub> nanotube arrays  
353 (TNTAs) and the g-C<sub>3</sub>N<sub>4</sub>TNTAs heterostructured photocatalysts were  
354 investigated using FESEM. As shown in **Fig. 2a**, the TNTAs exhibited a  
355 vertically aligned and highly ordered architecture, with an average inner  
356 diameter of  $102.57 \pm 12.61$  nm and a length of  $5327 \pm 677$  nm. Such  
357 dimensional enlargement of the nanotubular structure contributes to an  
358 expanded specific surface area, which is conducive to enhanced adsorption  
359 of reactants and improved photocatalytic efficiency [42,43]. FESEM imaging

360 of the g-C<sub>3</sub>N<sub>4</sub>/TNTAs composite (**Fig. 2b**) revealed that ultrathin g-C<sub>3</sub>N<sub>4</sub>  
361 nanosheets (NSs) were uniformly and robustly anchored onto the external  
362 and internal surfaces of the TNTAs, without inducing any noticeable  
363 structural distortion. This preservation of the underlying nanotubular  
364 morphology confirms the successful and conformal deposition of g-C<sub>3</sub>N<sub>4</sub> onto  
365 the TNTAs framework. Further structural validation was provided by X-ray  
366 diffraction (XRD) analysis (**Fig. 2c**), which displayed the characteristic  
367 diffraction peaks of g-C<sub>3</sub>N<sub>4</sub> at 2θ values of 12.88° and 27.64°, corresponding  
368 to the (100) and (002) crystallographic planes, respectively. These peaks  
369 were clearly discernible in the g-C<sub>3</sub>N<sub>4</sub>/TNTAs composite spectrum, while the  
370 anatase (101) and rutile (110) reflections of TiO<sub>2</sub>, originating from the TNTAs  
371 substrate remained unaltered, indicating that the integration of g-C<sub>3</sub>N<sub>4</sub> did  
372 not compromise the crystalline integrity of the TiO<sub>2</sub> nanotubes [44,45].

373 The optical properties of the synthesized photocatalysts were assessed  
374 via UV-Vis diffuse reflectance spectroscopy (DRS). As illustrated in **Fig. 2d**,  
375 the incorporation of g-C<sub>3</sub>N<sub>4</sub> nanosheets induced a marked redshift in the  
376 absorption edge of TNTAs, extending light absorption into the visible region  
377 (>400 nm). The corresponding bandgap energies were derived from the DRS  
378 data using the methodology detailed in Supplementary **Text S5**, employing  
379 Tauc plot analysis. As shown in **Fig. 2e**, the bandgap of pristine TNTAs (3.08  
380 eV) was reduced to 2.92 eV upon hybridization with g-C<sub>3</sub>N<sub>4</sub>. This narrowing  
381 of the bandgap enhances the material's ability to harness visible light,  
382 thereby promoting more efficient generation of electron-hole pairs and  
383 accelerating photocatalytic reaction kinetics [46,47]. Photoluminescence  
384 (PL) spectroscopy was further employed to probe the dynamics of charge  
385 carrier recombination. Among all modified samples, the g-C<sub>3</sub>N<sub>4</sub>/TNTAs  
386 heterostructure exhibited the lowest PL emission intensity, signifying  
387 effective suppression of photogenerated electron-hole recombination. This  
388 behavior is attributed to the formation of a well-defined heterojunction at the  
389 g-C<sub>3</sub>N<sub>4</sub>-TNTAs interface, which facilitates spatial separation of charge

390 carriers under photoexcitation. Such interfacial engineering has been widely  
 391 reported to enhance charge transfer efficiency and prolong carrier lifetimes,  
 392 thereby significantly boosting overall photocatalytic performance [48-50].



393  
 394 **Fig. 2.** Characteristics of the synthesized photocatalysts (a, b) FESEM  
 395 images of TNTAs and g-C<sub>3</sub>N<sub>4</sub>/TNTAs; (c) XRD; (d) UV-DRS; (e) Tauc-plot; (f)  
 396 PL spectra.

## 397 3.2. Descriptive statistics

398 In the present study, a comprehensive series of experiments was  
399 conducted to evaluate the photocatalytic efficacy of the synthesized g-  
400  $C_3N_4$ /TNTAs composite in converting  $CO_2$  into value-added chemical  
401 products, specifically methane ( $CH_4$ ) and carbon monoxide (CO). **The pristine**  
402 **TNTAs has been modified using g- $C_3N_4$  to improve the PC  $CO_2$  reduction**  
403 **activity. As depicted in Fig. S2, the rate of  $CH_4$  and CO production improved**  
404 **notably after the modification of TNTAs compared to pure TNTAs under**  
405 **identical experimental conditions.** The overall experiments were carried out  
406 under systematically varied operational and photoreactor conditions, as  
407 detailed in **Table 2**. To facilitate a rigorous statistical interpretation of the  
408 experimental outcomes, a multivariate descriptive analysis was performed  
409 based on seven key parameters: catalyst surface area, initial  $CO_2$   
410 concentration, feed pressure ( $CO_2 + H_2O$  vapor), incident light power,  
411 irradiation duration, and the production rates of  $CH_4$  and CO.

412 Descriptive statistics were computed to characterize the dataset and  
413 elucidate the typical experimental conditions. The mean values represent the  
414 central tendency of each variable for example, a mean catalyst **exposed**  
415 surface area of  $10 \text{ cm}^2$ ,  $CO_2$  concentration of 47 vol%, feed pressure of 250  
416 mbar, light power of 250 W, irradiation time of 2.5 h,  $CH_4$  production rate of  
417  $6.52 \text{ } \mu\text{mol}/\text{cm}^2$  and CO production rate of  $75.95 \text{ } \mu\text{mol}/\text{cm}^2$ . These averages  
418 provide a benchmark for representative operating conditions within the  
419 experimental design. The standard deviation (SD) was calculated to quantify  
420 the dispersion or variability of each parameter around its mean, thereby  
421 indicating the degree of data spread and experimental consistency.  
422 Additionally, the range defined by the minimum and maximum observed  
423 values for each variable delineates the boundaries of the experimental  
424 domain and informs the spacing and coverage of the sampled conditions.

425 To further assess the distributional characteristics of the data, percentile  
426 values (25th, 50th, and 75th) were determined. These quartiles partition the

427 dataset into four equal segments, enabling the identification of potential  
 428 skewness, clustering, or the presence of outliers that may influence model  
 429 performance or interpretation. Skewness was employed to evaluate the  
 430 symmetry of each variable's distribution; values near zero suggest  
 431 approximate symmetry, whereas significant positive or negative skewness  
 432 indicates a tail extending toward higher or lower values, respectively.  
 433 Concurrently, kurtosis was used to describe the tailedness and peakedness  
 434 of the distribution relative to a normal (Gaussian) distribution; negative  
 435 kurtosis implies a flatter, more uniformly distributed profile with lighter tails.  
 436 Collectively, these statistical descriptors encompassing measures of central  
 437 tendency (mean, median), dispersion (standard deviation, range), and shape  
 438 (skewness, kurtosis) offer a holistic characterization of the experimental  
 439 dataset. This robust statistical foundation not only enhances the  
 440 interpretability of the photocatalytic performance trends but also supports  
 441 subsequent modeling, optimization, and generalization of the CO<sub>2</sub>  
 442 photoreduction process under diverse operational regimes.

443  
 444 **Table 2** Descriptive statistics of the input and output data utilized in this  
 445 research.

Statistic	Catalyst surface area (cm <sup>2</sup> )	Initial concentration of CO <sub>2</sub> (%)	Feed pressure (mbar)	Light power (W)	Irradiation time (h)	CH <sub>4</sub> production (μmol/cm <sup>2</sup> )	CO production (μmol/cm <sup>2</sup> )
<b>Mean</b>	10	47	250	250	2.5	6.52	75.95
<b>Standard deviation</b>	4.47	33.46	111.86	111.86	1.11	2.39	16.51
<b>Minimum</b>	4	10	100	100	1	0.52	34.21
<b>25 %</b>	7	25	175	175	1.75	4.72	63.99

<b>50 %</b>	10	40	250	250	2.5	6.66	76.10
<b>75 %</b>	13	62	325	325	3.25	8.32	87.27
<b>Maximum</b>	16	100	400	400	4	12.12	118.27
<b>Skewness</b>	0	0.58	0	0	0	-0.13	-0.13
<b>Kurtosis</b>	-1.36	-1.07	-1.36	-1.36	-1.36	-0.74	-0.48

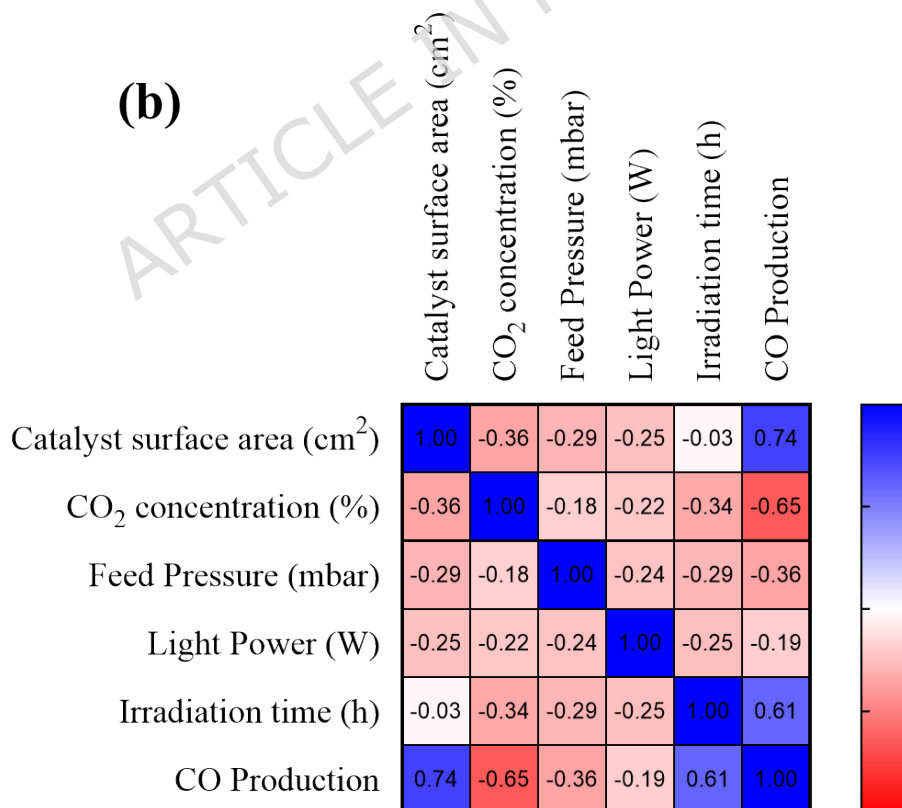
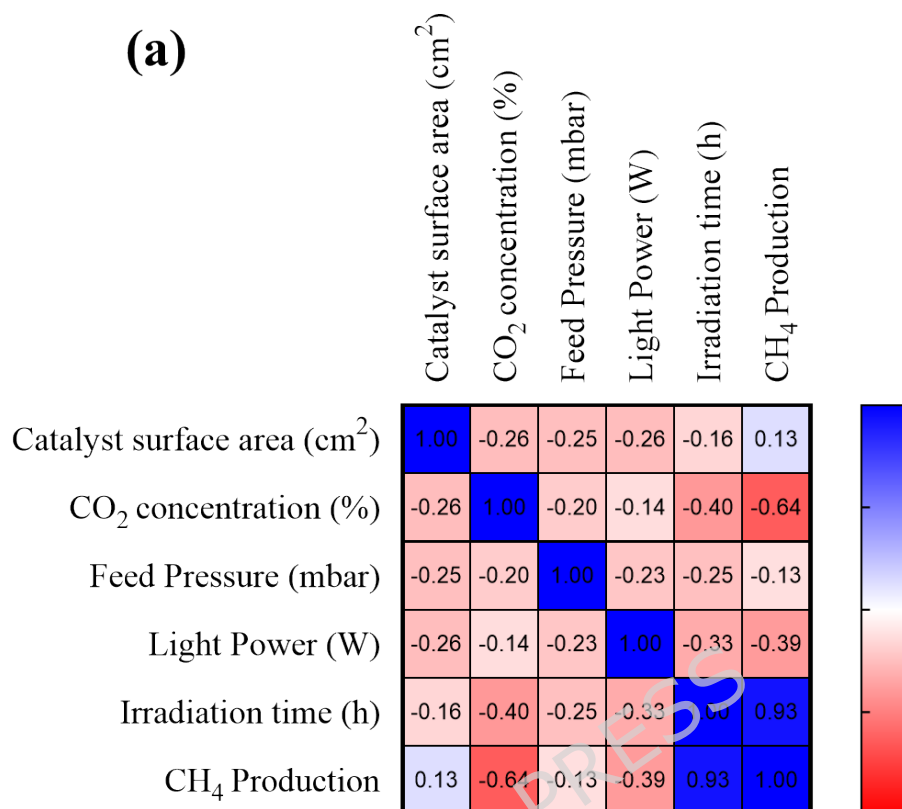
446

447 To elucidate the interdependencies between the experimental input  
 448 variables and the photocatalytic response metrics, a Pearson correlation  
 449 analysis was conducted. The resulting correlation matrix is visualized as a  
 450 heatmap in **Fig. 3**, which illustrates the pairwise relationships among five  
 451 input parameters: catalyst surface area, initial CO<sub>2</sub> concentration, feed  
 452 pressure, light power, and irradiation time, as well as the two primary output  
 453 variables: CH<sub>4</sub> and CO production rates. In this heatmap, the intensity and  
 454 hue of the color encoding convey both the magnitude and direction of the  
 455 linear associations. Specifically, darker shades denote stronger correlations,  
 456 while lighter tones indicate weaker relationships. Blue hues signify positive  
 457 correlations (i.e., as one variable increases, the other tends to increase),  
 458 whereas brown or reddish tones represent negative correlations (i.e., an  
 459 increase in one variable corresponds to a decrease in the other), with  
 460 reference to photocatalytic conversion efficiency. Notably, the analysis  
 461 revealed minimal intercorrelation among the input variables themselves,  
 462 suggesting that these parameters are largely independent and non-collinear  
 463 a desirable characteristic for robust multivariate modeling. The most  
 464 pronounced correlation was observed between irradiation time and CH<sub>4</sub>  
 465 production rate, with a Pearson correlation coefficient of  $r = 0.93$  ( $p < 0.01$ )  
 466 (**Fig. 3a**), indicating a very strong positive linear relationship. This implies  
 467 that prolonged exposure to light irradiation significantly enhances methane  
 468 generation, likely due to extended photoexcitation duration facilitating

469 greater charge carrier utilization. A similarly positive, albeit moderate,  
470 correlation was identified between irradiation time and CO production rate  
471 ( $r = 0.64$ ,  $p < 0.01$ ) (**Fig. 3b**), underscoring the beneficial role of longer  
472 irradiation periods in promoting CO evolution as well.

473 In contrast, the initial  $\text{CO}_2$  concentration exhibited substantial negative  
474 correlations with both  $\text{CH}_4$  ( $r = -0.64$ ,  $p < 0.01$ ) and CO ( $r = -0.64$ ,  $p < 0.01$ )  
475 production rates. This inverse relationship suggests that higher  $\text{CO}_2$   
476 concentrations in the feed gas mixture may impede photocatalytic efficiency  
477 potentially due to mass transfer limitations, competitive adsorption effects,  
478 or reduced light penetration at elevated gas densities. Furthermore, catalyst  
479 exposed surface area demonstrated a significant positive correlation with CO  
480 production ( $r = 0.74$ ,  $p < 0.01$ ), highlighting the importance of accessible  
481 active sites in driving CO formation. In comparison, the remaining input  
482 parameters (e.g., feed pressure and light power) showed relatively weak or  
483 negligible correlations with the product yields, indicating a less dominant  
484 influence under the tested conditions. Overall, the correlation heatmap  
485 provides an intuitive and informative visual summary of the directional and  
486 quantitative relationships between operational parameters and  
487 photocatalytic performance. This insight not only aids in identifying key  
488 drivers of  $\text{CO}_2$  photoreduction efficiency but also informs the selection and  
489 prioritization of variables for subsequent predictive modeling and process  
490 optimization.

491



493 **Fig. 3.** Heatmap representation of the experimental dataset of (a) CH<sub>4</sub> and  
494 (b) CO production.

### 495 3.3. Performance evaluation of ML models

#### 496 3.3.1. Prediction of CH<sub>4</sub> production

497 Photocatalytic CO<sub>2</sub> reduction is an appealing route to sustainable  
498 mitigation of greenhouse gas emissions while instantaneously producing  
499 value-added products and fuels like CH<sub>4</sub> and CO. In this process, CO<sub>2</sub> is  
500 converted to CH<sub>4</sub>, a green fuel, and CO, an important industrial feedstock,  
501 through the action of photoactivated catalysts. Precise quantitation of CH<sub>4</sub>  
502 and CO production is paramount to evaluate the efficiency of the  
503 photocatalytic system and its environmental footprint. Tracking these  
504 products not only ensures the highest efficiency of the photocatalytic reaction  
505 but also restricts the formation of unwanted byproducts, paving the way  
506 towards a cleaner environment. By accurately determining CH<sub>4</sub> and CO yield,  
507 researchers can optimize reaction conditions, enhance selectivity, and  
508 support the development of eco-friendly technologies for renewable energy  
509 and carbon-neutral applications. In addition to experimental measurements,  
510 ML algorithms have emerged as an essential tool for predicting CH<sub>4</sub> and CO  
511 production in photocatalytic CO<sub>2</sub> reduction. By utilizing extensive datasets  
512 produced from experiments, ML models have been analyzed through various  
513 statistical performance metrics and visual comparison plots. The production  
514 of CH<sub>4</sub> via CO<sub>2</sub> photoreduction by the g-C<sub>3</sub>N<sub>4</sub>/TNTAs photocatalysts was  
515 predicted using ten tree-based ML algorithms: AB, BG, CB, DT, ET, GB, HGB,  
516 LGBM, RF, and XGB. To assess the prediction accuracy of all listed ML  
517 models, scatter and residual plots were presented between observed and  
518 predicted CH<sub>4</sub> and CO production on the training and testing datasets. Each  
519 scatter plot showed a strong concordance of experimental and predicted  
520 values, clustering around the 45-degree line for high accuracy (**Fig. 5**). In  
521 each relationship, the ideal regression line denoted by  $y = x$  is represented  
522 by red dotted lines, while the values of the training and testing data sets are

523 indicated by black and red circles, respectively. Points close to the red  
524 diagonal line indicate accurate predictions, while deviation from the line  
525 suggests prediction errors, which may indicate limitations in the model or  
526 insufficient data. The residual plots in **Fig. S3** show the error values between  
527 the expected and experimental datasets. The residuals were plotted along the  
528 x-axis in ascending order of their respective experimental values to observe  
529 the distribution patterns better. A model is deemed more dependable when  
530 its residual points are distributed around the zero line, indicating good model  
531 performance. In contrast, systematic patterns may suggest underfitting or  
532 overfitting [25,51,52]. Radar plots serve as an effective tool for summarizing  
533 complex datasets and guiding decision-making in multifactorial systems.  
534 Each axis of the radar plot represents a distinct parameter, normalized for  
535 comparison, while the enclosed area indicates overall performance, with  
536 larger areas signifying better outcomes. Deviations along specific axes reveal  
537 influential parameters, guiding targeted optimization.

538 The predictive performance of the ten employed machine learning (ML)  
539 algorithms in forecasting  $\text{CH}_4$  production during photocatalytic  $\text{CO}_2$   
540 reduction was rigorously evaluated using a comprehensive suite of regression  
541 metrics, including the coefficient of determination ( $R^2$ ), mean absolute error  
542 (MAE), mean squared error (MSE), root mean squared error (RMSE), and  
543 median absolute error (MedAE), as detailed in **Table S3**. To facilitate a  
544 holistic comparison, the distribution of these performance indicators across  
545 both training and testing datasets for all models was visualized using radar  
546 plots (**Fig. 4**).

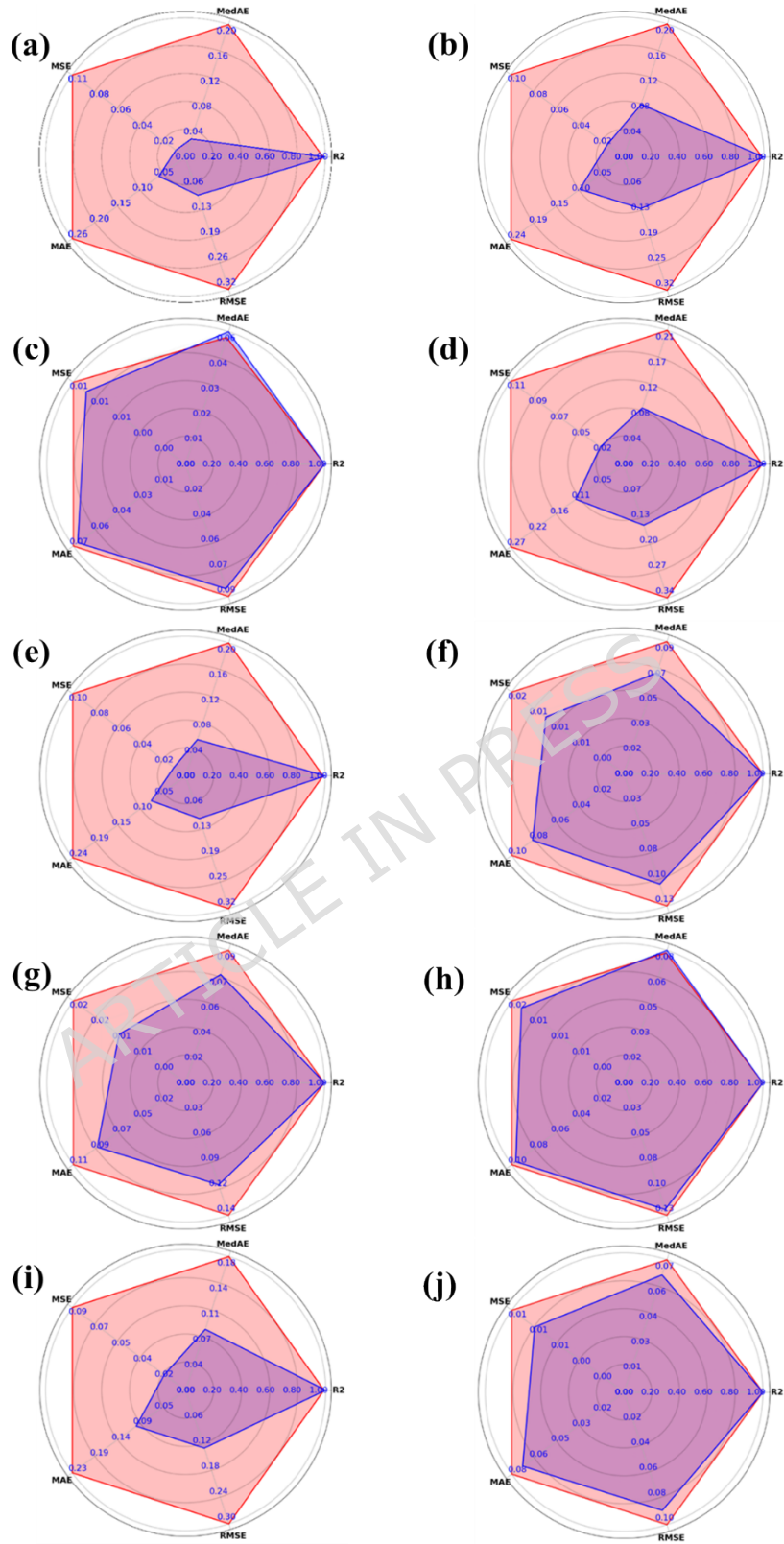
547 The  $R^2$  metric quantifies the proportion of variance in the observed  $\text{CH}_4$   
548 production rates that is explained by the model predictions; values  
549 approaching unity indicate an excellent fit and strong alignment between  
550 predicted and actual outcomes. The training phase yielded exceptionally high  
551  $R^2$  scores ranging from 0.9172 (AdaBoost) to 0.9887 (Extra Trees) reflecting  
552 effective hyperparameter tuning via Bayesian optimization and robust model

553 fitting. Specifically, the  $R^2$  values for AdaBoost (AB), Bagging (BG), CatBoost  
554 (CB), Decision Tree (DT), Extra Trees (ET), Gradient Boosting (GB),  
555 HistGradientBoosting (HGB), LightGBM (LGBM), Random Forest (RF), and  
556 XGBoost (XGB) were 0.9172, 0.9877, 0.9887, 0.9784, 0.9864, 0.9883, 0.9823,  
557 0.9772, 0.9769, and 0.9786, respectively. Complementing  $R^2$ , error-based  
558 metrics provide nuanced insights into prediction accuracy. MSE emphasizes  
559 larger errors by squaring deviations between predicted and actual values,  
560 thereby penalizing substantial outliers more severely. In contrast, MAE offers  
561 a linear measure of average absolute prediction errors, treating all deviations  
562 uniformly, while MedAE-based on the median of absolute errors, is more  
563 robust to extreme values and better reflects typical prediction performance  
564 in the presence of outliers. Lower values across MSE, MAE, and MedAE,  
565 along with reduced RMSE (the square root of MSE), collectively signify  
566 higher predictive fidelity. The models exhibited notably low MAE values  
567 during training: 0.5747 (AB), 0.0871 (BG), 0.0667 (CB), 0.0525 (DT), 0.1117  
568 (ET), 0.0762 (GB), 0.1646 (HGB), 0.2731 (LGBM), 0.1033 (RF), and 0.0701  
569 (XGB), underscoring their capacity to closely approximate true  $\text{CH}_4$  yields.

570 Scatter plots in **Fig. 5** further illustrate model performance by comparing  
571 predicted versus actual  $\text{CH}_4$  production rates. Points closely aligned with the  
572 ideal diagonal (black dashed line) denote high predictive accuracy. Among all  
573 models, CatBoost (**Fig. 5c**), Gradient Boosting (**Fig. 5f**), and XGBoost (**Fig.**  
574 **5j**) demonstrated the tightest clustering around this reference line, indicating  
575 superior consistency and minimal deviation across both training and testing  
576 phases. However, residual analysis depicted in supplementary residual plots  
577 (**Fig. S3**) revealed critical differences in model behavior. Residuals, defined  
578 as the difference between observed and predicted values, span a range of -2  
579 to +2  $\mu\text{mol}/\text{cm}^2$ . A pronounced dispersion of residuals, particularly at higher  
580  $\text{CH}_4$  production levels, suggests increased prediction uncertainty for elevated  
581  $\text{CO}_2$  conversion rates. Notably, the LightGBM model exhibited residuals  
582 tightly clustered near zero but failed to capture the full spectrum of data

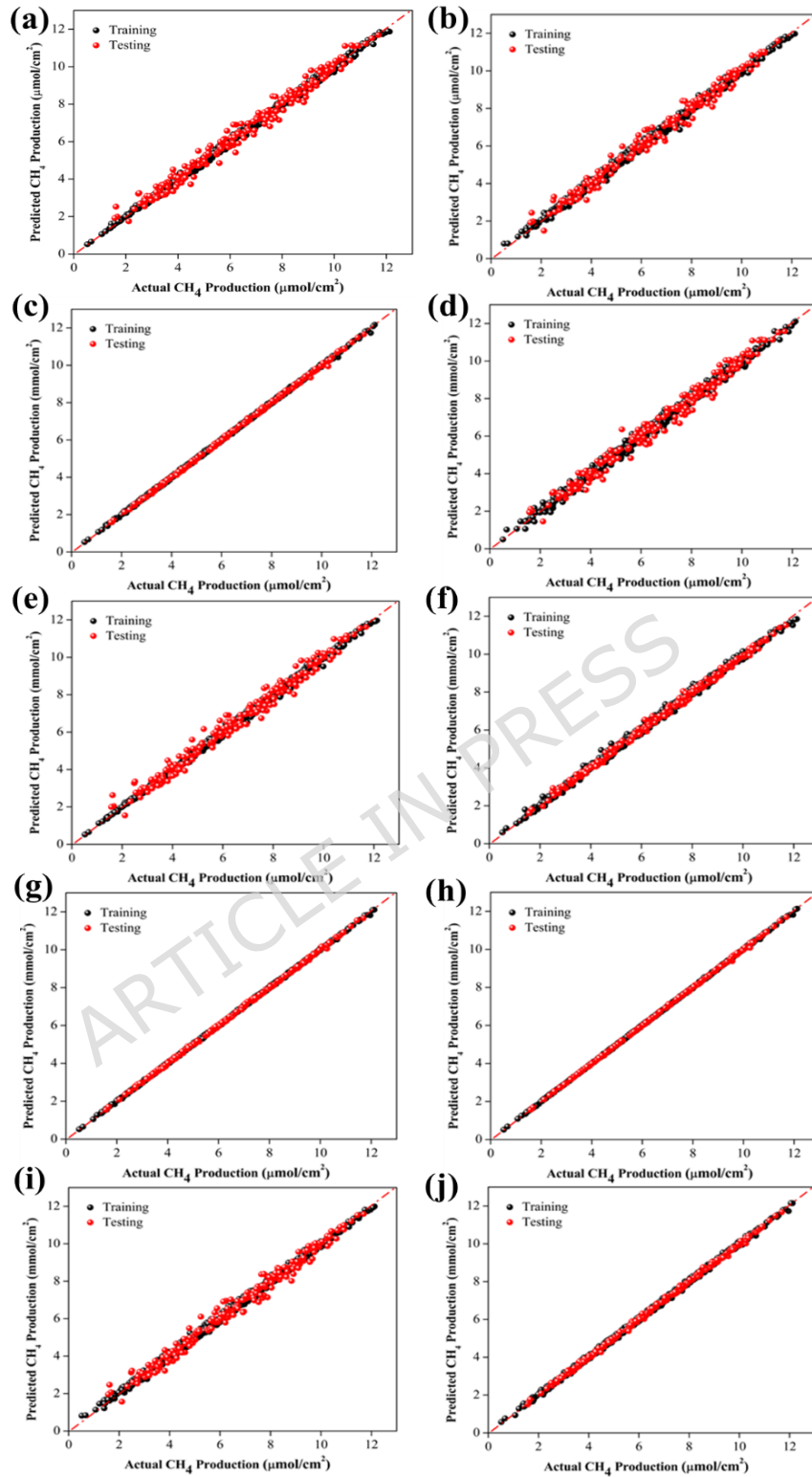
583 variability, a pattern indicative of overfitting where the model memorizes  
584 training patterns rather than learning generalizable relationships. In  
585 contrast, the CatBoost (CB) model displayed a more uniform residual  
586 distribution confined within a narrower band (-1 to +1  $\mu\text{mol}/\text{cm}^2$ ), with no  
587 systematic bias across the range of predicted outputs. This balanced error  
588 profile implies effective generalization and reliable performance on unseen  
589 data.

590 This conclusion is further corroborated by the radar plots in **Fig. 4**, which  
591 enable a multi-metric comparison of model efficacy. CatBoost consistently  
592 outperformed its counterparts, achieving the lowest values of MSE, RMSE,  
593 and MAE while maintaining a high  $R^2$  ( $>0.98$ ) on both training and testing  
594 sets. Crucially, the performance gap between training (pink) and testing  
595 (brown) phases for CB was minimal, particularly in error metrics, suggesting  
596 limited overfitting and strong robustness. The uniformity observed across  
597 datasets underscores CatBoost's suitability for practical deployment in  
598 predicting  $\text{CH}_4$  yields from photocatalytic  $\text{CO}_2$  reduction. This consistency  
599 highlights CatBoost model emerges as the most effective among the ten  
600 evaluated algorithms, distinguished by its exceptional predictive accuracy,  
601 low error rates, balanced generalization capability, and resilience to  
602 overfitting. These attributes position it as a robust and reliable tool for  
603 modeling and optimizing solar-driven  $\text{CO}_2$ -to-fuel conversion processes.



605 **Fig. 4.** The radar plots on training and testing data for CH<sub>4</sub> production (a)  
606 AB, (b) BG, (c) CB, (d) DT, (e) ET, (f) GB, (g) HGB, (h) LGBM, (i) RF, and (j)  
607 XGB models.

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609 **Fig. 5.** The scatter plot representing the association between the  
610 experimental and anticipated CH<sub>4</sub> production for (a) AB, (b) BG, (c) CB, (d)  
611 DT, (e) ET, (f) GB, (g) HGB, (h) LGBM, (i) RF, and (j) XGB models.

### 612 *3.3.2. Prediction of CO production*

613 In the context of photocatalytic CO<sub>2</sub> reduction, accurate prediction of  
614 carbon monoxide (CO) production is pivotal for optimizing reaction  
615 parameters and maximizing process efficiency. To rigorously assess the  
616 predictive capabilities of the ten tree-based machine learning (ML) models  
617 under investigation, a suite of visualization and statistical diagnostic tools,  
618 including scatter plots, residual plots, and radar plots was employed. As  
619 illustrated in **Fig. 6**, the scatter plots comparing predicted versus actual CO  
620 production rates reveal that CB, HGB, LGBM, and XGB achieved the highest  
621 predictive accuracy, with their data points closely aligned along the ideal 1:1  
622 diagonal line. The remaining models GB, ET, RF, BG, AB, and DT also  
623 demonstrated commendable performance, albeit with marginally higher  
624 deviations from the reference line, indicating only minor discrepancies in  
625 their predictive outputs.

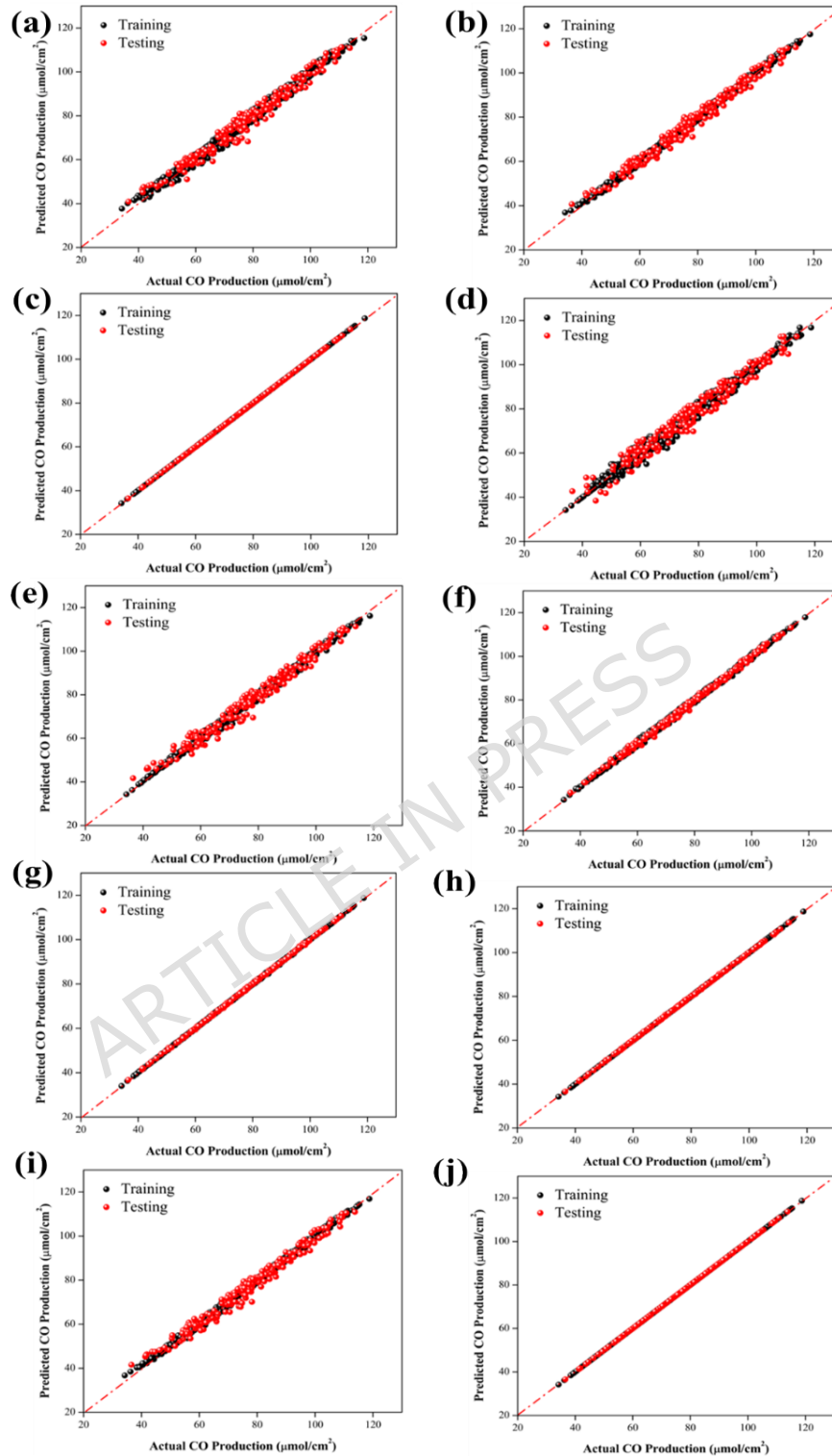
626 To further scrutinize model fidelity and uncover potential systematic  
627 biases, residual analysis was conducted using plots presented in **Fig. S4**.  
628 Residual plots serve as a fundamental diagnostic instrument in regression  
629 modeling, as they elucidate the distribution of prediction errors and help  
630 identify patterns that may indicate overfitting, underfitting, or  
631 heteroscedasticity [53]. In this study, residuals were plotted against the  
632 sorted experimental (actual) CO production values along the x-axis to  
633 facilitate a clearer interpretation of error distribution trends. The residual  
634 patterns for the CB and XGB models were notably well-behaved, exhibiting  
635 random scatter around the zero-error line without discernible structure,  
636 thereby affirming their reliability and robustness in capturing the underlying  
637 data-generating process. Quantitative model comparison was further  
638 supported by a comprehensive set of statistical performance metrics

639 compiled in **Table S4**. During the training phase, the coefficient of  
640 determination ( $R^2$ ) values for AB, BG, CB, DT, ET, GB, HGB, LGB, RF, and  
641 XGB were 0.9838, 0.9874, 0.9885, 0.9789, 0.9777, 0.9844, 0.9817, 0.9724,  
642 0.9755, and 0.9792, respectively. These high  $R^2$  scores, coupled with  
643 consistently strong performance on the independent testing dataset,  
644 underscore the efficacy of Bayesian optimization in fine-tuning  
645 hyperparameters to enhance predictive accuracy across all models.

646 Corresponding MAE values for the training set were recorded as 0.0382  
647 (AB), 0.6985 (BG), 0.0846 (CB), 1.8967 (DT), 0.5972 (ET), 0.5311 (GB),  
648 0.4769 (HGB), 2.1519 (LGBM), 0.8797 (RF), and 0.3762 (XGB). Notably, the  
649 CatBoost model not only achieved the highest  $R^2$  but also exhibited the lowest  
650 error metrics across the board specifically, the smallest MAE, RMSE, and  
651 MedAE, thereby establishing its superiority among all evaluated  
652 algorithms. This conclusion is visually reinforced by the radar plots in **Fig. 7**,  
653 which juxtapose training (blue) and testing (brown) performance across  
654 multiple evaluation criteria. For the CatBoost model, the near-perfect overlap  
655 between training and testing metric profiles indicates minimal overfitting and  
656 exceptional generalization capability. As quantified in Fig. 10c, CatBoost  
657 attained an outstanding training  $R^2$  of 0.9885, accompanied by remarkably  
658 low error values: MSE = 0.0114, RMSE = 0.1066, MAE = 0.0846, and MedAE  
659 = 0.0707. These results reflect a strong concordance between predicted and  
660 observed CO yields, with negligible prediction bias. Moreover, on the testing  
661 dataset, CatBoost maintained high predictive fidelity, achieving an  $R^2$  of  
662 0.9874 and correspondingly low errors (MSE = 0.0358, RMSE = 0.1891, MAE  
663 = 0.1484, MedAE = 0.1187), further validating its robustness and suitability  
664 for real-world application in forecasting CO production from photocatalytic  
665 CO<sub>2</sub> conversion. This model exhibited higher performance matrix values than  
666 other models, especially when predicting larger, more complex, and diverse  
667 datasets [54-56]. HistGradientBoosting (**Fig. 7g**) and XGBoost (**Fig. 7j**)  
668 show remarkable performance, achieving a high coefficient of determination

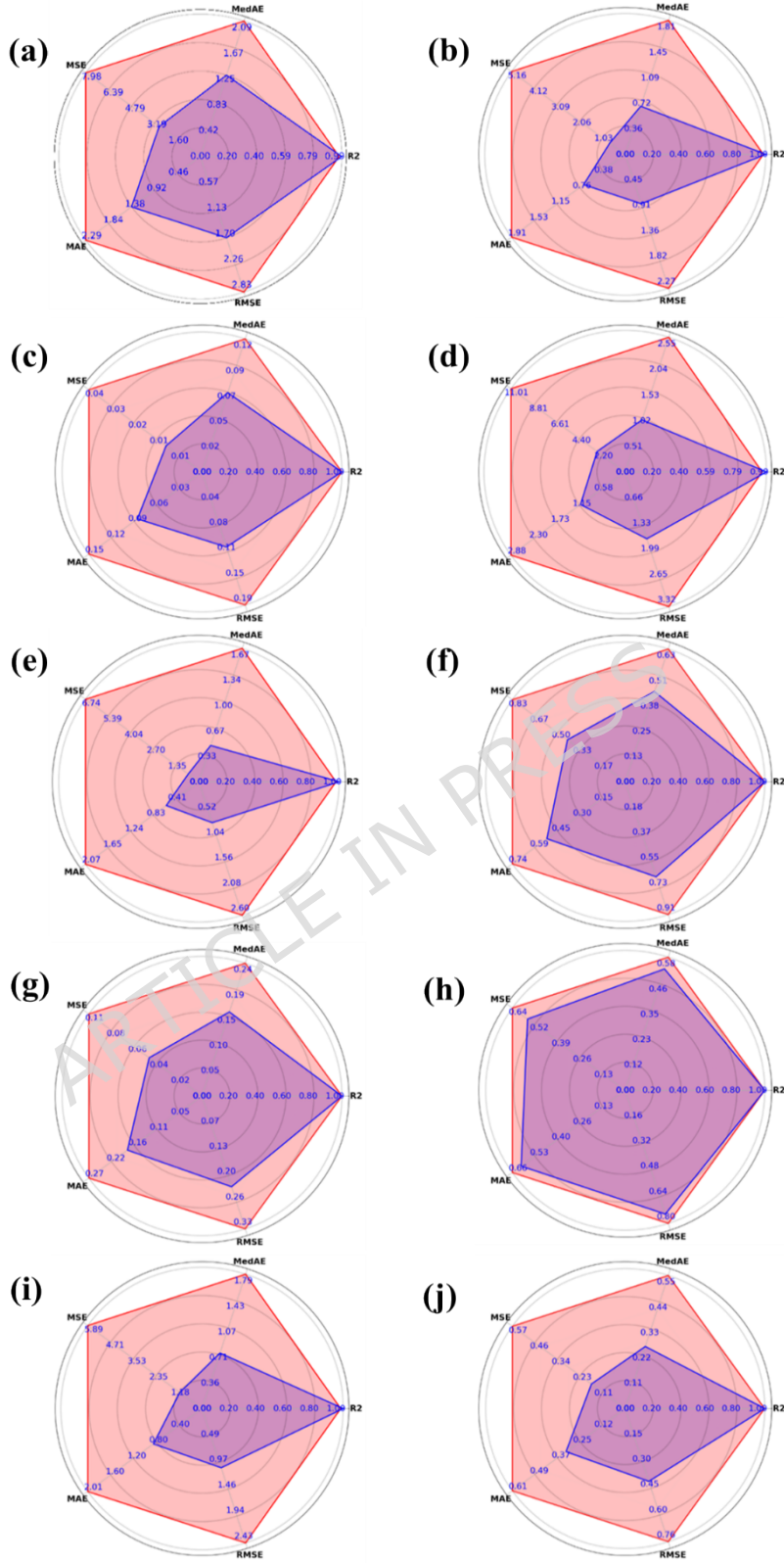
669 ( $R^2$ ) and demonstrating relatively low error metrics. The Bagging (**Fig. 7b**),  
670 ET model (**Fig. 7e**), GB model (**Fig. 7f**), and LightGBM model (**Fig. 7h**),  
671 demonstrate superior training performance ( $R^2 > 0.982$ ). Nevertheless, there  
672 is a less severe drop in performance on the testing dataset, with an  $R^2 >$   
673  $0.985$ . The AdaBoost, and Random Forest, as shown in **Figs. 7a** and **7i**,  
674 respectively, display high precision in training with an  $R^2$  value of more than  
675  $0.98$ . On the other hand, they encounter difficulties when trying to generalize  
676 their performance. On the other hand, the DT (**Fig. 7d**) demonstrates the  
677 lowest robustness compared to other models utilized.

678 In order to circumvent potential leakage issue, we split the data according  
679 to experimental batch/nearest grid cell in groups. This ensures that similar  
680 points never end up in both training and test sets. The hyperparameter tuning  
681 was done inside the nested cross-validation to prevent information leakage,  
682 and the learning curves were checked for overfitting. The permutation testing  
683 of  $\text{CH}_4$  and CO production gave a mean  $R^2$  of  $-0.367$  and  $-0.374$  ( $p < 0.01$ )  
684 respectively, indicating that our model indeed captures real patterns, not  
685 spurious correlations. Outer fold metrics with 95% confidence intervals are  
686  $R^2 = 0.9816$  and  $0.9818$ ,  $\text{RMSE} = 0.0462$  and  $0.2175$ , which shows that the  
687 predictive performance is good but generalized realistically (**Table S5**).  
688 These results confirm that high accuracy in the model is real and not an  
689 artifact of data leakage.



690

691 **Fig. 6.** The scatter plot representing the association between the  
 692 experimental and anticipated CO production for (a) AB, (b) BG, (c) CB, (d)  
 693 DT, (e) ET, (f) GB, (g) HGB, (h) LGBM, (i) RF, and (j) XGB models.



695 **Fig. 7.** The radar plots on training and testing data for CO production (a) AB,  
696 (b) BG, (c) CB, (d) DT, (e) ET, (f) GB, (g) HGB, (h) LGBM, (i) RF, and (j) XGB  
697 models.

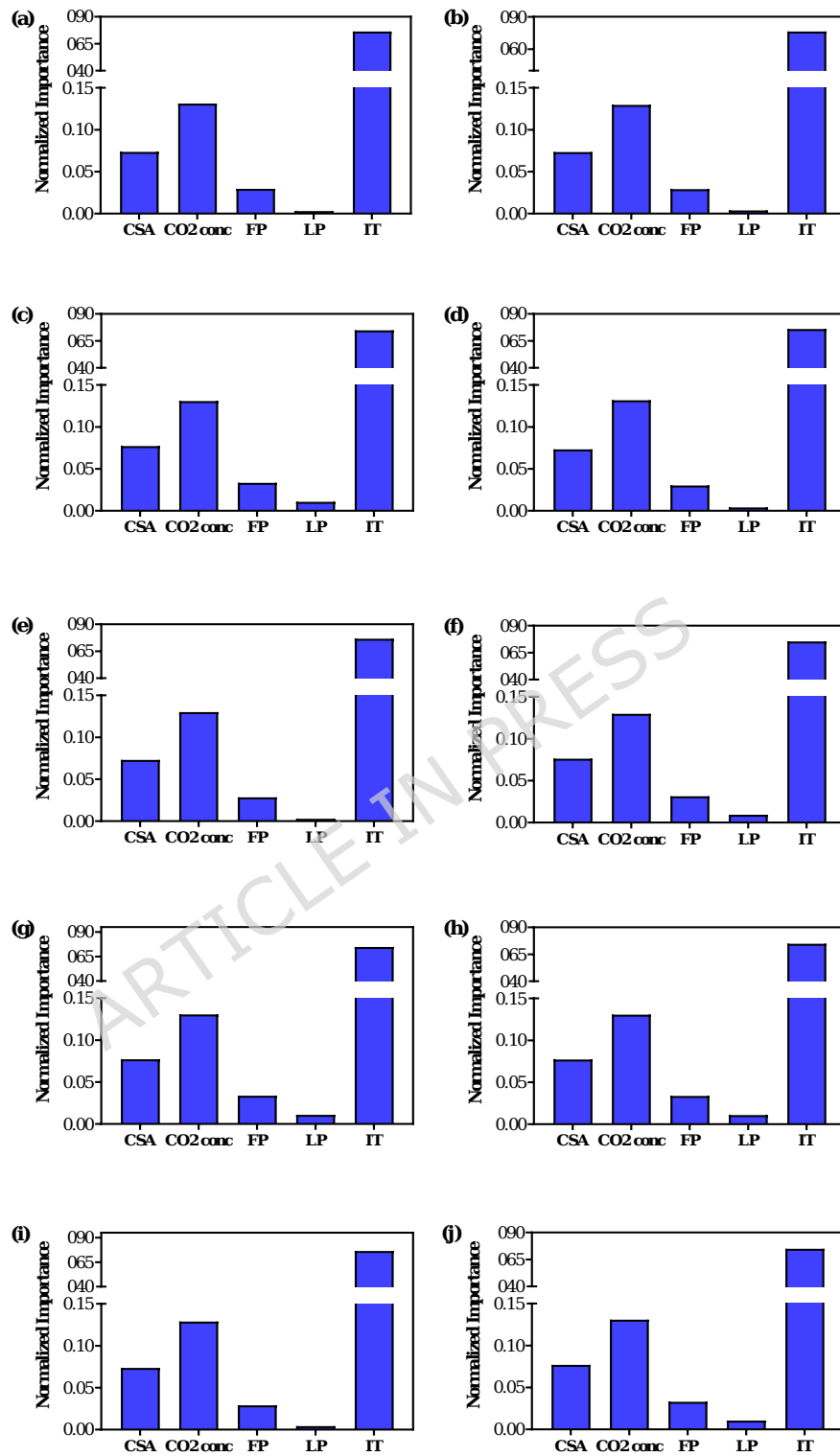
698 The learning curves also show that both CH<sub>4</sub> and CO production models have  
699 high training R<sup>2</sup> consistently at ~1.0, showing an excellent fit on the training  
700 data (**Fig. S5**). Cross-validation scores are low for small training sizes due to  
701 limited samples but increase with the use of more data until reaching a point  
702 of convergence near the training score. This trend indicates a scenario in  
703 which the model generalizes extremely well when sufficient data becomes  
704 available, with very low overfitting for large proportions of training.

### 705 3.3.3. Feature importance and robustness of the models

706 Photocatalytic CO<sub>2</sub> reduction is a complex process influenced by various  
707 experimental and photocatalytic parameters, each of them affecting the  
708 selectivity toward CH<sub>4</sub> and CO production. It is simple to visualize the impact  
709 of input parameters on the targeted variables by using the measure of feature  
710 importance. As shown in **Figs. 8** and **9**, the normalized importance of input  
711 attributes affecting the competence of PC conversion of CO<sub>2</sub> into CH<sub>4</sub> and CO  
712 products had been retrieved for each utilized predictive model. To provide a  
713 better overview, the input parameters were abbreviated as CSA for catalyst  
714 surface area, CO<sub>2</sub> conc. for initial concentration of CO<sub>2</sub>, FP for feed pressure,  
715 LP for light power, and IT for irradiation time. For CH<sub>4</sub> production, the IT was  
716 identified as the most influential factor by all the models due to the fact that  
717 more prolonged exposure allows more chances for better interaction between  
718 CO<sub>2</sub> molecules with the catalyst, which enhanced photoconversion efficiency  
719 [57–59]. This is followed by CO<sub>2</sub> conc., CSA, FP, and LP in descending order  
720 (**Fig. 8**). In CO production, CSA was the most influential parameter,  
721 emphasizing the need for ample active sites, followed by IT, LP, FP, and CO<sub>2</sub>  
722 conc., which had the least effect (**Fig. 9**). Based on the rating of importance  
723 it is apparent that these parameters play a significant role in CH<sub>4</sub> and CO  
724 production. Irradiation time is a crucial parameter in both, showing its

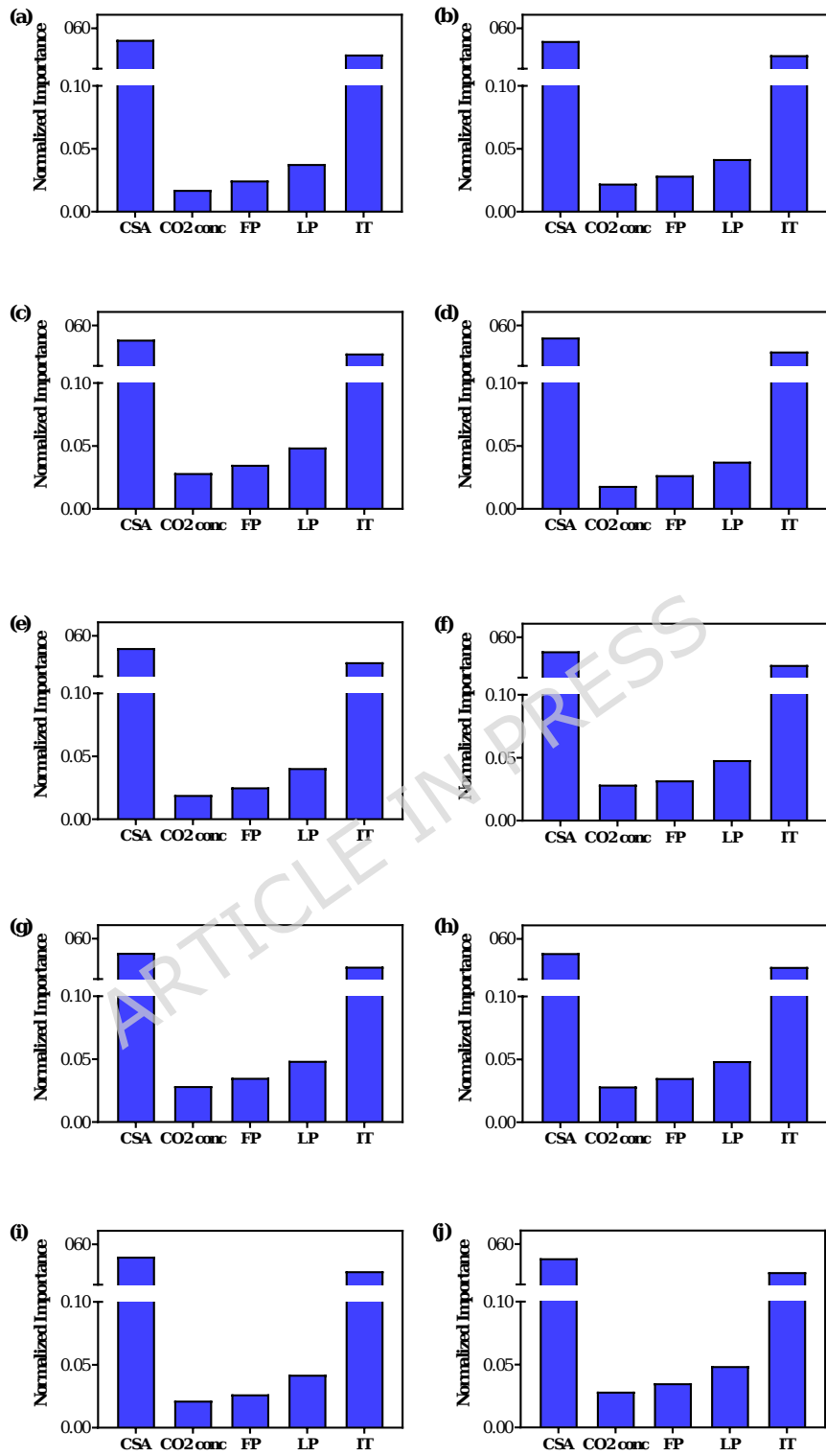
725 importance in maintaining reaction rates for effective conversion. However,  
726 for CH<sub>4</sub>, CO<sub>2</sub> conc. plays a more vital role in ensuring the sufficiency of the  
727 reactant, while catalyst surface area is less critical. The reverse is the case  
728 for the production of CO, with high dependence on CSA and negligible CO<sub>2</sub>  
729 conc. These differences indicate different reaction pathways and  
730 dependencies, which can be of significant value for fine-tuning g-C<sub>3</sub>N<sub>4</sub>/TNTAs  
731 photocatalysts and photocatalytic conditions toward optimum selectivity and  
732 efficiency in the CO<sub>2</sub> reduction process. **Tables S6 and S7** demonstrate the  
733 statistical robustness of the input features concerning the CH<sub>4</sub> and CO  
734 production during photocatalytic CO<sub>2</sub> reduction.

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736 **Fig. 8.** The feature importance matrix of input parameters for CH<sub>4</sub>  
737 production evaluated by (a) AB, (b) BG, (c) CB, (d) DT, (e) ET, (f) GB, (g) HGB,  
738 (h) LGBM, (i) RF, and (j) XGB models.

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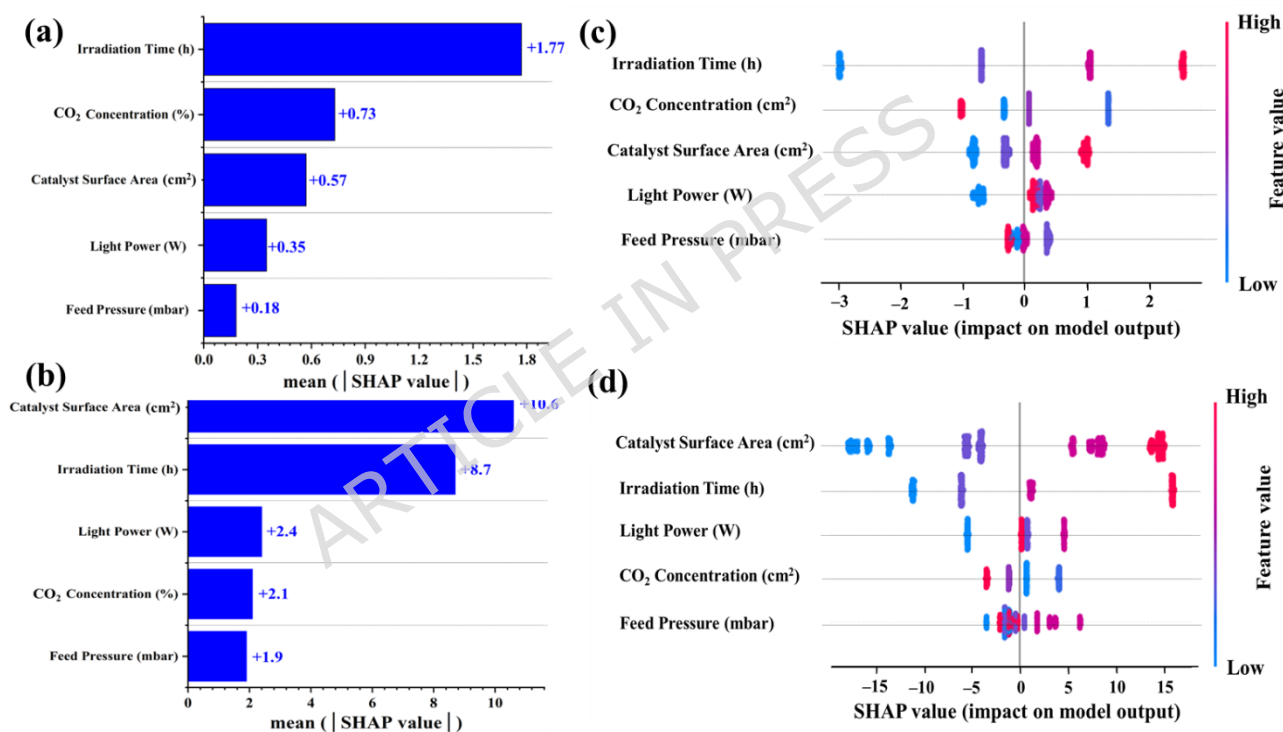


740 **Fig. 9.** The feature importance matrix of input parameters for CO production  
741 evaluated by (a) AB, (b) BG, (c) CB, (d) DT, (e) ET, (f) GB, (g) HGB, (h) LGBM,  
742 (i) RF, and (j) XGB models.

743 Understanding the factors that influence photocatalytic processes is  
744 critical to optimizing the conversion of CO<sub>2</sub> into valuable chemicals such as  
745 CH<sub>4</sub> and CO. In this work, the contribution of key experimental parameters  
746 was quantified using SHapley Additive exPlanations (SHAP) to determine the  
747 global feature importance rankings of the outperformed CB model using g-  
748 C<sub>3</sub>N<sub>4</sub>/TNTAs photocatalysts. For CH<sub>4</sub> production, **Fig. 10a** represents that  
749 the irradiation time showed the most impactful feature in magnitudes of a  
750 mean SHAP value higher than +1.75. Such a feature enabled increasing  
751 interactions between CO<sub>2</sub> molecules with the catalyst. Further, CO<sub>2</sub>  
752 concentration is around +0.73 for enough reactant supply, followed by a  
753 catalyst surface area at around +0.57. The corresponding average SHAP  
754 values, which are close to +0.35 and +0.18, represent these less pronounced  
755 changes in the reaction medium associated with light power and feed  
756 pressure. For CO production, as explained in **Fig. 10b**, the catalyst surface  
757 area became the most crucial factor, where the average SHAP value  
758 surpassed +10.6, showing that the maximization of active sites is essential.  
759 It was followed very closely by irradiation time, with a value above +8.7,  
760 showing it plays a role in sustaining the reaction. On the other hand, light  
761 power, CO<sub>2</sub> concentration, and feed pressure had SHAP values of  
762 approximately +2.4, +2.1, and +1.9, respectively, which describes a lesser  
763 impact. Global feature importance ranks in the CB model have elicited similar  
764 insights: established variables reflect robust evidence for hierarchical effects  
765 and reinforce such findings. These provide a variety of routes and  
766 dependencies on CH<sub>4</sub> and CO production and could well direct efforts at  
767 enhancing the selectivity and efficiency of CO<sub>2</sub> photoreduction via g-  
768 C<sub>3</sub>N<sub>4</sub>/TNTAs composite.

769 The SHAP summary plots of CH<sub>4</sub> and CO production give further insight  
770 into how different experimental parameters influence model predictions for  
771 both processes. For CH<sub>4</sub> production, the most influential factor is identified  
772 to be the irradiation time (**Fig. 10c**). The high values of the irradiation time,  
773 depicted in red, positively influence CH<sub>4</sub> production since it prolongs the  
774 interaction of the CO<sub>2</sub> molecules with the catalyst, enhancing its catalytic  
775 efficiency. The lower values of the same, coloured in blue, affect production  
776 negatively and reduce the overall conversion. The second most critical  
777 parameter is the initial concentration of CO<sub>2</sub>, whereby higher concentrations  
778 in red enhance CH<sub>4</sub> production by ensuring sufficient reaction availability,  
779 while lower concentrations presented in blue decrease efficiency. The  
780 catalyst surface area also has a significant effect: the larger the active surface  
781 area, red, the more it enhances production due to higher catalytic activity,  
782 while smaller surface areas blue hinder the reaction. Among all of these, feed  
783 pressure and light power were found to be less sensitive, while their higher  
784 values also support CH<sub>4</sub> production, though at a lower level. The distribution  
785 of SHAP values for CO production appeared in different hierarchy of features  
786 (**Fig. 10d**). In that case, catalyst surface area was the most important, and  
787 its high value in red signifies enhanced CO production by providing active  
788 sites where the reaction can take place; smaller areas in blue showed reduced  
789 efficiency. The irradiation time is the second crucial factor; the longer the  
790 exposure to irradiation, the more contact and conversion can occur, but the  
791 shorter exposure inhibits the reaction. The generation of CO was more  
792 significantly impacted by light power than CH<sub>4</sub> because CO is favorably  
793 formed by higher light intensities [60-62]. The CO<sub>2</sub> concentration and feed  
794 pressure for CO generation exhibited the least impact. The SHAP analysis of  
795 relative importance underlines these differences in the parameter  
796 dependencies of CH<sub>4</sub> and CO production. Although the irradiation time is  
797 most relevant in both prediction models, the higher CO<sub>2</sub> concentration for  
798 CH<sub>4</sub> production is outweighed by the dominance of the catalyst surface area  
799 in the case of CO production.

800 From the model-agnostic permutation importance analysis, it can be seen  
 801 that the key drivers for CH<sub>4</sub> and CO production are quite different (**Fig. S6**).  
 802 The most influential feature for CH<sub>4</sub> production is irradiation time, since it  
 803 produces the largest drop in R<sup>2</sup> if shuffled, making it the primary driver of  
 804 the output. On the other hand, CO<sub>2</sub> concentration and catalyst surface area  
 805 have a moderate impact, whereas feed pressure and light power contribute  
 806 very little. In contrast, the dominant factor for CO production is catalyst  
 807 surface area. Irradiation time remains important but less so than the former.  
 808 light power contributes moderately, feed pressure minimally, whereas CO<sub>2</sub>  
 809 concentration has the least effect in view of its minimal role in CO prediction.



810  
 811 **Fig. 10.** Global feature importance of CB model using SHAP values (a) The  
 812 importance rankings for CH<sub>4</sub> prediction and (b) CO prediction; (c)  
 813 Distribution of SHAP values for CH<sub>4</sub> prediction and (b) CO prediction.

#### 814 815 3.3.4. Robustness of the best-predicted model

816 In the analysis of PC CO<sub>2</sub> conversion to CH<sub>4</sub> and CO, scatter plots and  
 817 residual plots were utilized to evaluate the predictive accuracy and error

818 distribution of the models, revealing that the CB model demonstrated  
819 superior alignment between predicted and actual values with minimal  
820 systematic bias. Radar plots provided a comparative visualization of  
821 experimental conditions, highlighting the CB model's ability to consistently  
822 outperform other models across diverse parameter spaces. Feature  
823 importance charts and SHAP plots further underscored the interpretability of  
824 the CB model, identifying key influencing factors such as irradiation time and  
825 catalyst surface area, while offering insights into their contributions to the  
826 observed outcomes. Collectively, these analyses confirm the CB model as the  
827 most robust and reliable choice for the tested datasets in predicting and  
828 optimizing CO<sub>2</sub> conversion performance. The performance of the CB model  
829 for training and testing datasets was further investigated using box plot,  
830 violin plot and Taylor diagram (**Fig. S7**). For CH<sub>4</sub> production, the box plots  
831 showed that both the training and testing datasets had a median error close  
832 to zero, which could be taken to mean this model's predictions were  
833 reasonably accurate and relatively unbiased (**Fig. S7a**). The interquartile  
834 range (IQR) is a measure of variability for the central 50 % of data. A small  
835 IQR suggests reliable predictions that are mostly stable, with only a handful  
836 of outliers present. The violin plots visualized the distribution of errors for  
837 the CH<sub>4</sub> production prediction of the CB model. As presented in **Fig. S7b**, the  
838 training errors were roughly within the range from -0.1 to 0.2, and the test  
839 errors extended a little bit more, within the range from -0.1 to 0.3. The Taylor  
840 diagram is supportive, enabling the analysis of performance by comparing  
841 model output and observed data for some crucial metrics: STD, R<sup>2</sup>, and  
842 centered root mean square error. The Taylor diagram showed CH<sub>4</sub> production  
843 with excellent proficiency, with a predicted point lying close to the observed  
844 one (**Fig. S7c**). The standard deviation (STD) was well predicted for the  
845 training dataset with an estimated value of 2.373 compared with the observed  
846 one of 2.381 and an almost perfect correlation coefficient of 0.9836. For the  
847 test dataset, a similarly high-quality estimation was achieved for STD with a

848 predicted value of 2.420 in comparison with the observed 2.435 and a  
849 corresponding correlation coefficient of 0.9825.

850 The robustness of the CB model to predict CO generation efficiency was  
851 further investigated using box plot, violin plot and Taylor diagram (**Fig. S8**).  
852 The CO production errors showed a slightly wider IQR in the testing dataset,  
853 with several outliers as presented in **Fig. S8a**. This suggests that the model  
854 struggles a bit harder to predict the higher values of CO production. Although  
855 overall, the performance of the models is good, the higher variability of CO  
856 production errors shows that further refinement is necessary in feature  
857 selection methods or addressing data imbalances for improving the accuracy  
858 of the predictions. The test errors (-0.75 to 1.25) in violin plots exhibited  
859 considerable variability, where the border range indicated higher complexity  
860 in the proper forecast of its values (**Fig. S8b**). These plots showed the  
861 differences in model performance between the training and testing phases  
862 and highlighted the need to work on the variability in error distributions in  
863 order to achieve better predictive reliability. These results, when plotted on  
864 a Taylor diagram, showed that during training and testing phases the model  
865 bears a strong potential to replicate the variability with a strong linear  
866 relationship. With a correlation coefficient of 0.9818, the training dataset's  
867 predicted STD of 16.504 was nearly identical to the observed one of 16.509,  
868 which was practically desirable. The test dataset similarly showed strong  
869 alignment, with a high correlation coefficient of 0.9831 supporting the  
870 observed STD of 16.521 and the anticipated STD of 16.440. The strong  
871 performance indicates the model's accuracy and dependability in predicting  
872 photocatalytic CO<sub>2</sub> reduction efficiency.

873

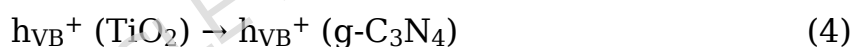
### 874 *3.3.5. Optimization of input variables*

875 **Table 3** summarizes the optimized operational parameters for  
876 photocatalytic CO<sub>2</sub> reduction, alongside corresponding experimental and  
877 model-predicted yields of methane (CH<sub>4</sub>) and carbon monoxide (CO), thereby

878 validating the robustness and predictive fidelity of the proposed machine  
879 learning driven optimization framework. The identified conditions represent  
880 the most favorable configuration for maximizing catalytic efficiency in the  
881 context of TiO<sub>2</sub> nanotube array (TNTAs) - based photocatalysis. For CH<sub>4</sub>  
882 production, the optimal setup comprises a catalyst exposed surface area of  
883 16 cm<sup>2</sup>, an initial CO<sub>2</sub> concentration of 35 vol%, a feed (CO<sub>2</sub> + H<sub>2</sub>O) pressure  
884 of 270 mbar, a light irradiance of 190 W, and an irradiation duration of 4  
885 hours. Under these conditions, pristine TNTAs yielded an experimental CH<sub>4</sub>  
886 production rate of 1.47 μmol/cm<sup>2</sup> with a selectivity of 15.28%. In stark  
887 contrast, the g-C<sub>3</sub>N<sub>4</sub>-modified TNTAs exhibited a markedly enhanced CH<sub>4</sub>  
888 output of 12.15 μmol/cm<sup>2</sup>, representing an approximately 8.25-fold increase  
889 relative to the unmodified catalyst. This substantial improvement is  
890 attributed to the favorable electronic and structural modifications induced by  
891 g-C<sub>3</sub>N<sub>4</sub> integration. Critically, this experimental value aligns almost perfectly  
892 with the model's prediction of 12.17 μmol/cm<sup>2</sup>, differing by a mere 0.02  
893 μmol/cm<sup>2</sup>, thereby underscoring the model's exceptional accuracy in  
894 forecasting photocatalytic performance under optimized conditions. The  
895 enhanced activity of the g-C<sub>3</sub>N<sub>4</sub>/TNTAs heterostructure can be rationalized  
896 through the formation of a Type-II (staggered) band alignment at the  
897 interface. In this configuration, photogenerated electrons in the conduction  
898 band (CB) of g-C<sub>3</sub>N<sub>4</sub> migrate to the CB of TiO<sub>2</sub>, while holes in the valence  
899 band (VB) of TiO<sub>2</sub> transfer to the VB of g-C<sub>3</sub>N<sub>4</sub> (as described in **Eqs. 3** and **4**).  
900 This spatial charge separation effectively suppresses electron-hole  
901 recombination, a key bottleneck in photocatalysis, thereby significantly  
902 augmenting quantum efficiency and overall reaction kinetics.

903 For CO production, the optimization algorithm recommended a distinct  
904 set of conditions: a catalyst surface area of 16 cm<sup>2</sup>, CO<sub>2</sub> concentration of 20  
905 vol%, feed pressure of 280 mbar, light power of 270 W, and irradiation time  
906 of 4 hours. Experimental validation under these parameters yielded CO  
907 production rates of 44.32 μmol/cm<sup>2</sup> for bare TNTAs and 118.50 μmol/cm<sup>2</sup> for

908 **g-C<sub>3</sub>N<sub>4</sub>/TNTAs, with the latter achieving a high selectivity of 84.72% toward**  
 909 **CO.** The close agreement between these empirical results and the model-  
 910 predicted values, evidenced by negligible deviations, further corroborates the  
 911 framework's capacity to accurately simulate and anticipate catalytic behavior  
 912 across diverse product channels. Quantitatively, the final predictive models  
 913 exhibited outstanding statistical performance. For CH<sub>4</sub>, the model achieved  
 914 an R<sup>2</sup> of 0.9864, MSE of 0.0033, RMSE of 0.0578, MAE of 0.0427, and MedAE  
 915 of 0.0341. Similarly, for CO prediction, the metrics were R<sup>2</sup> = 0.9758, MSE  
 916 = 0.0541, RMSE = 0.2326, MAE = 0.1742, and MedAE = 0.1424. These  
 917 results collectively affirm that the Bayesian-optimized machine learning  
 918 model not only captures the complex, nonlinear relationships governing  
 919 photocatalytic CO<sub>2</sub> conversion but also provides a highly reliable tool for  
 920 process design, performance forecasting, and catalyst evaluation in solar fuel  
 921 synthesis applications.



922 The differential evolution (DE) optimization was explicitly constrained to  
 923 the experimental range for all features; no extrapolation beyond the tested  
 924 values was allowed. **Table S8** summarizes the withheld test performance  
 925 metrics of CH<sub>4</sub> and CO, obtained using the CB model, which showed the best  
 926 predictive performance among all tested algorithms. Since new laboratory  
 927 experiments could not be conducted, the model's reliability was established  
 928 by testing its performance with a withheld test set of 205 samples that were  
 929 excluded both during training and tuning of hyperparameters, ensuring true  
 930 out-of-sample performance of the prediction. Therefore, this model has very  
 931 high predictive accuracy, as reflected in the R<sup>2</sup> value of 0.9827 for CH<sub>4</sub> and  
 932 0.9903 for CO, suggesting almost perfect agreement between the predicted  
 933 and withheld experimental values. Low RMSE values of 0.0427 and 0.0567  
 934 for CH<sub>4</sub> and CO, respectively, along with negligible MAE and MedAE, further

935 establish the model as reliable. From the results, it emerges that the CatBoost  
936 model can predict photocatalytic product yields with high accuracy under  
937 novel experimental conditions.

938 The Pareto plots in **Figures S9 and 10** were used to find optimal  
939 experimental conditions by visualizing Pareto fronts for multi-objective  
940 optimization. These plots show that the high CO or CH<sub>4</sub> production in large  
941 measure occurs at or near boundaries of the key experimental variables, with  
942 respect to catalyst exposed surface area, CO<sub>2</sub> concentration, and irradiation  
943 time. They result from a multi-objective optimization that, in parallel, was  
944 performed to maximize product yields (CH<sub>4</sub> or CO) at minimum light power  
945 and thus defines conditions balancing high photocatalytic efficiency with  
946 energy consumption. Such Pareto fronts give, for each product, solutions that  
947 yield the best compromise between maximum production and minimum light  
948 intensity of the corresponding product, showing that the conditions selected  
949 using DE-optimization correspond to true or near-optimum solutions for both  
950 target products. This not only confirms the reliability of the CatBoost-  
951 predicted yields but also yields practical guidelines for experiments under  
952 energy-efficient conditions.

953 As part of the uncertainty assessment, the reliability of the highest CO  
954 and CH<sub>4</sub> production values was interrogated with respect to the five nearest  
955 experimental neighbors in **Table S9**. For CO, the distance-weighted mean  
956 and the very minimal standard deviation ( $\pm 3.32\%$ ) indicate that the  
957 surrounding experiments display minimal variation in CO production,  
958 suggesting that the peak value of CO is both locally consistent and supportive  
959 of the dataset's underlying trends. In contrast, the uncertainty for CH<sub>4</sub> is  
960 relatively higher ( $\pm 8.08\%$ ), reflecting greater variability among the proximal  
961 experiments and suggesting that the maximum CH<sub>4</sub> point is somewhat less  
962 stable in its local experimental neighborhood. Using five neighbors increases  
963 the robustness of the analysis, as it captures a more representative and  
964 reliable snapshot of the local data distribution. Overall, these findings show

965 that uncertainty quantification provides a stringent and data-driven means to  
 966 assess the credibility of the maximum production values measured.

967 These findings highlight the effectiveness of the optimization framework  
 968 and support its ability to lessen trial-and-error in experimental setups. The  
 969 framework will enable the exploration of optimal reaction parameters by  
 970 accurately predicting production values, thereby conserving resources and  
 971 saving time. The high accuracy achieved for various reactions, such as CH<sub>4</sub>  
 972 and CO, underscores the framework's adaptability and utility across a broad  
 973 range of catalytic processes. This advancement is crucial for developing  
 974 greener and economically feasible methods for chemical production,  
 975 positioning this framework as a valuable asset in the field of catalysis,  
 976 especially for the photocatalytic conversion process utilizing TNTA's.

977

978

979 **Table 3.** Optimized input variables to achieve maximum products.

Catalysts	Products	Catalyst surface area (cm <sup>2</sup> )	CO <sub>2</sub> concentration (%)	Feed Pressure (mbar)	Light power (W)	Irradiation time (h)	Predicted production (μmol/cm <sup>2</sup> )	Experimental production (μmol/cm <sup>2</sup> )
TNTAs g-C <sub>3</sub> N <sub>4</sub> /TNTAs	CH <sub>4</sub>	16	35	270	190	4	1.23	1.47
	CO	16	20	280	270	4	46.25	44.32
	CH <sub>4</sub>	16	35	270	190	4	12.17	12.15
	CO	16	20	280	270	4	118.72	118.50

980

#### 981 4. Conclusion

982 The gas-phase photocatalytic (PC) reduction of CO<sub>2</sub> into value-added  
 983 fuels, specifically methane (CH<sub>4</sub>) and carbon monoxide (CO), using graphitic  
 984 carbon nitride (g-C<sub>3</sub>N<sub>4</sub>)-modified TiO<sub>2</sub> nanotube arrays (TNTAs) constitutes a

985 pivotal advancement toward sustainable energy generation and atmospheric  
986 CO<sub>2</sub> mitigation. This study demonstrates the successful integration of tree-  
987 based machine learning (ML) methodologies to not only predict but also  
988 strategically optimize the yields of CH<sub>4</sub> and CO in a gas-phase photocatalytic  
989 system. Comprehensive model evaluation, grounded in a suite of regression  
990 performance indicators including the R<sup>2</sup>, MSE, RMSE, MAE, and MedAE-  
991 unequivocally established CatBoost (CB) as the superior predictive algorithm  
992 across all assessed metrics. Specifically, the CatBoost model exhibited  
993 exceptional performance in forecasting CH<sub>4</sub> production, achieving R<sup>2</sup> scores  
994 of 0.9887 on the training set and 0.9883 on the testing set. Similarly, for CO  
995 prediction, it attained R<sup>2</sup> values of 0.9885 (training) and 0.9874 (testing),  
996 underscoring its high fidelity, minimal bias, and robust generalization  
997 capability. The consistency between two complementary interpretability  
998 techniques, normalized feature importance and SHAP values, further  
999 reinforces the credibility of the model's insights and provides a coherent,  
1000 physically interpretable understanding of how input variables jointly  
1001 influence photocatalytic outcomes. According to the optimized CatBoost  
1002 model, the relative influence of operational parameters on product formation  
1003 follows a clear hierarchy: **catalyst exposed surface area emerged as the most**  
1004 **dominant factor, followed by irradiation time, light power, initial CO<sub>2</sub>**  
1005 **concentration, and, to a significantly lesser extent, feed pressure.** This  
1006 ranking aligns well with established photocatalytic principles, where surface  
1007 area governs active site availability, irradiation duration dictates charge  
1008 carrier utilization, and light intensity modulates excitation efficiency, thereby  
1009 validating both the model's internal logic and the underlying reaction  
1010 mechanisms. These data-driven insights offer actionable guidance for  
1011 experimental design, enabling researchers to rationally engineer  
1012 photocatalytic systems with enhanced efficiency for CO<sub>2</sub>-to-fuel conversion.  
1013 By leveraging ML-guided optimization, the need for labor-intensive, iterative  
1014 trial-and-error experimentation is substantially reduced, leading to  
1015 significant savings in time, resources, and material costs. Moreover, the high

1016 predictive accuracy and interpretability of the CatBoost framework facilitate  
1017 the rapid identification of optimal operational windows, accelerating the  
1018 development of next-generation photocatalysts. Critically, the study also  
1019 highlights the exceptional promise of g-C<sub>3</sub>N<sub>4</sub>/TNTAs heterostructures as  
1020 high-performance platforms for solar-driven CO<sub>2</sub> valorization, capable of  
1021 achieving markedly elevated production rates of CH<sub>4</sub> and CO under optimized  
1022 conditions. Taken together, these findings underscore the transformative  
1023 potential of integrating advanced machine learning with materials science to  
1024 advance sustainable photocatalytic technologies for renewable fuel synthesis  
1025 and carbon neutrality.

1026

#### 1027 **CRedit authorship contribution statement**

1028 **Md. Arif Hossen:** Conceptualization, Methodology, Data collection, Data  
1029 analysis, Writing-original draft, Writing - review & editing. **Meherunnesa**  
1030 **Prima:** Data curation, Methodology, Software, Visualization, Writing -  
1031 review & drafting. **Azrina Abd Aziz:** Funding acquisition, Project  
1032 administration, Writing- review & editing. **Nadeem A Khan:**  
1033 Conceptualization, Software, Writing - review & editing. **Yunus Ahmed:**  
1034 Conceptualization, Software, Supervision, Visualization, Writing - review &  
1035 editing.

1036

#### 1037 **Conflicts of interest**

1038 The authors affirm that none of the findings in this research may have  
1039 been impacted by any known competing financial interests or personal  
1040 relationships.

1041

#### 1042 **Data availability**

1043 Data will be made available on request to corresponding authors.

1044

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